Plasma I

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Exercise 1

Evaluate the value of the speeds $\sqrt{\langle v_x^2 \rangle}$, $\sqrt{\langle \vec{v}^2 \rangle}$ and $\langle |\vec{v}| \rangle$ as a function of the thermal velocity defined as $v_{th\alpha} = \sqrt{\frac{T_{\alpha}}{m_{\alpha}}}$ for a maxwellian distribution:

$$f_{\alpha}(\vec{v}) = \left(\frac{m_{\alpha}}{2\pi T_{\alpha}}\right)^{3/2} \exp\left(-\frac{m_{\alpha}}{2T_{\alpha}}\vec{v}^{2}\right)$$

Exercise 2

To produce a plasma, a cylindrical vacuum tube (length l=2m, radius a=1m) is pumped down to a base pressure $p<10^{-8} {\rm torr}$ (760torr is the atmospheric pressure), and then filled with Argon (ionization energy 15.8 eV) at $p=10^{-3} {\rm torr}$ that you can assume to be at room temperature. A mono-energetic electron beam (radius $r=10 {\rm cm}$, total current $I=1 {\rm A}$ and energy $U_e=30 {\rm eV}$) is injected along the axis of the tube using an electron gun.

- a.) Evaluate the total number of ions per second produced in the tube by the impact of the electrons on the neutrals.
- b.) Assuming no recombination and no fueling of gas, how long could we maintain this discharge?

Suppose to have an ionisation cross-section for electrons at 30eV of $\sigma_{ion} \sim 10^{-20} \text{m}^2$.

Exercise 3

Semi-conductor manufacturers use plasma during surface treatment of materials. In a vacuum chamber of $0.5 \text{m} \times 0.5 \text{m} \times 0.5 \text{m}$ dimensions, an inert gas is partially ionised by radio waves.

Consider the case where the gas used is Argon that you can assume to be at room temperature ($p=10^{-4} {\rm torr}$, $n_e=10^{16} {\rm m}^{-3}$, $T_e=3 {\rm eV}$, and $T_i=0.1 {\rm eV}$ -first ionisation):

- a.) Calculate the relative ionisation degree of the gas used.
- b.) Estimate the collision frequency (electron-neutral ν_{en}) assuming a cross section of $\sigma = 1000\pi a_0^2$, where $a_0 = 5.29 \times 10^{-11}$ m is the Bohr radius.
- c.) Can we consider this gas as a plasma? Why?