

SOLID STATE PHYSICS III

Fall Semester 2023 PHYS-419

Andreas Läuchli LLTCP @ EPFL & LTC @ PSI

> Tianyue Huang LLTCP @ EPFL

FQH EFFECT, LAUGHLIN WF

Pseudopotentials for Coulomb interactions

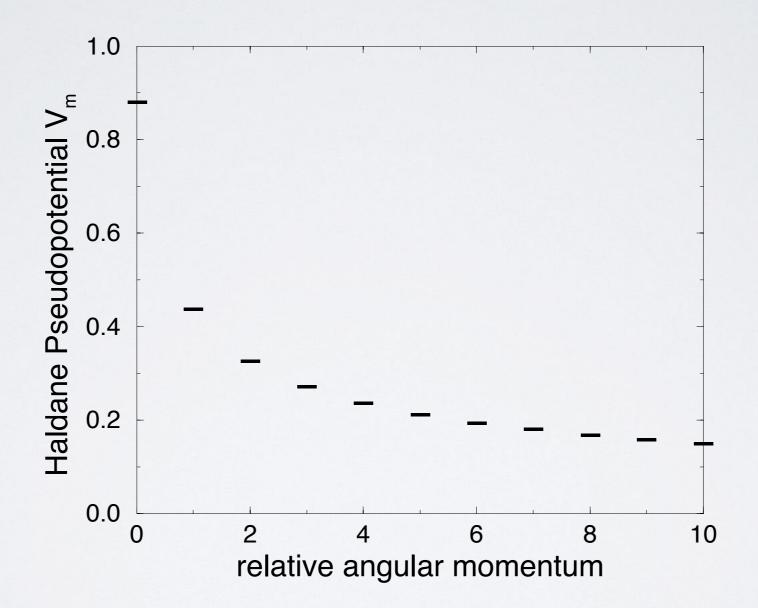


Figure 2: The Haldane pseudopotential V_m vs. relative angular momentum m for two particles interacting via the Coulomb interaction. Units are $e^2/\epsilon \ell$, where ϵ is the dielectric constant of the host semiconductor and the finite thickness of the quantum well has been neglected.

FQH EFFECT, LAUGHLIN WF

Snapshots of Laughlin wave function

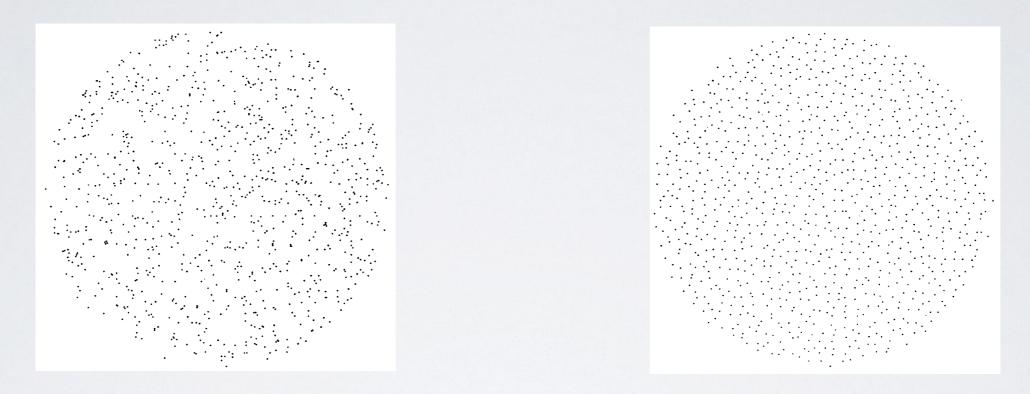
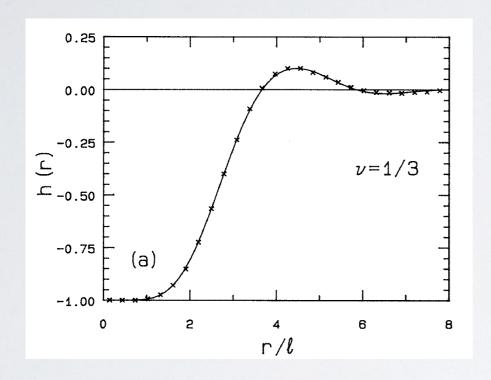


Figure 4: Comparison of typical configurations for a completely uncorrelated (Poisson) distribution of 1000 particles (left panel) to the distribution given by the Laughlin wave function for m=3 (right panel). The latter is a snapshot taken during a Monte Carlo simulation of the distribution. The Monte Carlo procedure consists of proposing a random trial move of one of the particles to a new position. If this move increases the value of $|\Psi|^2$ it is always accepted. If the move decreases the value of $|\Psi|^2$ by a factor p, then the move is accepted with probability p. After equilibration of the plasma by a large number of such moves one finds that the configurations generated are distributed according to $|\Psi|^2$. (After R. B. Laughlin, Chap. 7 in [2].)

FQH EFFECT, LAUGHLIN WF

Density correlations in the Laughlin wavefunction



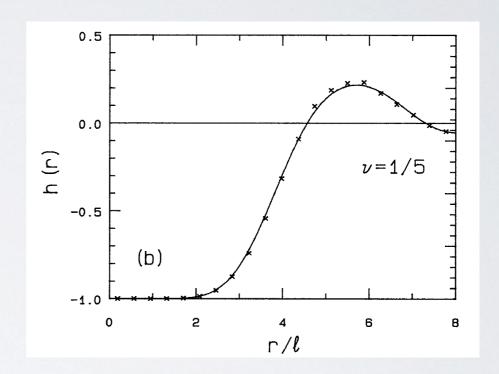


Figure 5: Plot of the two-point correlation function $h(r) \equiv 1 - g(r)$ for the Laughlin plasma with $\nu^{-1} = m = 3$ (left panel) and m = 5 (right panel). Notice that, unlike the result for m = 1 given in eq. (46), g(r) exhibits the oscillatory behavior characteristic of a strongly coupled plasma with short-range solid-like local order.