## Swiss Plasma Center

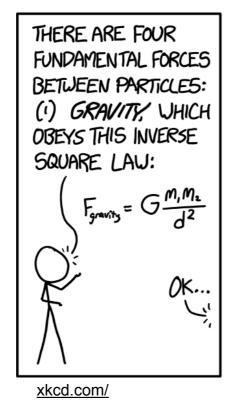
# General Physics: Mechanics

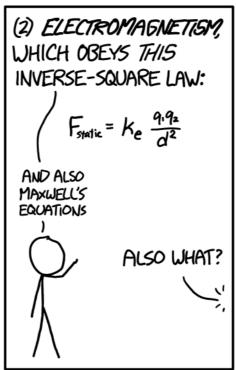
**PHYS-101(en)** 

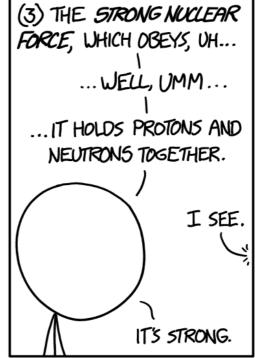
Lecture 3a:

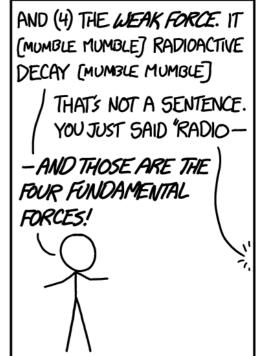
**Newton's laws of motion** 

Dr. Marcelo Baquero marcelo.baquero@epfl.ch September 23rd, 2024









## Today's agenda (Serway 5, MIT 7-8)



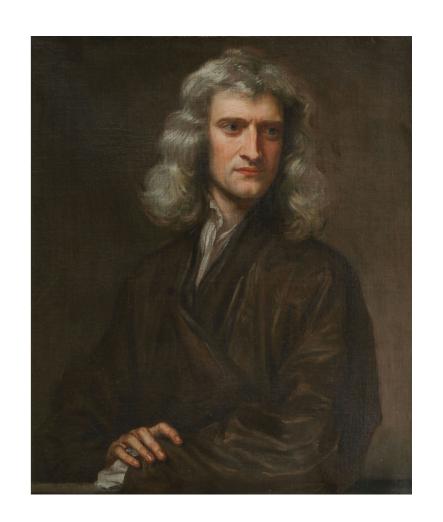
- 1. Finish discussion on projectile motion
- 2. Newton's laws of motion:
  - 1. Newton's 1st law of motion
  - 2. Newton's 2nd law of motion
  - 3. Newton's 3rd law of motion
- And along the way we'll conceptualize
  - Force

Friction

Mass

Springs

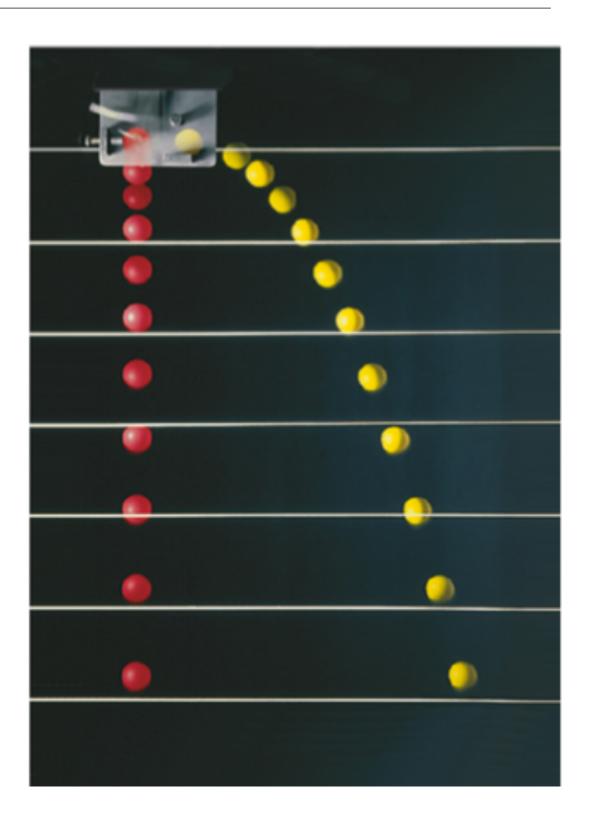
- Frames of reference
- Free body diagrams





## Projectile motion

- Two balls are released simultaneously under gravity
- What causes the difference in their motions?
- What equations of motion need modified?





## Velocity throughout projectile motion

Projectile

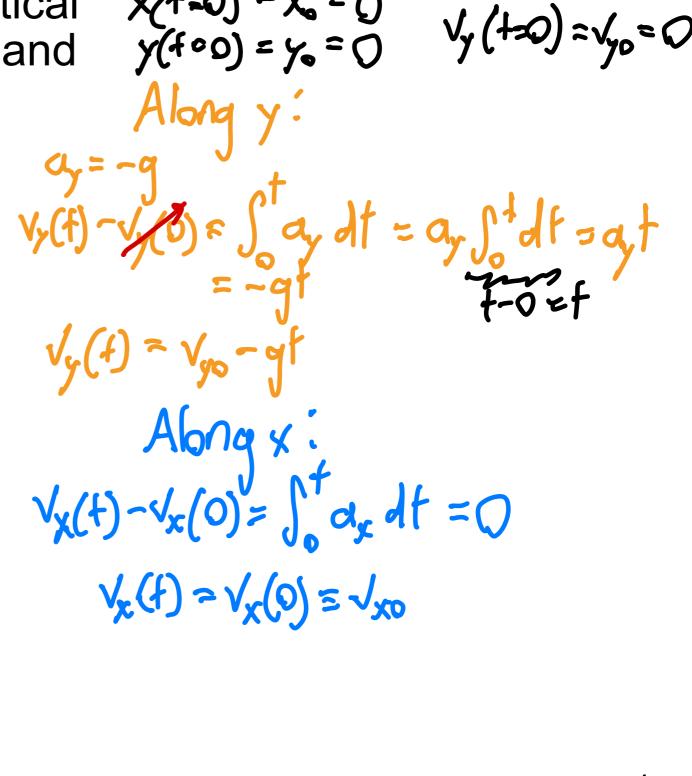
motion

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Motion in horizontal and vertical x(f=0) = X = Q
 components are decoupled and independent

Vertical

fall

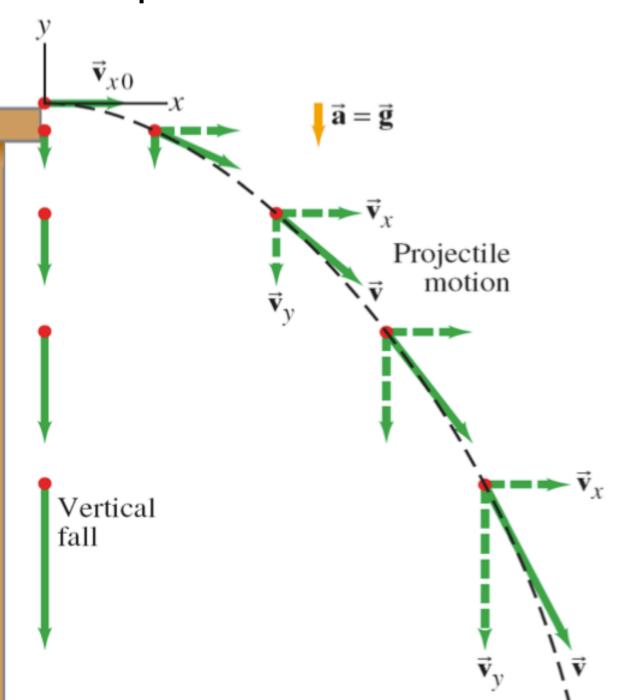




## Position throughout projectile motion

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 Motion in horizontal and vertical components are decoupled and independent

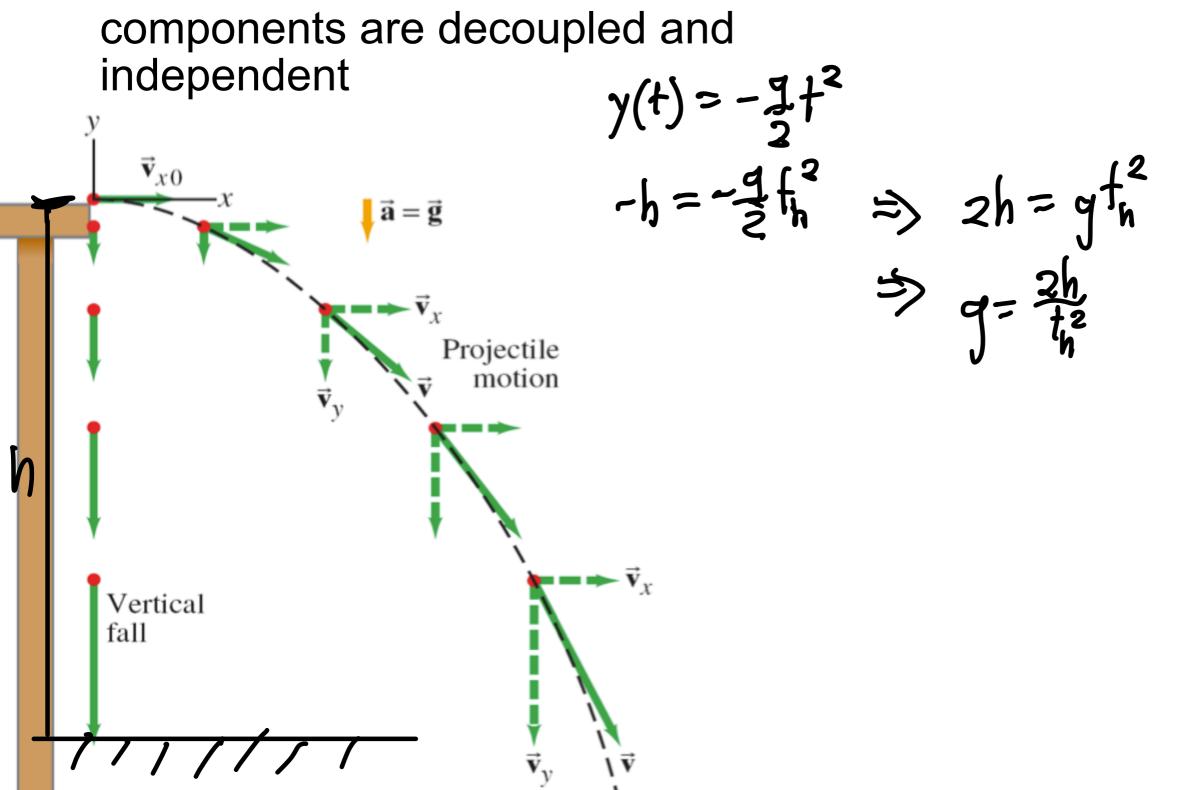


## Calculating "g"



Motion in horizontal and vertical components are decoupled and

independent



$$\Rightarrow 2h = 9^{t_n^2}$$

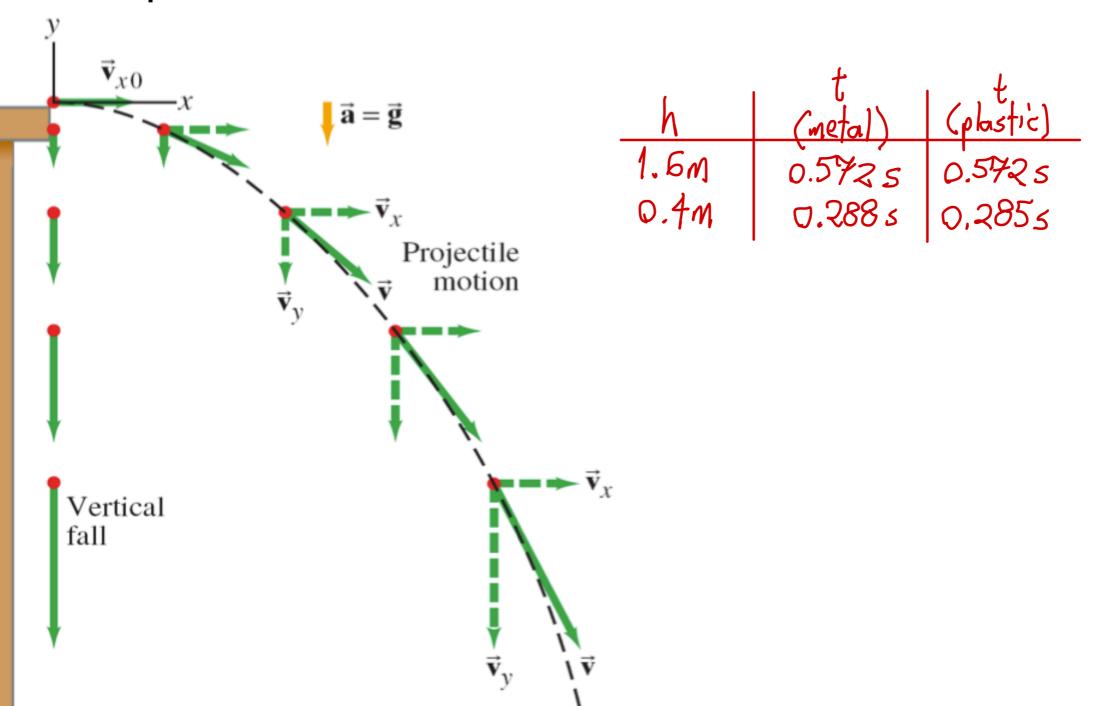
$$\Rightarrow 9 = \frac{2h}{t_n^2}$$

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## Calculating "g"

 Motion in horizontal and vertical components are decoupled and independent

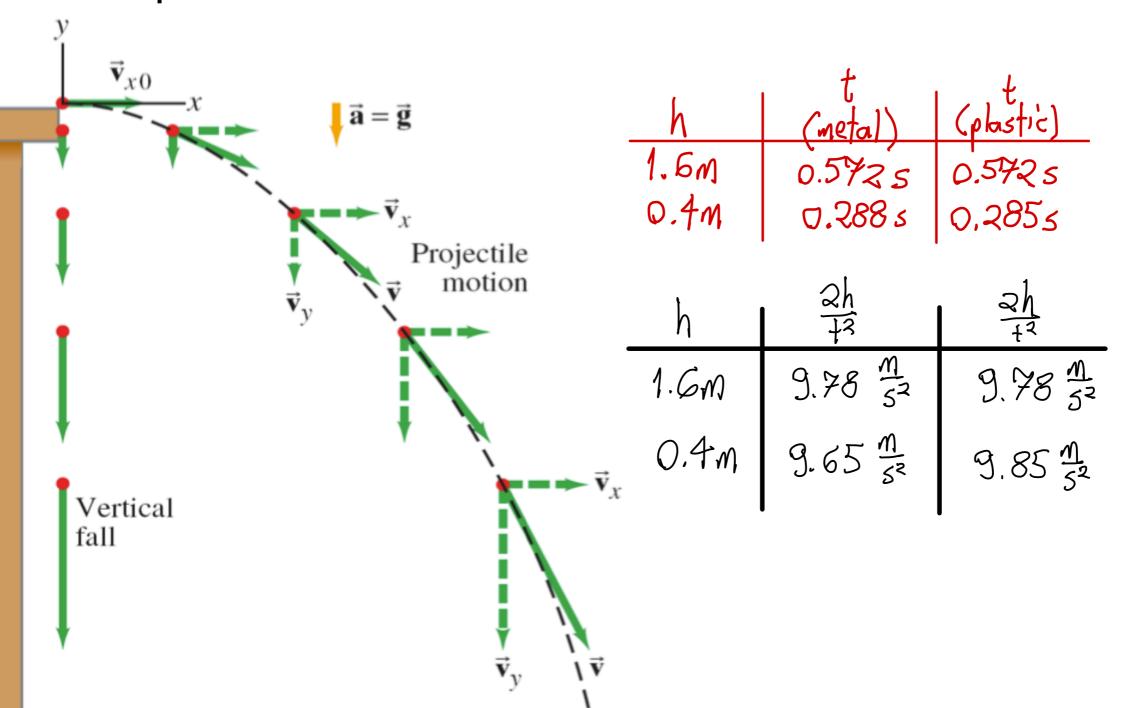




Center

## Calculating "g"

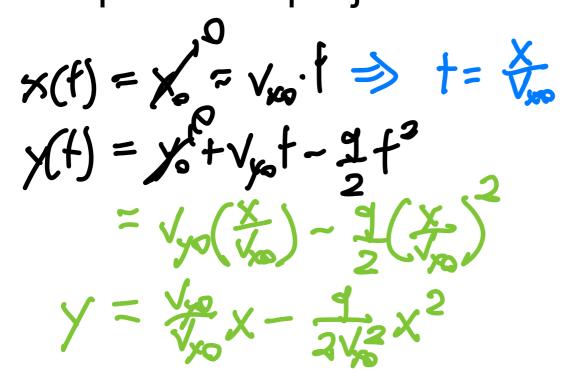
 Motion in horizontal and vertical components are decoupled and independent

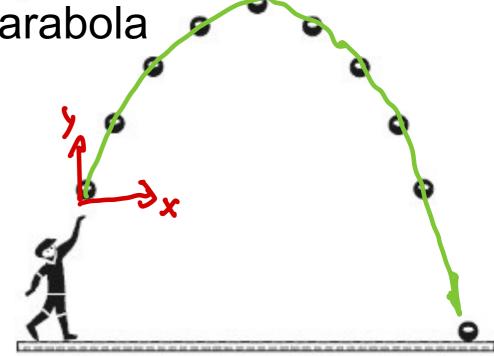


## Trajectory of projectile motion



The path of a projectile is always a parabola





## $\mathsf{DEMO}\left(\infty\right)$



## $\mathsf{DEMO}(\infty)$



An object at rest, stays at rest...

## **DEMO** (766)



An object in motion at a constant velocity stays in motion at a constant velocity...

#### Newton's 1st law of motion



In an inertial reference frame, an object will remain at rest, or in motion at a constant speed in a straight line, unless acted upon by a net <u>force</u>.

#### Newton's 1st law of motion



In an inertial reference frame, an object will remain at rest, or in motion at a constant speed in a straight line, unless acted upon by a net <u>force</u>.

Expresses the idea of "inertia"

## The concept of force



- A force is an influence that can change the motion of an object
- Whenever an object is accelerating in an inertial reference frame, there must be a force behind it
- It is a vector quantity, often denoted by  $\overrightarrow{F}$
- Measured in units of *Newtons* ([N] =  $\left| \frac{m}{s^2} \right|$ )

#### Newton's 1st law of motion



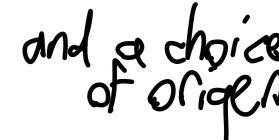
In an <u>inertial reference frame</u>, an object will remain at rest, or in motion at a constant speed in a straight line, unless acted upon by a net force.

- Expresses the idea of "inertia"
- In mathematics:

$$\Sigma \overrightarrow{F} = 0 \iff \overrightarrow{v} = \text{constant}$$



• A frame of reference is a coordinate system and a choice of original

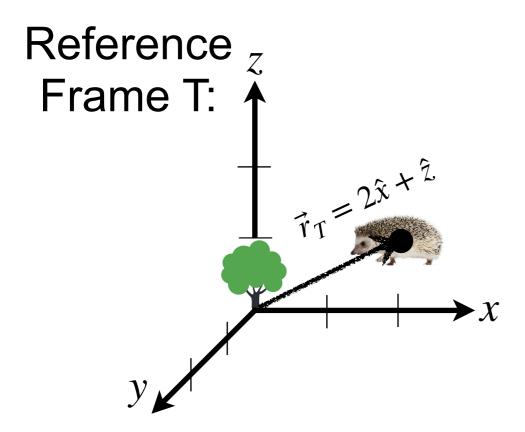


• Consider a hedgehog, he's still a point mass



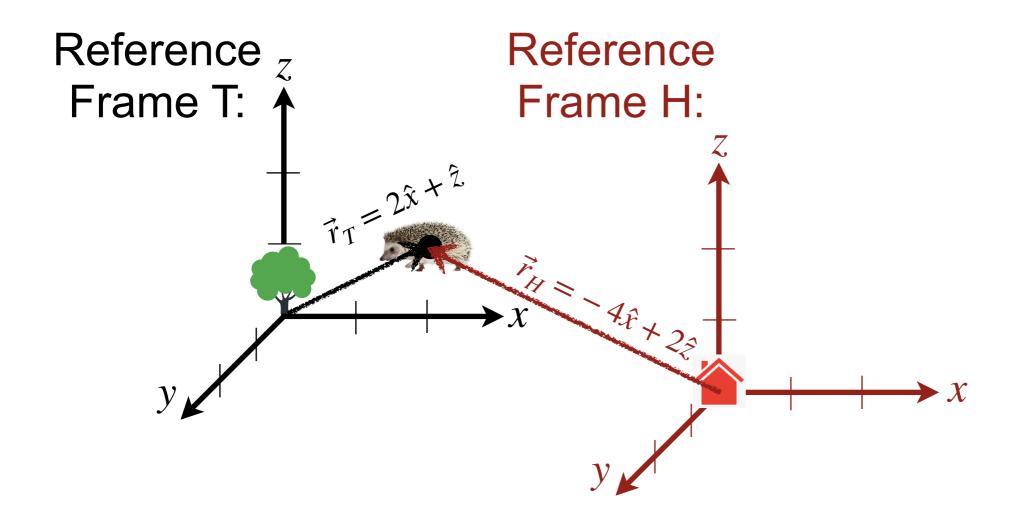


- A frame of reference is a coordinate system
- Consider a hedgehog, he's still a point mass
- You can quantify his position relative to another object, like a tree



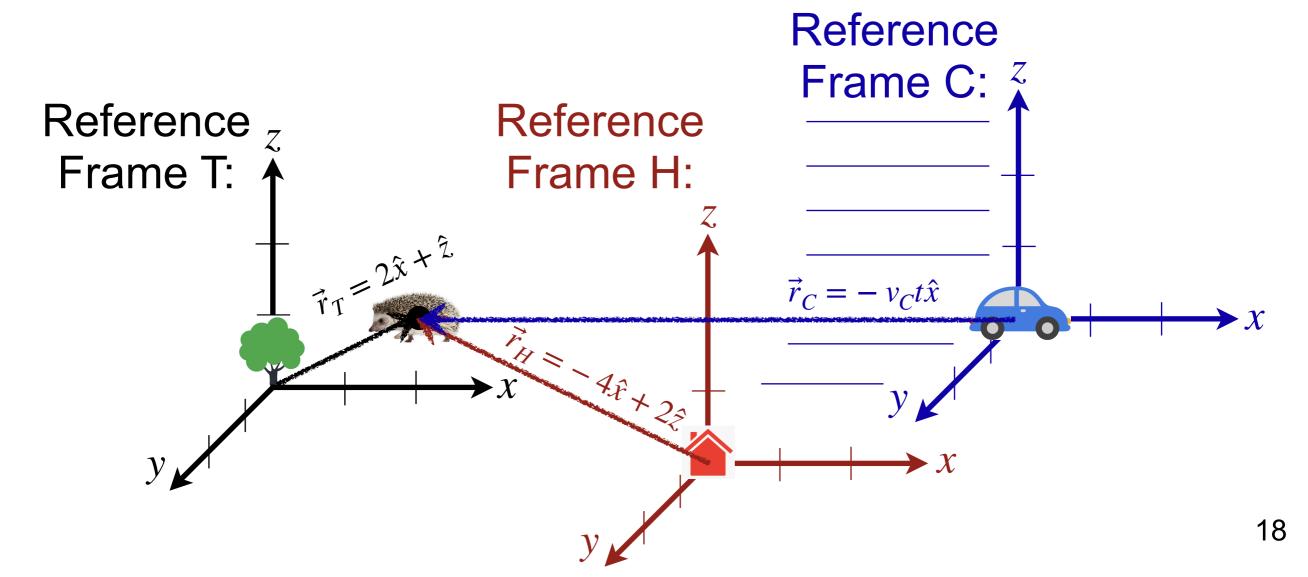


- A frame of reference is a coordinate system
- Consider a hedgehog, he's still a point mass
- You can quantify his position relative to another object, like a tree or a house



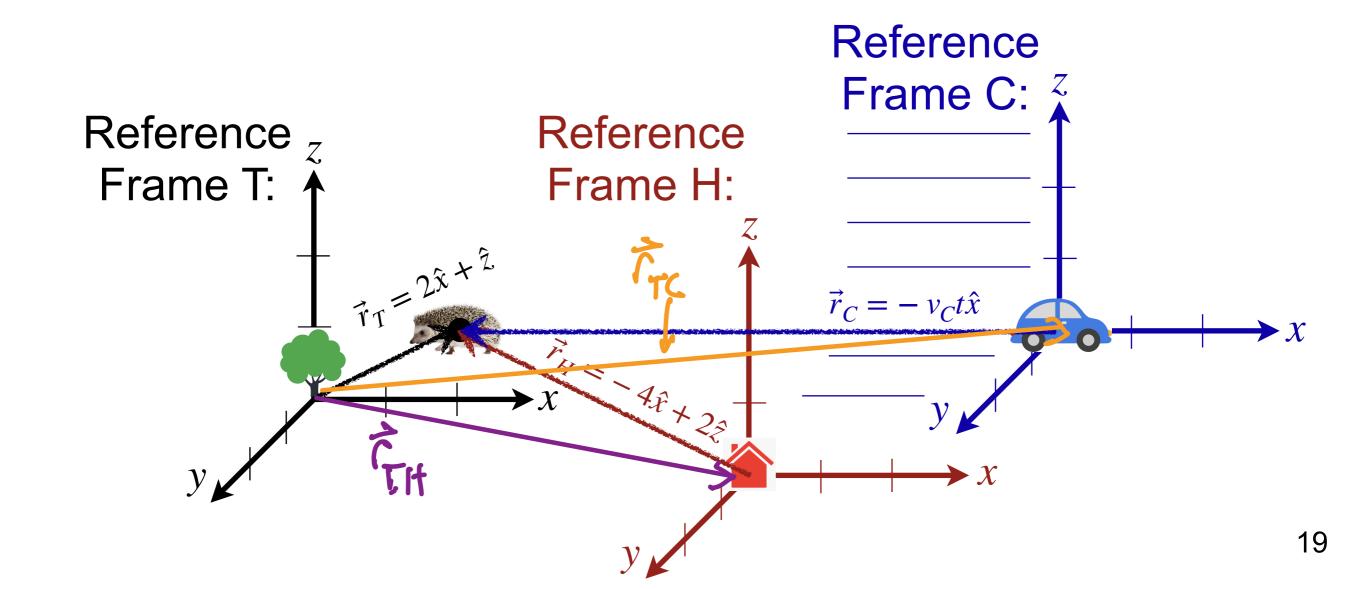


- A frame of reference is a coordinate system
- Consider a hedgehog, he's still a point mass
- You can quantify his position relative to another object, like a tree or a house or even a moving car





You can convert between frames of reference by



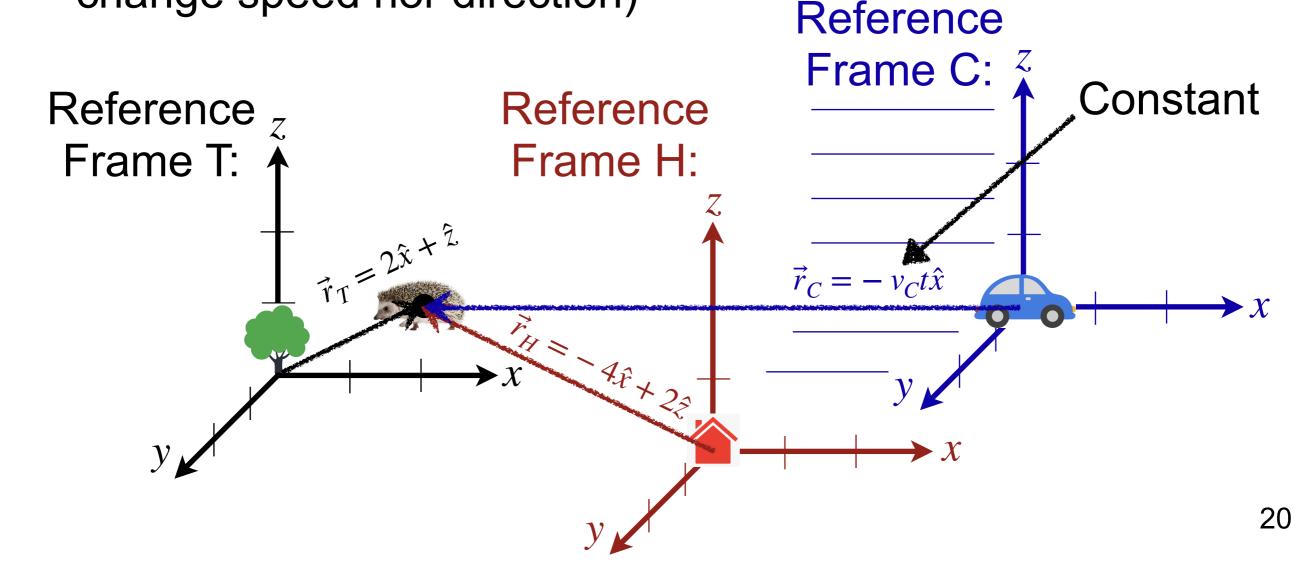


You can convert between frames of reference by comparing origins

$$\vec{r}_T = \vec{r}_{TH} + \vec{r}_H$$
 or  $\vec{r}_T = \vec{r}_{TC}(t) + \vec{r}_C$ 

Inertial reference frames do NOT accelerate (i.e. don't

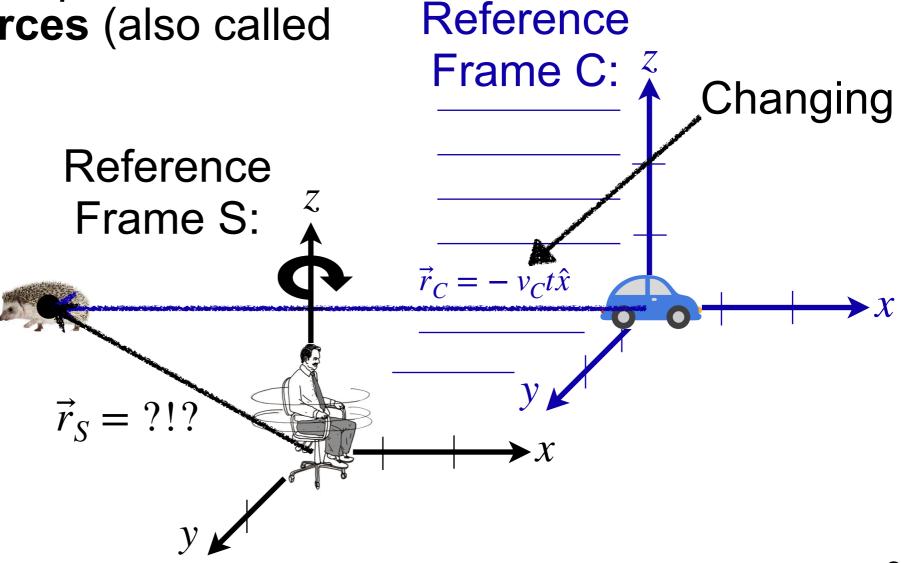
change speed nor direction)



#### Non-inertial frames of reference



- Non-inertial reference frames can accelerate (i.e. change speed or direction)
- Such coordinate systems can sometimes be helpful, but lead to fictitious forces (also called inertial forces)



#### Newton's 1st law of motion



In an inertial reference frame, an object will remain at rest, or in motion at a constant speed in a straight line, unless acted upon by a net force.

- Expresses the idea of "inertia"
- In mathematics:

$$\Sigma \overrightarrow{F} = 0 \iff \overrightarrow{v} = \text{constant}$$

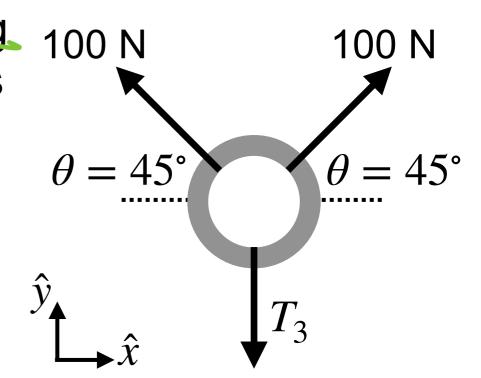
## Conceptual question

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Three people are pulling on a ring in a two-dimensional tug of war. Shown is a "top view". No one is winning, so the ring is sitting still. The pulls are configured as shown. Teams 1 and 2 are each pulling with a force of 100 N, while team 3 pulls with unknown force  $T_3$ .

Which expression gives the sum of the forces in the  $\hat{y}$  direction?

- A. 100 N
- B. 200 N
- C. 200 N \* cos(45) (=141 N)
- None of these





In an inertial reference frame, an object accelerates when it is acted upon by a net force.

The acceleration is directly proportional to the net force, and inversely proportional to the mass.



$$\Sigma \overrightarrow{F} = m\overrightarrow{a}$$



$$\Sigma \vec{F} = m\vec{a}$$
acceleration:
$$\vec{a} = \frac{d\vec{v}}{dt} = \frac{d^2\vec{x}}{dt^2}$$



$$\Sigma \overrightarrow{F} = m\overrightarrow{a}$$
mass

## The concept of mass



- Mass is an intrinsic property of an object
- It quantifies the inertia of an object, i.e. its resistance to changing its motion
- It is sometimes understood as the "amount" of matter in an object
- Mass is measured in kilograms [kg]
- It is <u>not</u> weight mass is a property of an object, while weight is the force exerted on an object by gravity
  - If you go to the moon (which has 6 times weaker gravity than Earth), your weight will decrease by a factor of 6 while your mass will stay the same



$$\Sigma \overrightarrow{F} = m\overrightarrow{a}$$
force





	Force	Magnitude	Direction
	ravitational n general)	$ \overrightarrow{F}  = G \frac{m_1 m_2}{r^2}$	In a straight line between the centers of the two masses, pulling them together
(a	ravitational at Earth's surface)	$ \overrightarrow{F}  = mg$ where $g = \frac{Gm_E}{r_E^2}$	- 9.81 Downwards
	ectrostatic Coulomb's Law)	$ \overrightarrow{F}  = k_e \frac{ q_1  q_2 }{r^2}$	In a straight line between the centers of the two charges
(Ho	Elastic ooke's Law)	$ \overrightarrow{F}  = k\Delta x$	Restores to equilibrium position
	Normal	$ \overrightarrow{F}  = N$	Perpendicular to the surface
Sta	atic Friction	$ \overrightarrow{F}  < \mu_s N$	Opposing the direction of impending motion
Kin	etic Friction	$ \overrightarrow{F}  = \mu_k N$	Opposing the direction of motion
Vis	scous Drag	$ \overrightarrow{F}  = bv^n$	Opposing the direction of motion
	Tension	$ \overrightarrow{F}  = T$	Against the direction of opposing forces

#### The four fundamental forces



- Modern physics now recognizes four fundamental forces
  - 1. Gravity
  - 2. Electromagnetism
  - 3. Strong nuclear (confines quarks in protons, neutrons and other subatomic particles)
  - 4. Weak nuclear ("responsible for some forms of nuclear decay")

#### The four fundamental forces



- Modern physics now recognizes four fundamental forces
  - 1. Gravity
  - 2. Electromagnetism
  - 3. Strong nuclear (confines quarks in protons, neutrons and other subatomic particles)
  - 4. Weak nuclear ("responsible for some forms of nuclear decay")
- What about friction, the normal force, tension, etc?
  - Except for gravity, all other "everyday" forces are due to electromagnetism acting at the atomic scale



$$\sum \overrightarrow{F} = m\overrightarrow{a}$$
NET force

## Free body diagrams



- Graphically represent ALL of the external forces acting on an object
- Remember that force is a vector
- Label each force and make the magnitudes and directions reasonably accurate
- Draw a separate diagram for each object

#### Free body diagrams

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- Graphically represent ALL of the external forces acting on an object
- Remember that force is a vector
- Label each force and make the magnitudes and directions reasonably accurate
- Draw a separate diagram for each object

An object in free fall (without drag)





#### More free body diagrams



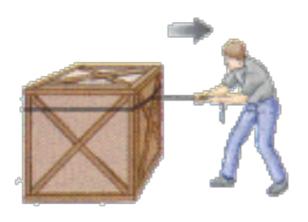
A lamp suspended from the ceiling by a chain

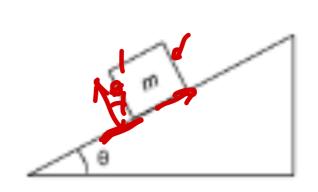
A box pulled along a rough surface

A block on an inclined plane

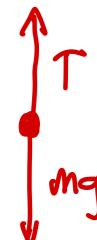
A foot in contact with the ground when walking

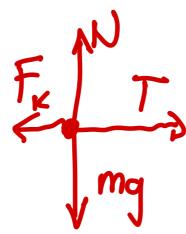




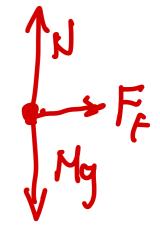














#### Conceptual question

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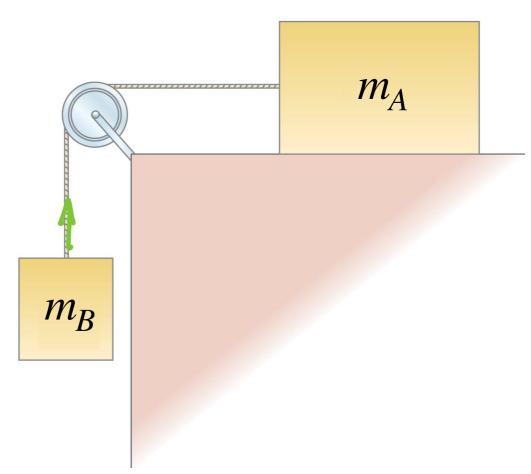
How does the force exerted on block A by the string (T)compare with the weight of block B?

Assume all surfaces are *frictionless*, the pulley is massless, and rope is *massless* and *inextensible*.

A. 
$$T = m_B g$$

$$B. T < m_B g$$

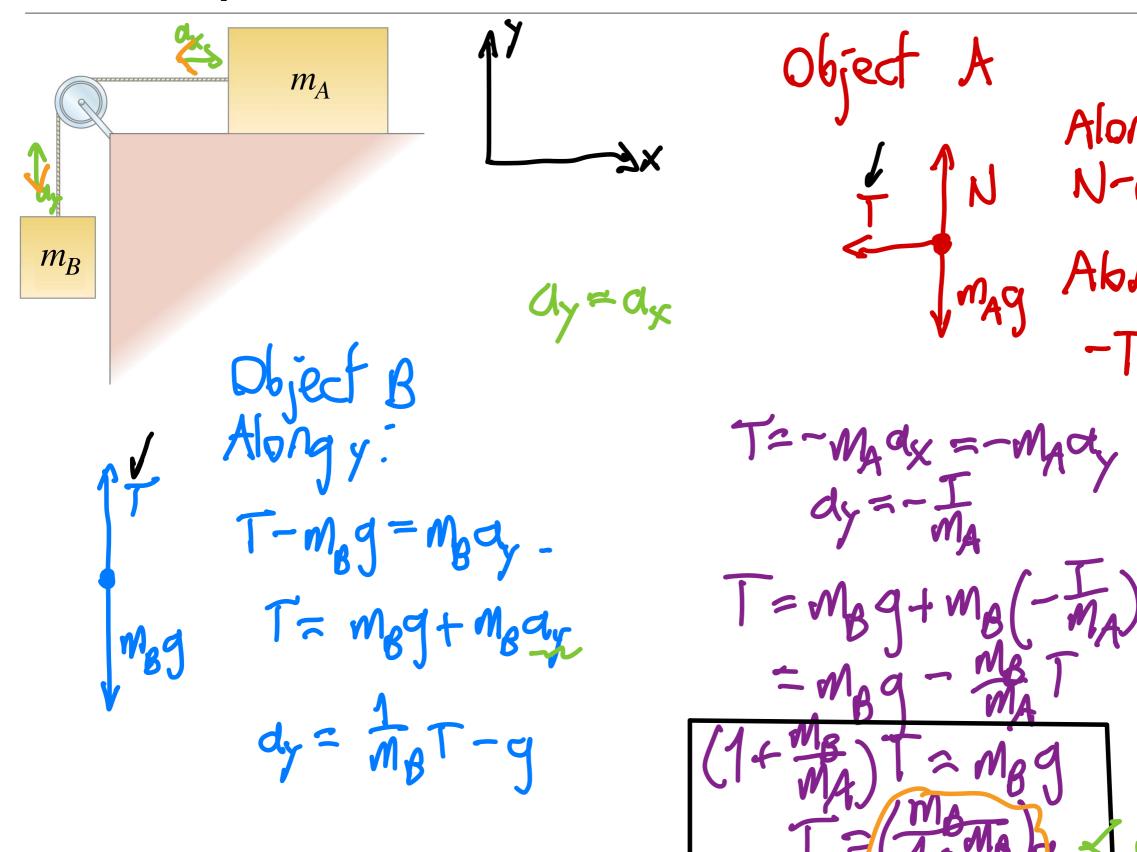
C. 
$$T > m_B g$$





#### Conceptual solution

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#### Friction

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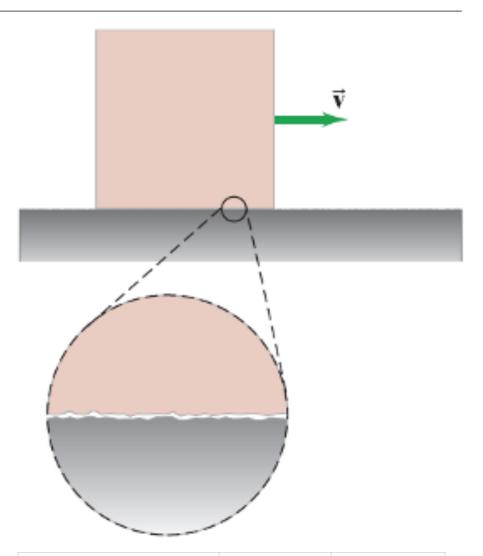
- Friction is always present when two solid surfaces are in contact
- Friction while sliding is called kinetic friction and approximately follows

$$|F| = \mu_k N$$

 Static friction is when the two surfaces are at rest relative to each other, which balances an applied force up to the maximum value of

$$|F| \leq \mu_{s}N$$

- It is easier to keep an object sliding than it is to get it started
- Surface area doesn't enter



Surfaces	$\mu_{_S}$	$\mu_k$
Rubber tires on pavement	0.9	0.8
Metal on ice	0.022	0.02
Steel on steel	0.6	0.4
Steel on steel (with grease)	0.1	0.05

#### Direction of frictional forces

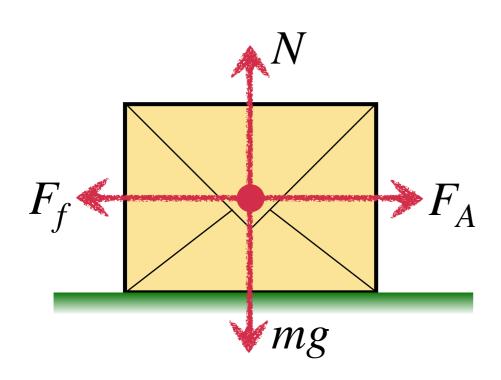


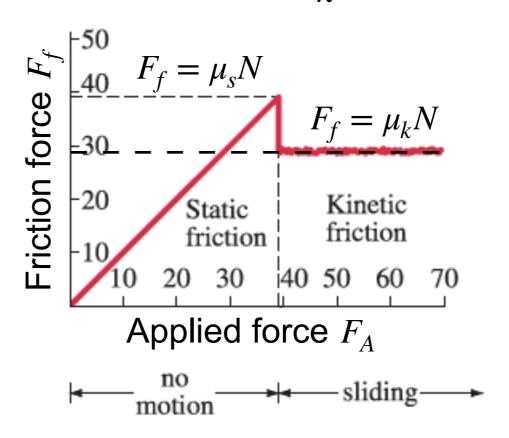
- ◆ If an object is sliding on a surface, kinetic friction applies:
  - The friction force experienced by the object is in the direction opposite to its velocity (relative to the surface)
  - The friction force experienced by the surface is equal and opposite
- ◆ If an object is at rest on a surface, static friction applies:
  - The static friction force experienced by the object is in the direction opposite to what its velocity (relative to the surface) would be if there was no friction
  - The friction force experienced by the surface is equal and opposite





• The dependence of the friction force on the applied force for a 10 kg box on a horizontal floor with the coefficients of static friction  $\mu_s = 0.4$  and kinetic friction  $\mu_k = 0.3$ 





# **DEMO** (69)



**Friction** 

#### Springs

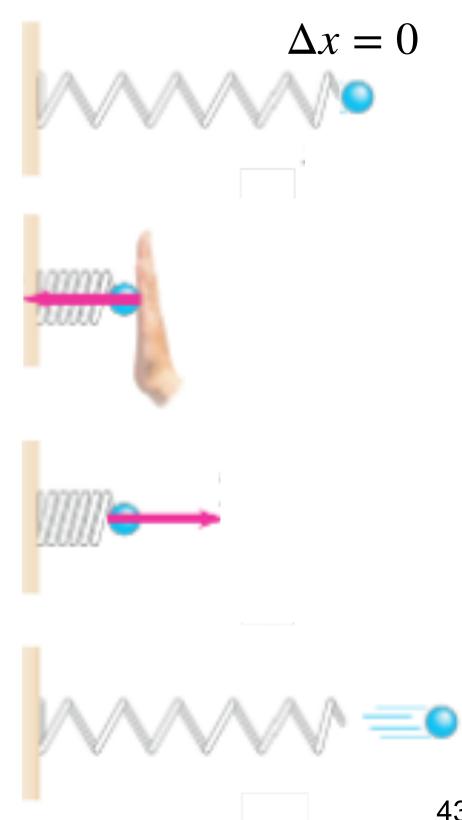


 The force required to compress or stretch a spring is

$$\overrightarrow{F} = -k\Delta \overrightarrow{x}$$

where k is the spring constant and  $\Delta \vec{x}$  is the displacement from the equilibrium position

- "Restoring" force is proportional to the displacement
- Springs might seem weird to focus on, but they are a good model for many applications
  - E.g. rubber bands, pendulums, electrical circuits, nuclear physics!



## **DEMO** (20)



Stretching a spring





If two objects interact, the force exerted by object 1 on object 2 is equal and opposite to the force exerted by object 2 on object 1.





If two objects interact, the force exerted by object 1 on object 2 is equal and opposite to the force exerted by object 2 on object 1.

- This known as the principle of action and reaction
- In mathematics:

$$\overrightarrow{F}_{12} = -\overrightarrow{F}_{21}$$

#### Newton's 3rd law of motion



If two objects interact, the force exerted by object 1 on object 2 is equal and opposite to the force exerted by object 2 on object 1.

- This known as the principle of action and reaction
- In mathematics:

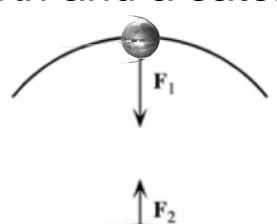
$$\overrightarrow{F}_{12} = -\overrightarrow{F}_{21}$$

Action-reaction pairs must act on different objects!

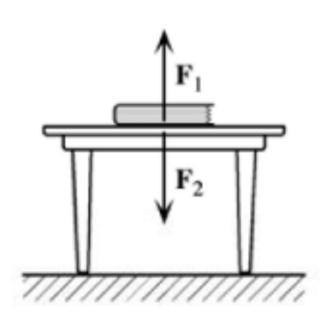
#### Examples of action-reaction pairs



Gravitational forces between Earth and a satellite



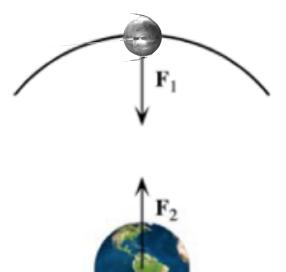
Normal forces between a book and a table



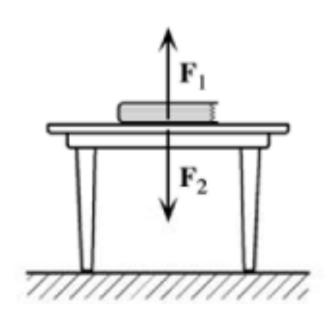
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#### Examples of action-reaction pairs

# Gravitational forces between Earth and a satellite



# Normal forces between a book and a table



- To test if two forces are action-reaction pairs, try stating the forces in your head, e.g.
- "The gravitational force of the Earth on the satellite and the gravitational force of the satellite on the Earth"
- "The normal force of the table on the book and the normal force of the book on the table"

### **DEMO** (765)



Action-reaction buggy

#### **EPFL**

#### Conceptual question

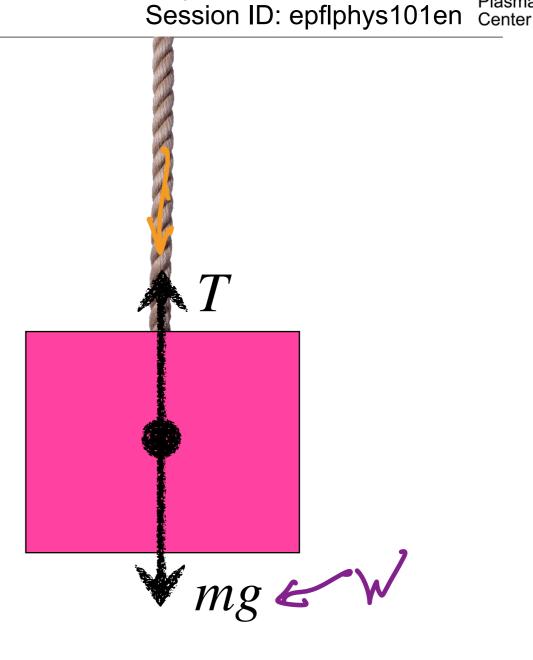
Here is a stationary pink box hanging from a rope.

Are the two forces shown (i.e. the tension force from the rope and the gravitational force on the box) action-reaction pairs?

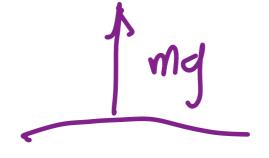
A. Yes

B. No

C. Maybe



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### Tomorrow we rock climb (theoretically)



