# **Neutronics Exercises**

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# 16 Reactivity feedbacks

# 16.1 Doppler effect reactivity

#### **Exercise description:**

Consider the following situation:

In a reactor fuelled with  $^{235}U$  and with  $\Lambda = 10^{-3}$  s, the average fuel temperature (Tc) changes suddenly from 400°C to 1050°C.

- (a) What is the step change in reactivity (in \$), if the fuel temperature (Doppler) coefficient is: (i)  $+3.10^{-6}$ /°C, (ii)  $-1.10^{-5}$ /°C? Assume that there are no other changes such as control rod movements, change in moderator temperature, etc.
  - (b) What is the stable period in the two cases?
- (c) Estimate the corresponding values, assuming the complete absence of delayed neutrons.

Knowledge to be applied:  $\rho_s = \Delta T_c \alpha_c$ ,

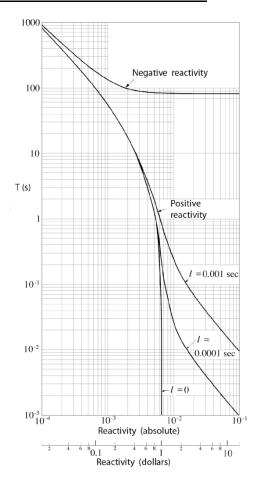
figure, 
$$T' = \frac{\Lambda}{|\rho|}$$

**Expected results:** (a, i)  $\rho_s = 30$ ¢

(a, ii) 
$$\rho_s = -1$$
\$

(b, i) 
$$T(30c) = 20s$$
 (b, ii)  $T(-1s) = 85s$ 

$$(c, i) T' = 0.51s (c, ii) T' = 0.15s$$



## 16.2 Doppler coefficient

#### **Exercise description:**

The temperature dependence of the resonance integral for fertile captures may be expressed by the following empirical relation:  $I_{\rm eff}(T_c) = I_{\rm eff}(300^{\circ}K) \left[1 + C\left(\sqrt{T_c} - \sqrt{300}\right)\right]$ , where  $T_c$  is the fuel temperature in K, and C is a function of the fuel properties.

Constant C is given approximately by:  $C = C_1 + (C_2/a\rho)$ , where  $C_1$ ,  $C_2$  are constants for a given fuel type, a is the fuel radius in cm, and  $\rho$  is the fuel density in  $g/cm^3$ .

- (a) Show that, for a thermal reactor, the resulting expression for the fuel temperature coefficient (due to broadening of the resonances) is:  $\alpha_c = -\frac{c}{2\sqrt{T_c}} \ln\left[\frac{1}{p(300^\circ K)}\right]$ , where p is the resonance escape probability. Consider now a reactor fuelled with metallic uranium ( $\rho$ =19.1 g/cm<sup>3</sup>), in which p=0.878 for T<sub>c</sub>=300K. The fuel rods have a diameter of 2.8 cm.
- (b) Calculate the Doppler coefficient corresponding to a fuel temperature of (i) 450°C, (ii) 1100°C, using appropriate data from the table. N.B.:  $\alpha_c \simeq \frac{1}{k} \frac{\mathrm{dk}}{\mathrm{dT}_c} \simeq \frac{1}{p} \frac{\mathrm{dp}}{\mathrm{dT}_c}$  with  $p = \exp\left(-\frac{N_c V_c I_{\mathrm{eff}}}{\xi_m N_m V_m}\right)$

Combustible	C <sub>1</sub> [10 <sup>-4</sup> ]	C <sub>2</sub> [10 <sup>-2</sup> ]
U <sup>238</sup> (métal)	48	1.28
U <sup>238</sup> (oxyde)	61	0.94
Th (métal)	85	2.68
ThO <sub>2</sub>	97	2.40

Knowledge to be applied: 
$$\alpha_c \simeq \frac{1}{p} \frac{\mathrm{dp}}{\mathrm{dT}_c}$$
,  $p = \exp\left(-\frac{N_c V_c I_{\mathrm{eff}}}{\xi_m N_m V_m}\right)$ ,  $I_{\mathrm{eff}}(T_c) = I_{\mathrm{eff}}(300^\circ K)[1 + C(\sqrt{T_c} - \sqrt{300})]$ 

Expected results: (a) 
$$\alpha_c = -\frac{c}{2\sqrt{T_c}} \ln \left[ \frac{1}{p(300^\circ K)} \right]$$

(b, i) 
$$\alpha_c(723^{\circ}K) = -1.28 \times 10^{-5}/^{\circ}C$$
 (b, ii)  $\alpha_c(1373^{\circ}K) = -9.3 \times 10^{-6}/^{\circ}C$ 

### 16.3 Shut down margin

#### **Exercise description:**

Consider a homogeneous thermal reactor, fuelled with highly enriched uranium (i.e. with p= $\epsilon$ =1), which is critical at a temperature of 230°C. The reactor is shut down and the temperature drops to the ambient value of 20°C. The change in temperature modifies the fuel and moderator cross-sections, such that the reactor parameters vary

	230 °C	20 °C
$\eta_{\rm c}$	2.055	2.060
f	0.592	0.596
$M^2$ (cm <sup>2</sup> )	32.0	31.5

according to the values in the table. The delayed neutron fraction for U-235 is equal to 0.0065.

- (a) What is the critical size of the reactor at 230°C, assuming spherical geometry?
- (b) Estimate the minimal reactivity worth of control rods needed to ensure a safety margin of 2\$ for the reactor's shutdown state at 20°C. You may neglect the changes in density and dimensions with temperature.

**Knowledge to be applied:**  $B^2 = \left(\frac{\pi}{R_e}\right)^2 = B_m^2 = \frac{k_{\infty} - 1}{M^2}$ ,  $k_{\text{eff}} = \frac{k_{\infty}}{1 + B^2 M^2}$ , safety margin of 2\$,

**Expected results:** (a)  $R_e = 38.2 \text{cm}$  (b)  $\rho_{\text{min}} = 3.8$ \$

## 16.4 Reactivity coefficients

#### **Exercise description:**

In a certain PWR, the total reactivity associated with going from cold to hot power conditions for the moderator is -\$ 6.00 and that associated with the fuel is -\$ 4.14. In this reactor cold temperature is  $T_c\!\!=\!\!20$  C; mean moderator operating temperature is  $T_H\!\!=\!\!320$  C; and the mean fuel operating temperature is  $T_f\!\!=\!\!1700$  C . Find the moderator and fuel temperature reactivity coefficients.

**Expected results:**  $\alpha_M = -0.02 \ \text{s/°C}; \ \alpha_F = -0.00246 \ \text{s/°C}$