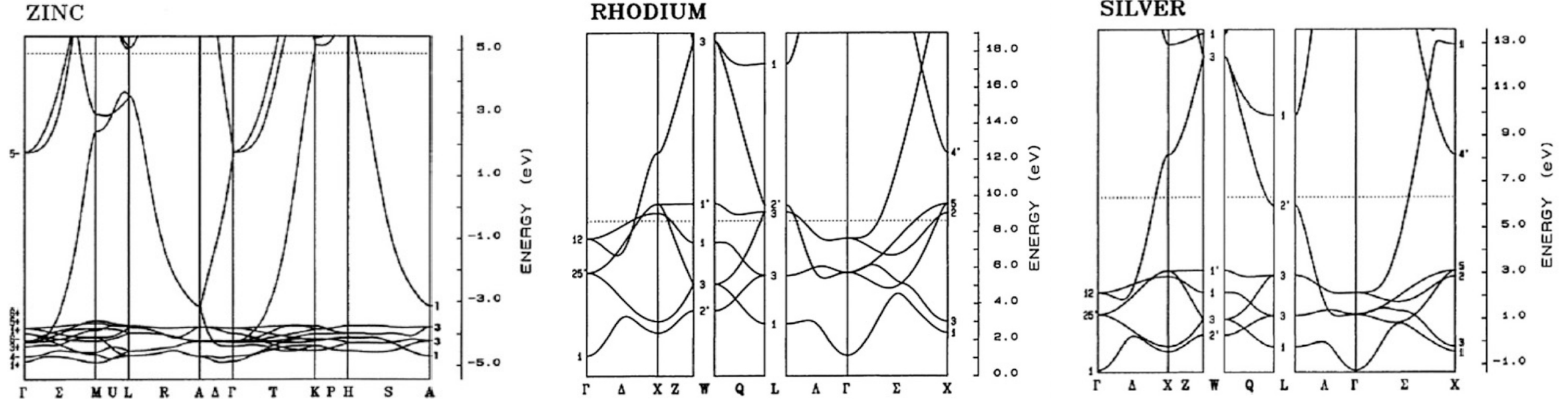


Magnetic alloy

We want to form a magnetic alloy with high magnetic moment mixing Co with one of these three elements, which are not magnetic in bulk: Zn, Rh, Ag.

Considering their band structure, class them according to the suitability.



Solution: Magnetic alloy

The magnetic moment of the alloy is an average of the magnetic moment of Co and of the second element.

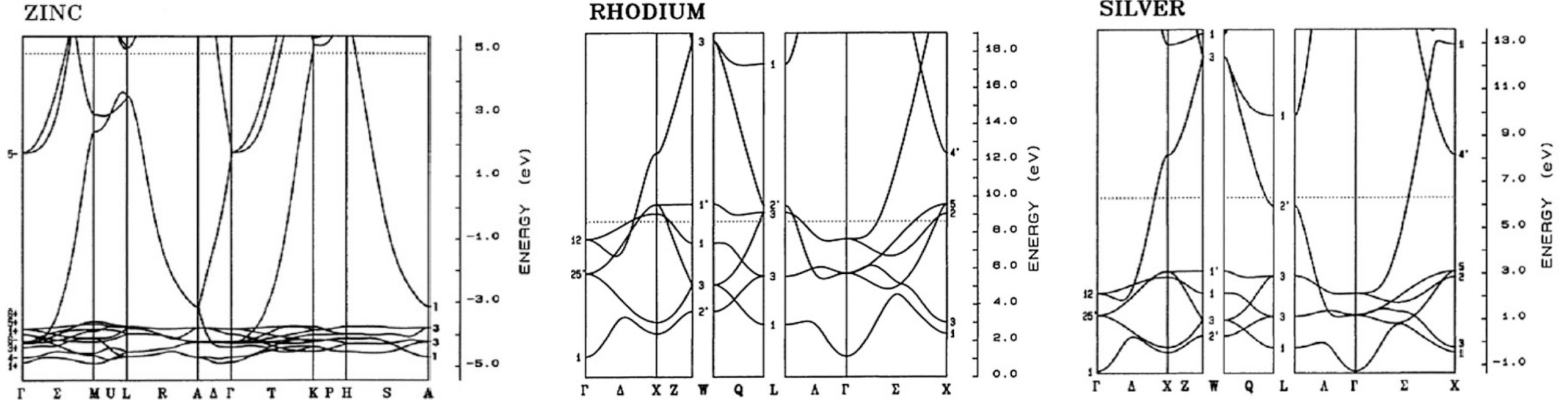
The necessary condition to have a contribution of the second element is a high d-state DOS at the Fermi level.

Then the three elements can be classified in the following order:

Rh

Ag

Zn



Magnetic moments

We want to evaluate the magnetic moment of atoms in several situations. We apply an external magnetic field B applied along the z direction and for simplicity we assume $T = 0$ K.

- 1) Calculate the magnetic moment of a free-standing Co (Ar $3d^7 4s^2$), Sm (Xe $4f^6 6s^2$) and Dy (Xe $4f^{10} 6s^2$) atom
- 2) Calculate the magnetic moment of a Co atom in bulk Co knowing that $n_{3d}(\downarrow) = 5.0$, $n_{3d}(\uparrow) = 3.3$, $n_{4s}(\downarrow) = 0.35$, $n_{4s}(\uparrow) = 0.35$ where n_{3d} and n_{4s} the number of electrons with spin down/up in the respective band
- 3) Consider the composites SmCo_5 and DyCo_5 . In both composites the magnetic moment of the Co atoms is anti-parallel to the magnetic moment of the rare earth element. Assume for Co the electronic configuration $n_{3d}(\downarrow) = 5.0$, $n_{3d}(\uparrow) = 3.0$, $n_{4s}(\downarrow) = 0.35$, $n_{4s}(\uparrow) = 0.35$. For the rare earth assume the standard (Xe $4f^{N-1} 5d^1 6s^2$) configuration. In addition, the electron in the $5d$ band occupies the orbital with $L_z = 0$ and its spin is parallel to the spin of the $4f$ shell. What is the magnetic moment per unit formula?

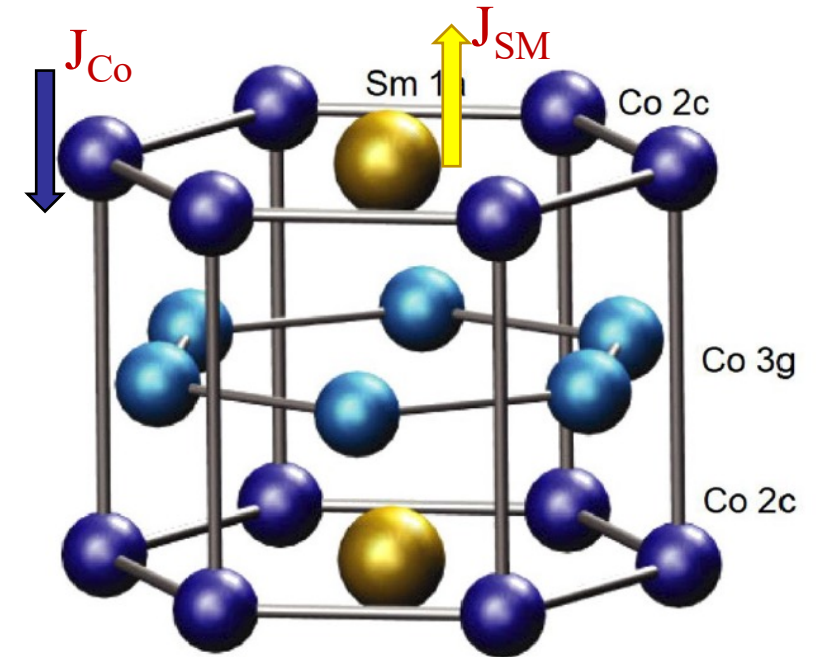
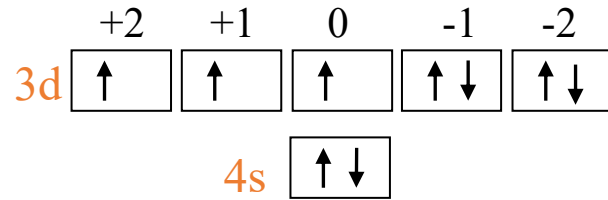


FIG. 1. Unit cell of the hexagonal intermetallic SmCo_5 .

Solution: magnetic moments

1)

Ground state of Co (Ar 3d⁷ 4s²)



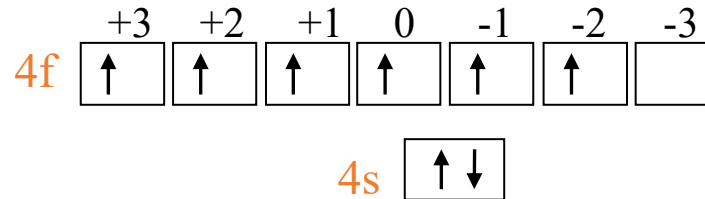
$$L = 3, S = 3/2, J = 9/2$$

$$m_L = L \mu_B = 3 \mu_B,$$

$$m_S = 2 S \mu_B = 3 \mu_B,$$

$$m_{at} = g J \mu_B = 6 \mu_B$$

Ground state of Sm (Xe 4f⁶ 6s²)



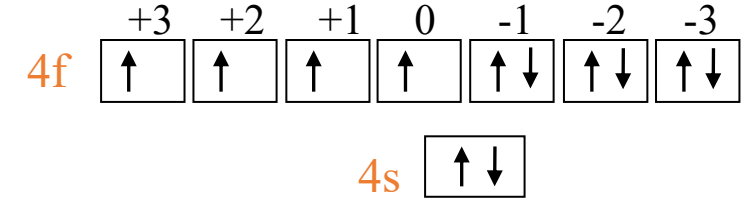
$$L = 3, S = 3, J = 0$$

$$m_L = L \mu_B = 3 \mu_B,$$

$$m_S = 2 S \mu_B = 6 \mu_B,$$

$$m_{at} = g J \mu_B = 0 \mu_B$$

Ground state of Dy (Xe 4f¹⁰ 6s²)



$$L = 6, S = 2, J = 8$$

$$m_L = L \mu_B = 6 \mu_B,$$

$$m_S = 2 S \mu_B = 4 \mu_B,$$

$$m_{at} = g J \mu_B = 10 \mu_B$$

2)

In bulk the orbital moment is quenched; thus, $L = 0$

Using the occupation number $n_{3d}(\downarrow) = 5.0$, $n_{3d}(\uparrow) = 3.3$, $n_{4s}(\downarrow) = 0.35$, $n_{4s}(\uparrow) = 0.35$, for the spin we obtain a contribution of $m_S = 2 \cdot \frac{1}{2} \cdot 1.7 = 1.7 \mu_B$ from the 3d band and a contribution of $m_S = 0$ from the 4s band. Thus, $m_{at} = 1.7 \mu_B$

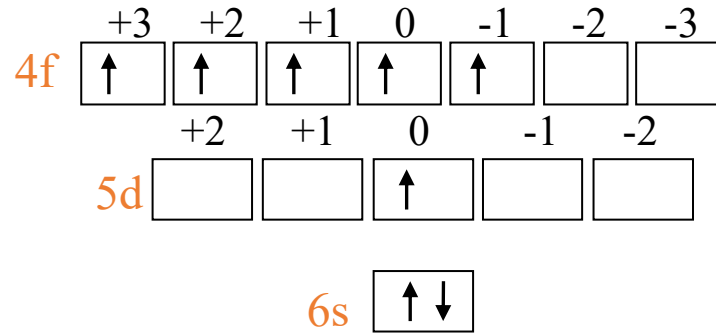
Solution: magnetic moments

3) Co contribution: in bulk the orbital moment is quenched thus $L = 0$

Using the occupation number $n_{3d}(\downarrow) = 5.0$, $n_{3d}(\uparrow) = 3.0$, $n_{4s}(\downarrow) = 0.35$, $n_{4s}(\uparrow) = 0.35$, for the spin we obtain a contribution of $m_S = 2 \cdot \frac{1}{2} \cdot 2 = 2.0 \mu_B$ from the 3d band and a contribution of $m_S = 0$ from the 4s band. Thus, $m_{Co} = 2 \mu_B$ in both composite.

Rare earth contribution can be calculated with Hund's rules

Ground state of Sm ($Xe 4f^5 5d^1 6s^2$)



$$4f: L = 5, S = 5/2, J = 5/2$$

$$m_{4f} = g J \mu_B = 5/7 \mu_B$$

$$5d: L = 0, S = 1/2, J = 1/2$$

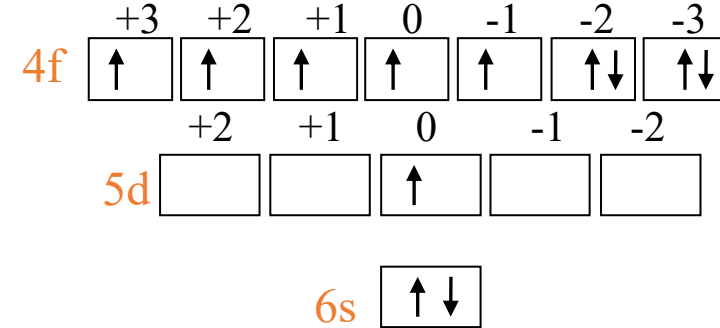
$$m_{5d} = g J \mu_B = 1 \mu_B$$

$$m_{6s} = g J \mu_B = 0 \mu_B$$

$m_{Sm} = 2/7 \mu_B$ (S_{5d} is parallel to S_{4f} but since $L_{4f} > S_{4f}$, J_{4f} is parallel to L_{4f} and antiparallel to S_{4f})

$$m_{u.f.} = 5 m_{Co} - m_{Sm} = 68/7 \mu_B$$

Ground state of Dy ($Xe 4f^9 5d^1 6s^2$)



$$4f: L = 5, S = 5/2, J = 15/2$$

$$m_{4f} = g J \mu_B = 10 \mu_B$$

$$5d: L = 0, S = 1/2, J = 1/2$$

$$m_{5d} = g J \mu_B = 1 \mu_B$$

$$m_{6s} = g J \mu_B = 0 \mu_B$$

$$m_{Dy} = 11 \mu_B$$

$$m_{u.f.} = 5 m_{Co} - m_{Dy} = -1 \mu_B$$