

PAUL SCHERRER INSTITUT



EPFL



Marianne Liebi– Material Science at Large Scale Facilities

Coherent Diffraction Imaging

EPFL Master Course 2024 MSE435

Course program

09.09.24	Introduction, sources, beamlines, detectors	Steven Van Petegem
16.09.24	Holiday	
23.09.24	Excursion to PSI	Steven Van Petegem / Marianne Liebi
30.09.24	Interaction with matter	Steven Van Petegem
07.10.24	Fluorescence	Marianne Liebi
14.10.24	Diffraction I	Steven Van Petegem
21.10.24	Break	
28.10.24	Small angle x-ray scattering	Marianne Liebi
04.11.24	Cancelled	
11.11.24	XANES/EXAFS	Marianne Liebi
18.11.24	Phase contrast / Tomography	Steven Van Petegem
25.11.24	Coherent imaging	Marianne Liebi
02.12.24	Diffraction II / Neutron imaging	Steven Van Petegem
09.12.24	PEEM / Magnetic scattering	Steven Van Petegem
16.12.24	Case study presentations	Steven Van Petegem / Marianne Liebi

- Question: Do you get the same information if you measure at a K-edge or an L-edge of a material?

The question is not simple but the fast answer is that the information one can get from K and L edges XANES is complimentary.

K- and L1 edges XANES mainly probe the p-density of unoccupied states because there s to d transition are formally forbidden. Nevertheless the K pre-edges correspond to s to d forbidden transitions providing information about 3d elements local symmetry, intense pre-edge correspond to non-centrosymmetric coordination (e.g. tetrahedral).

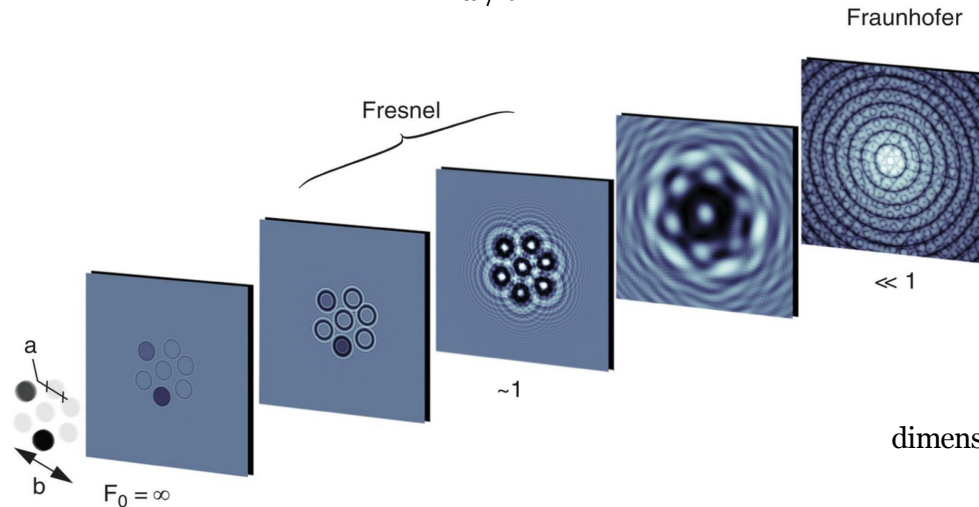
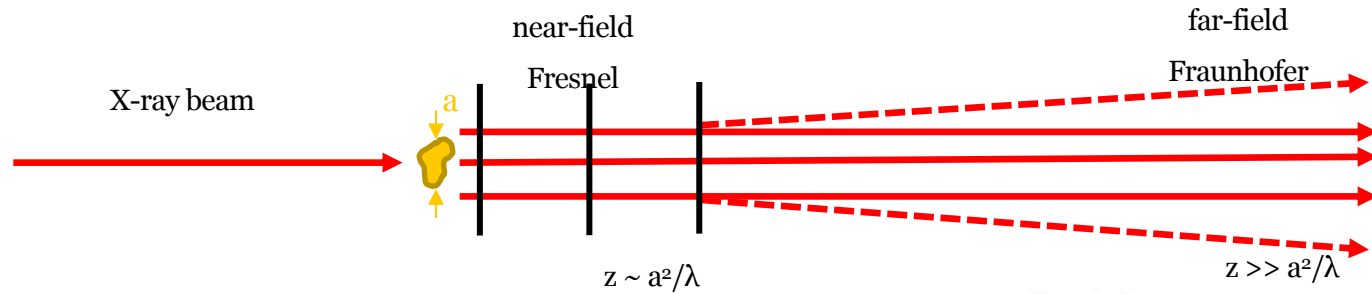
L2 and L3 are sensitive to d-projected density of unoccupied states.

K-edges of heavy elements are also often very broad due to high lifetime broadening, therefore they may not show many features except for the E-shift due to the oxidation state. L-edges are more narrow showing more fine structure, which helps to distinguish fine details of the local structure.

For EXAFS K-edges are preferable, as they are better separated in energy, less overlap with other elements, easier to measure up to high wavenumbers with good statistics.

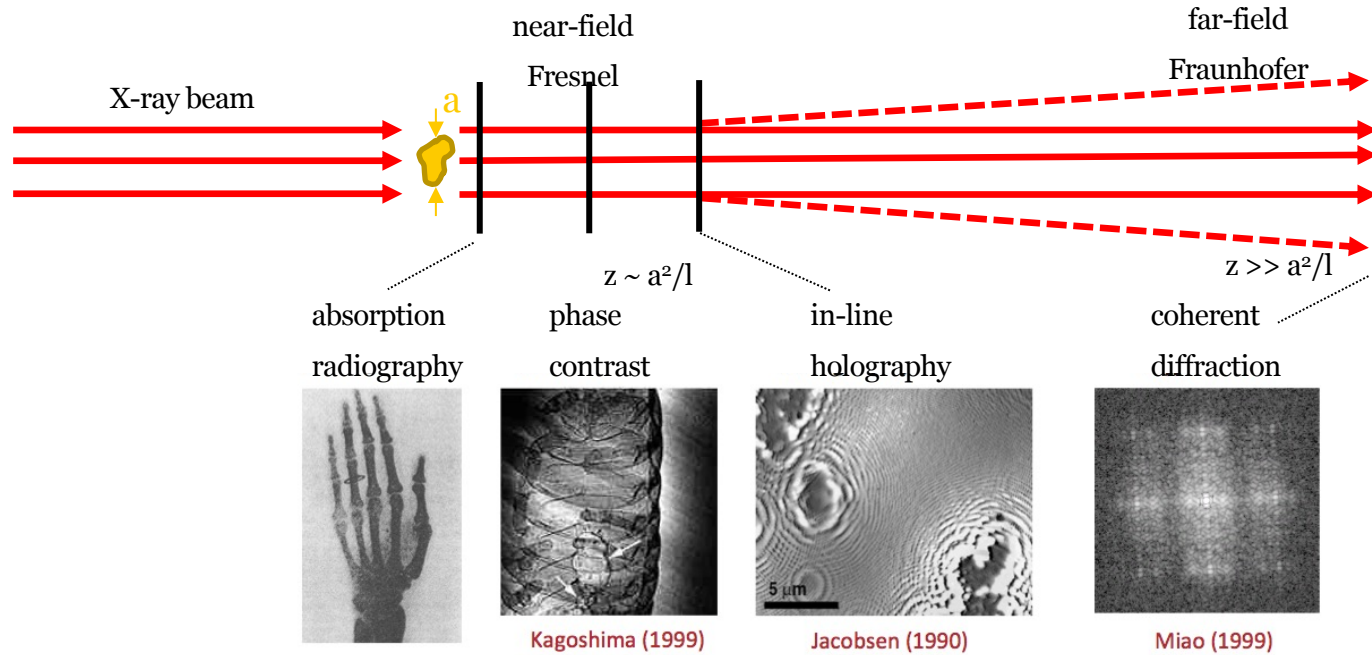
Olga Safonova (Beamline Scientist SuperXAS)

Far-field Fraunhofer Regim



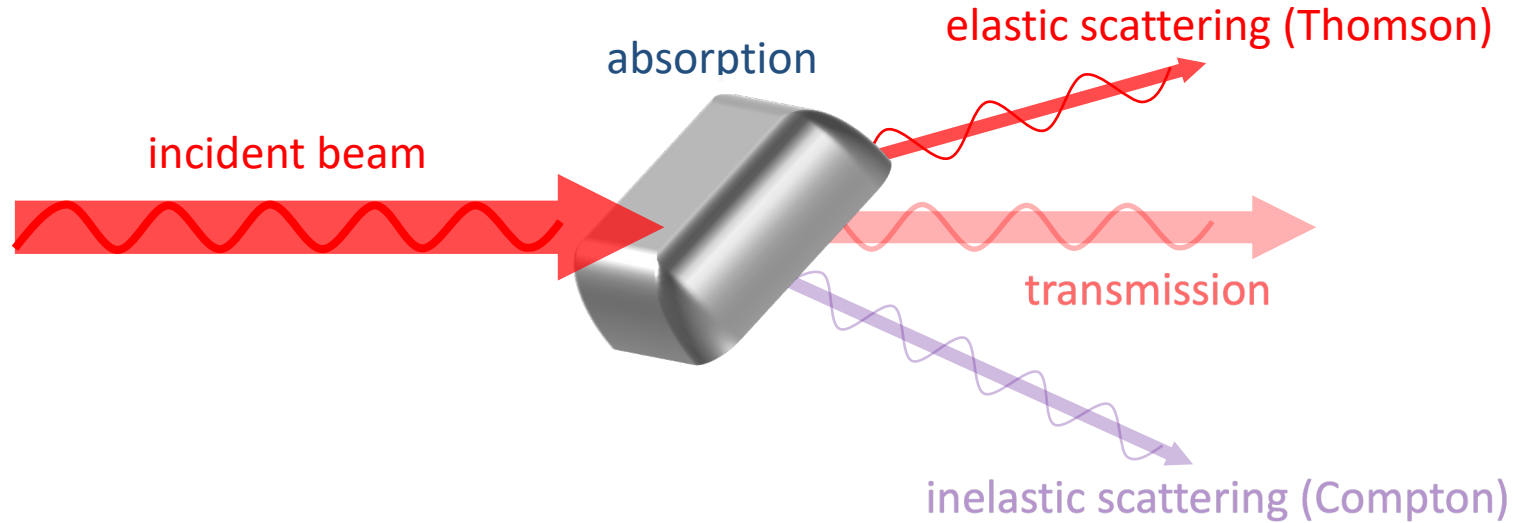
dimensionless Fresnel number $F_0 = a^2/z\lambda$

X-ray imaging: full-field

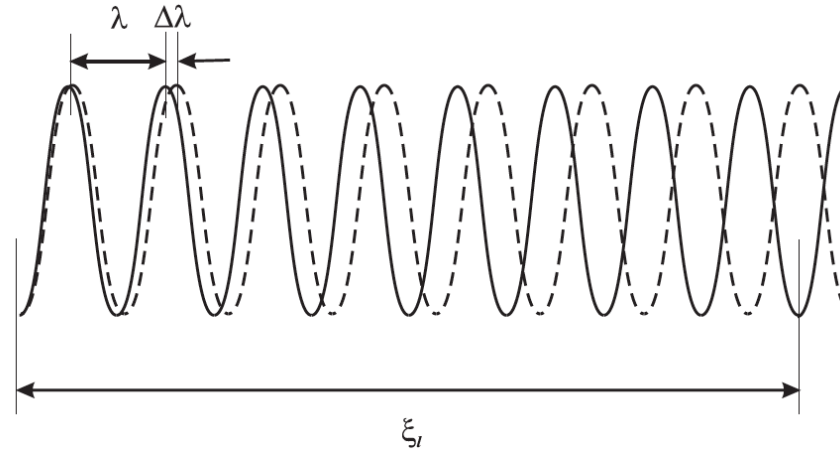


Interaction of X-rays with matter

interaction with electrons



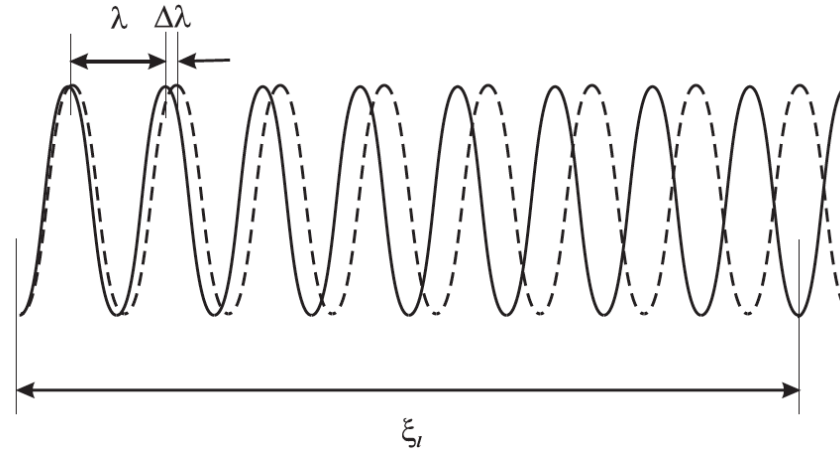
Longitudinal coherence



Longitudinal coherence length: $\xi_l \simeq \frac{1}{2} \frac{\lambda^2}{\Delta\lambda}$

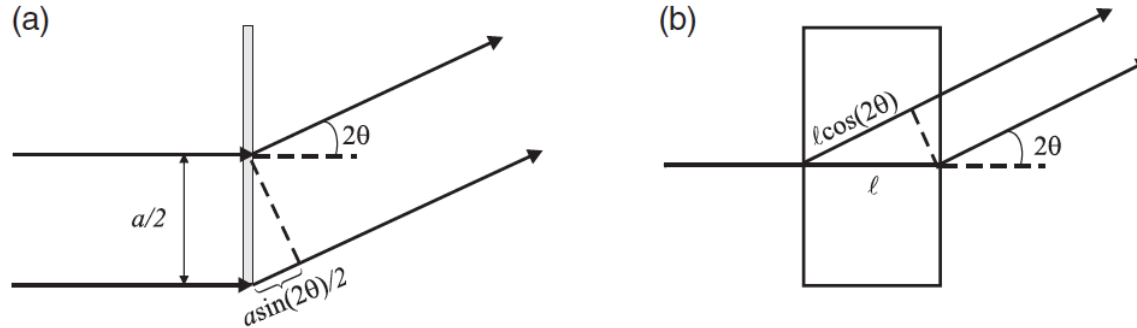
"Propagation of two waves with wavelengths λ and $\lambda + \Delta\lambda$. The longitudinal coherence length is defined as the distance over which the phase difference between the two waves is π ."

Longitudinal coherence



Longitudinal coherence length: $\xi_l \simeq \frac{1}{2} \frac{\lambda^2}{\Delta\lambda}$ Si (111) monochromator: $DI/l = 1.3 \times 10^{-4}$
 $l = 2 \text{ \AA} \rightarrow x_l \approx 800 \text{ nm}$

Implications of longitudinal coherence

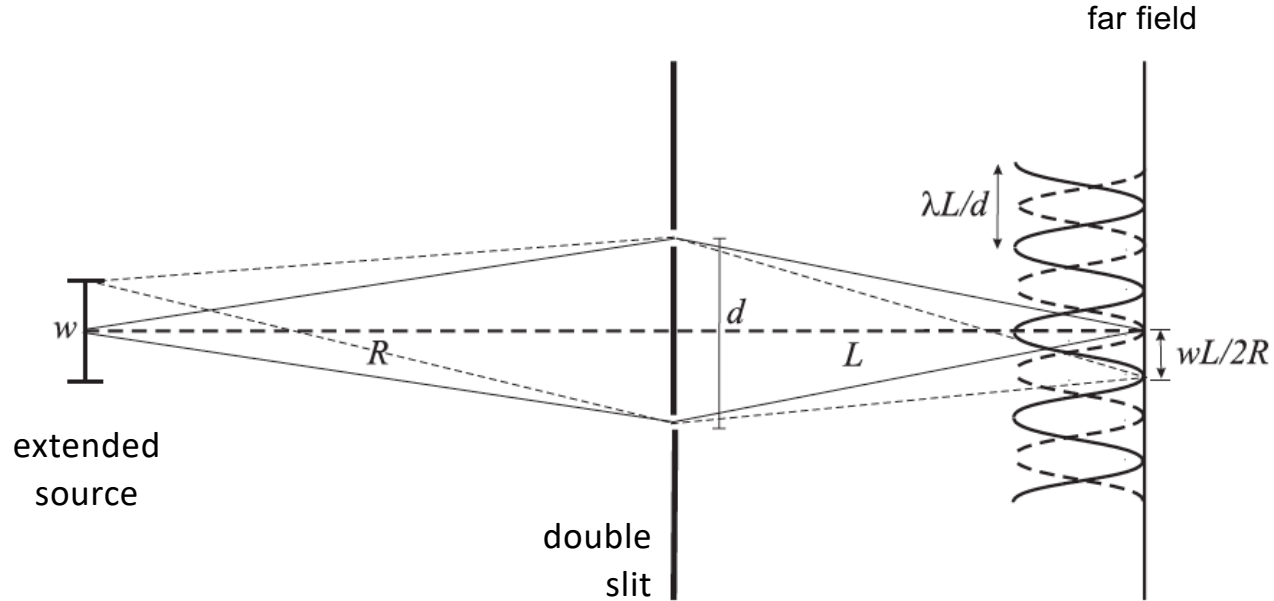


A condition for coherence is that the path length difference between points scattered from different points at the sample is smaller than the longitudinal coherence length x_l

$$\frac{\Delta\lambda}{\lambda} < \frac{s}{a}$$

In order to resolve an object of size $a = 5 \mu\text{m}$ to within $s = 10 \text{ nm}$, one has to keep the bandwidth below $2 \times 10^{-3} \rightarrow$ crystal monochromator

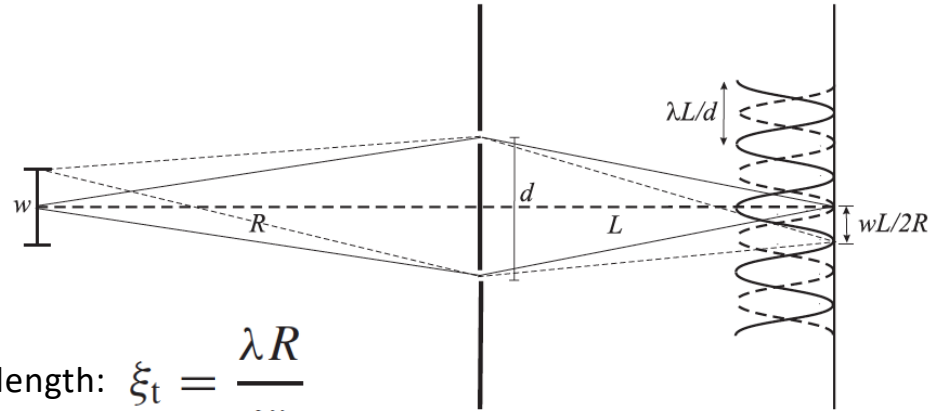
Transversal coherence



Transversal coherence length: $\xi_t = \frac{\lambda R}{w}$

Maximum distance between two slits such that they produce constructive interference when illuminated by an extended source size

Transversal coherence



Transversal coherence length: $\xi_t = \frac{\lambda R}{w}$

Numbers for a typical 3rd generation source

Laboratory: $x_h < 1 \mu\text{m}$

$$l = 2 \text{ \AA}$$

$$R = 34 \text{ m}$$

$$w_v = 20 \text{ mm} \rightarrow x_v = 340 \mu\text{m}$$

$$w_h = 200 \text{ mm} \rightarrow x_h = 34 \mu\text{m}$$

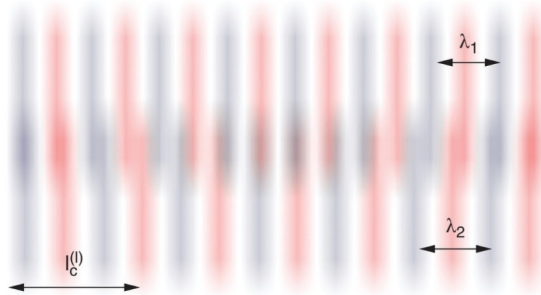
Max IV (4th generation synchrotron:

$$w_v = 6 \mu\text{m}, R = 60 \text{ m}, l = 1 \text{ \AA}$$

$$x_v \sim 1 \text{ mm}$$

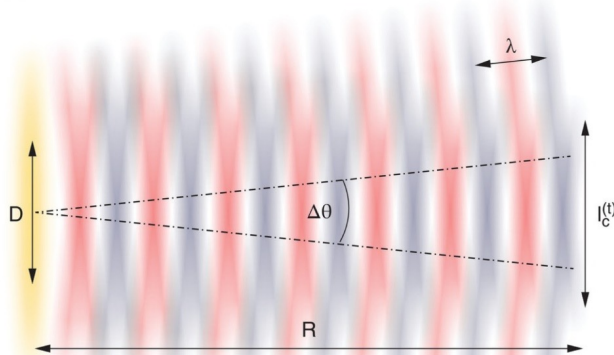
Coherence

(a)



longitudinal (temporal) coherence length
determined by monochromacy of the source

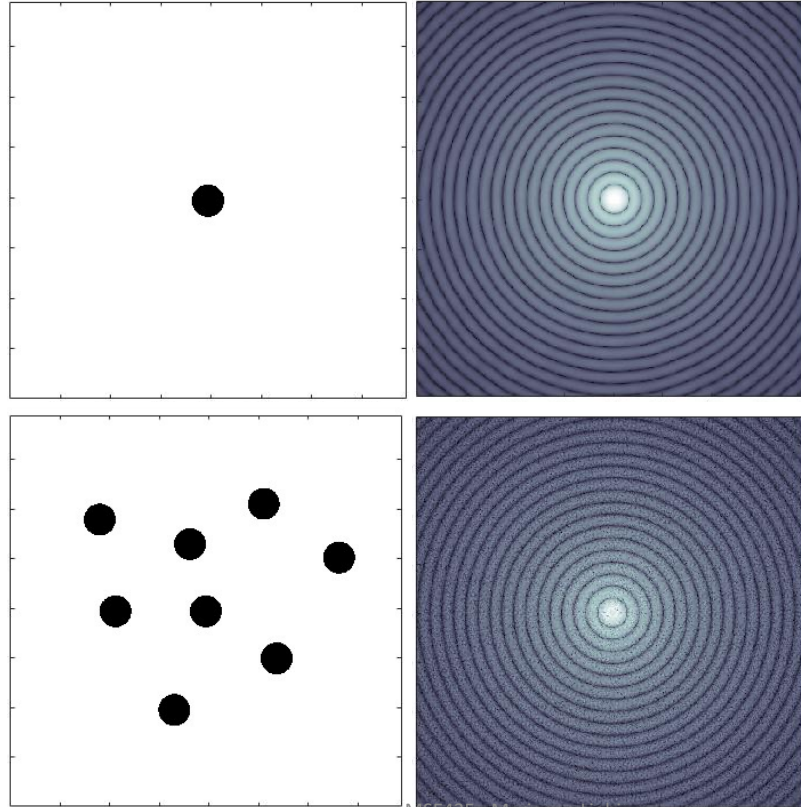
(b)



transverse (spatial) coherence length
depends on the beam divergence and source size

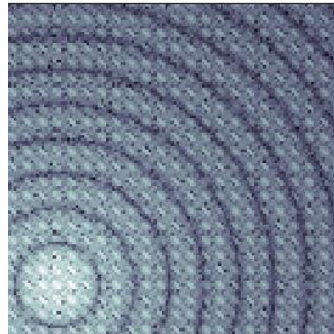
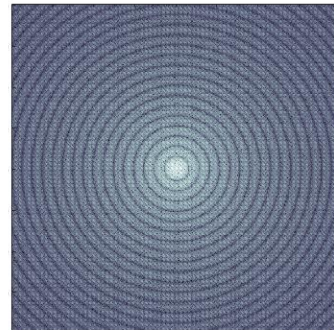
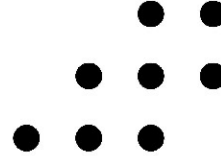
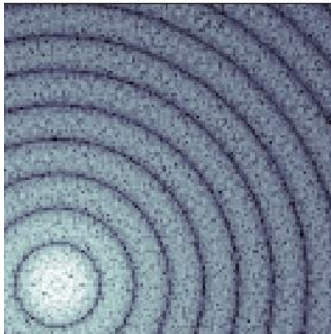
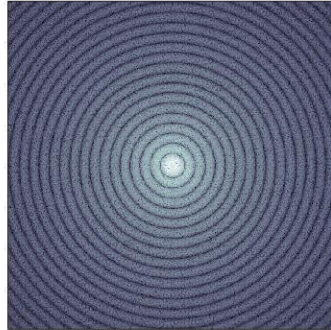
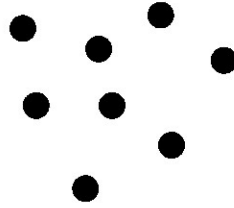
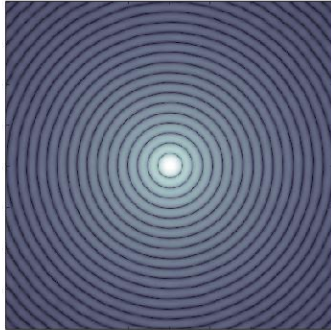
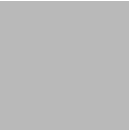
Willmott, P. (2019). Scattering Techniques. An Introduction to Synchrotron Radiation, John Wiley & Sons, Ltd: 133-221.

small-angle X-ray scattering



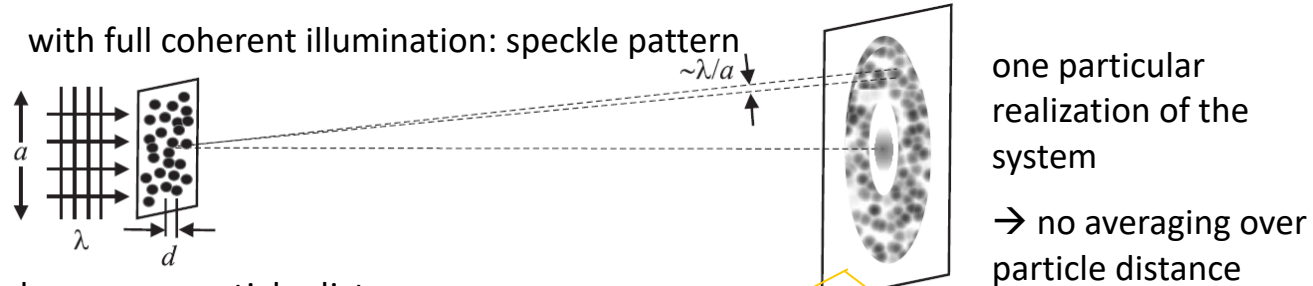
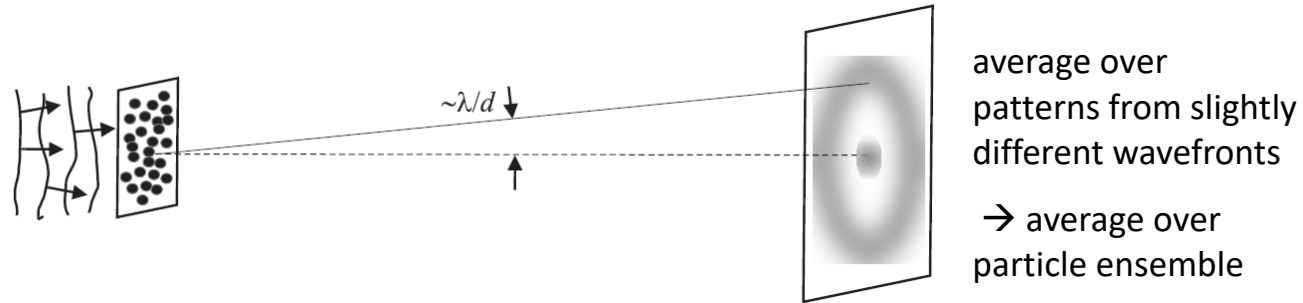
scattering pattern shows
average over particle ensemble

Scattering with coherent illumination



Coherent scattering

X-ray scattering from a disordered medium in the far field (Fraunhofer)



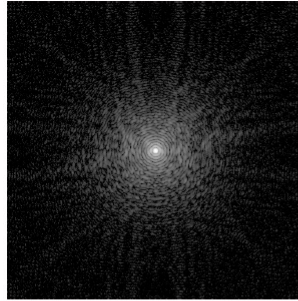
d: average particle distance

a: size of illuminated area

dynamics: XPCS/DLS

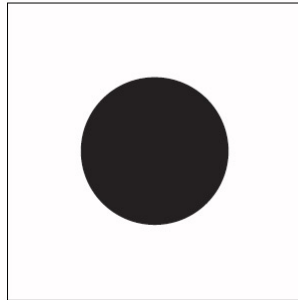
imaging

Coherent diffraction imaging (CDI)



**Fourier
constraint**

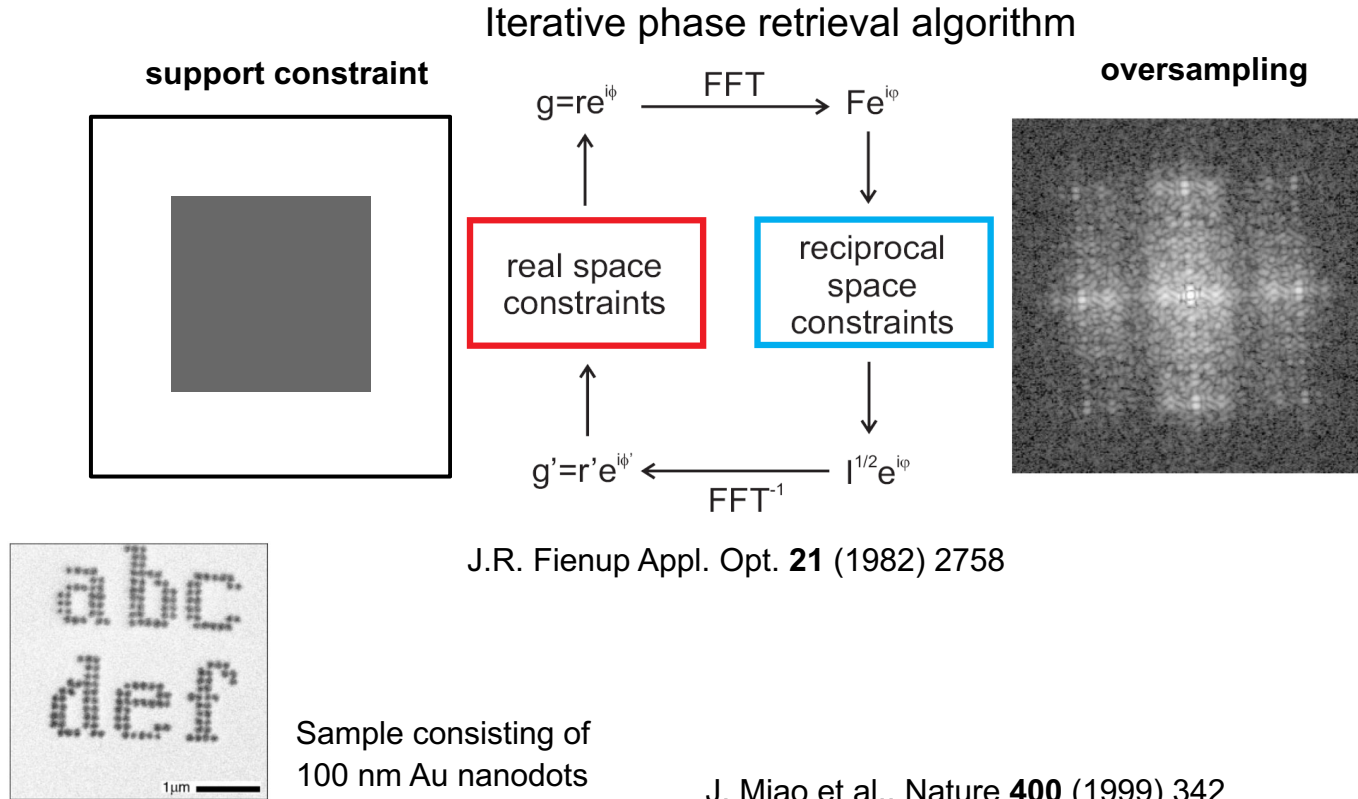
image is consistent with measured intensity



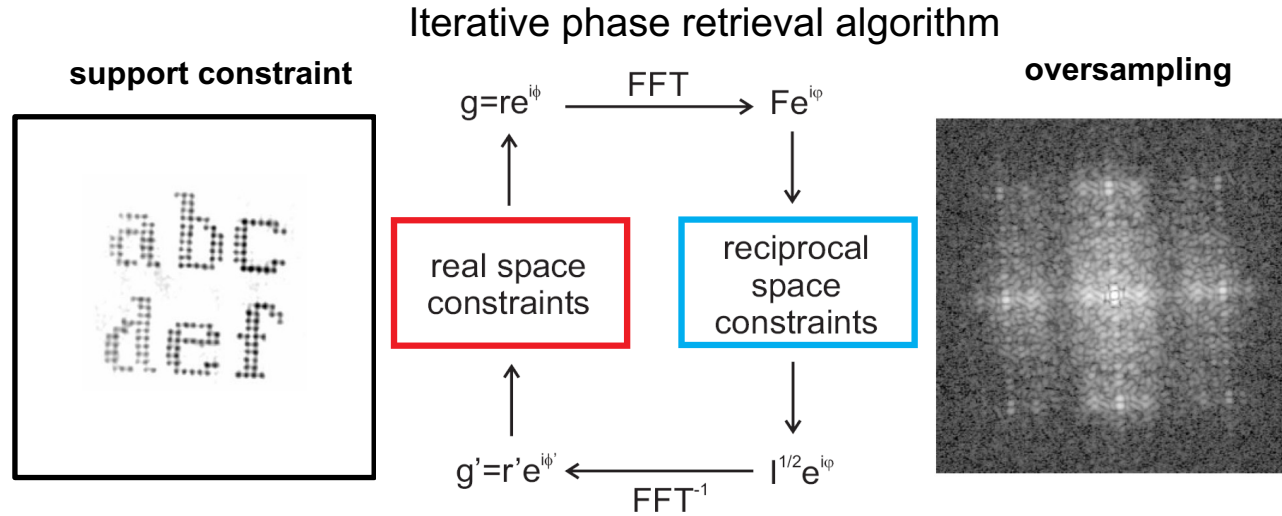
**support
constraint**

the object is inside a finite support

Coherent diffraction imaging (CDI)

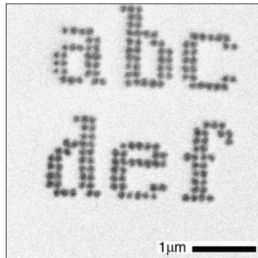


Coherent diffraction imaging (CDI)



J.R. Fienup Appl. Opt. **21** (1982) 2758

- Resolution not limited by optics



Sample consisting of
100 nm Au nanodots

J. Miao et al., Nature **400** (1999) 342

SAXS analysis: iterative approach

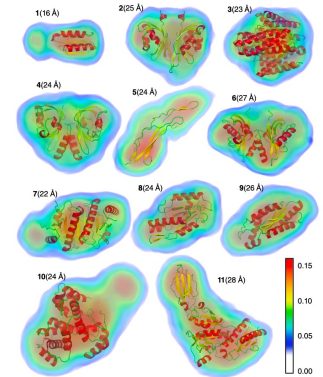
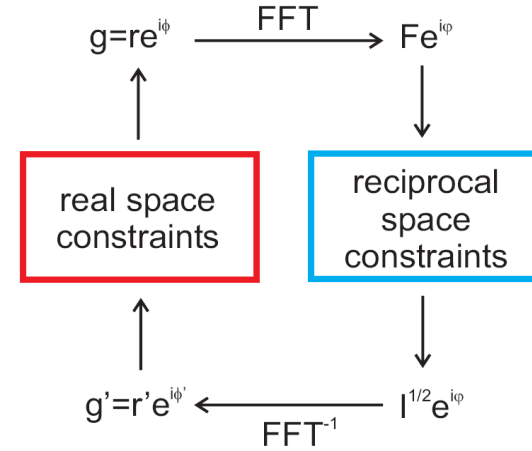
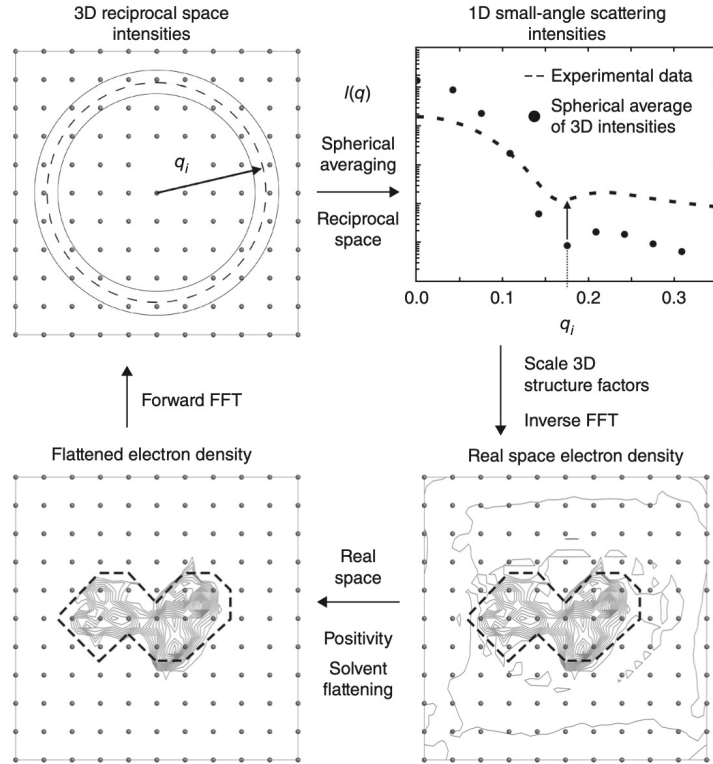


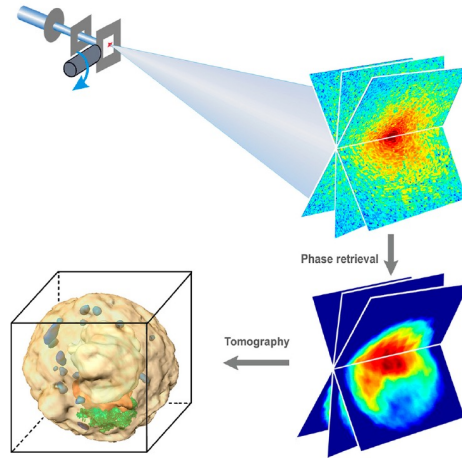
Figure 2 | Electron density reconstructions from experimental solution scattering data for samples 1-11 (Supplementary Table 1). Electron densities are shown as volumes colored according to density (color bar indicates electron density values in $e^-/\text{\AA}^3$). X-ray crystal structures (for PDB IDs, see Supplementary Table 1) are shown in cartoon format. Estimated resolutions of the solution scattering reconstructions are shown next to sample 10 (see Online Methods).

- SAXS only **average** nanostructure of sample illuminated,
- CDI image of the nanostructure illuminated

Grant, T. D., *Nature Methods* **2018**, 15, 191.

3D coherent diffraction imaging

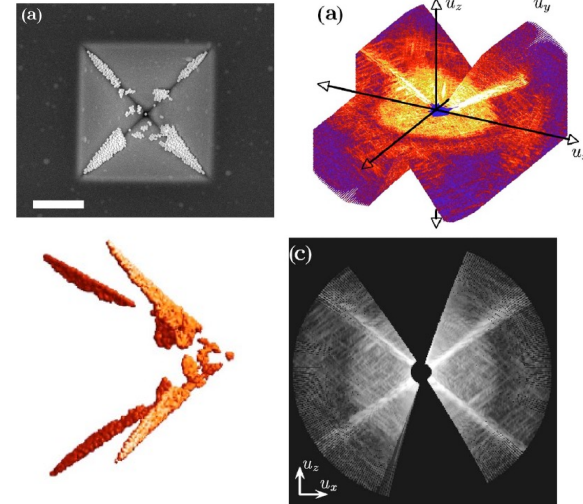
School of J. Miao



H. Jiang *et al.*,
PNAS **107** (2010) 11234

- 2D phase retrieval on each 2D coherent diffraction pattern recorded at different angles
- Conventional tomography

School of H. N. Chapman

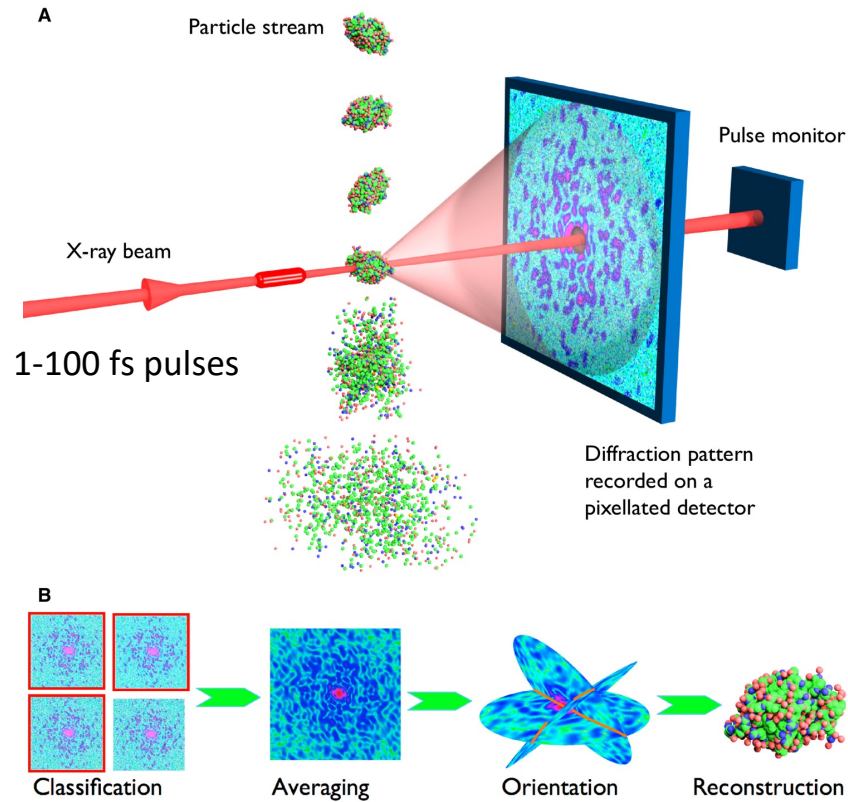


H. N. Chapman *et al.*,
J. Opt. Soc. Am. A **23** (2006) 1179

- 3D reciprocal space construction from 2D coherent diffraction patterns recorded at different angles
- 3D phase retrieval

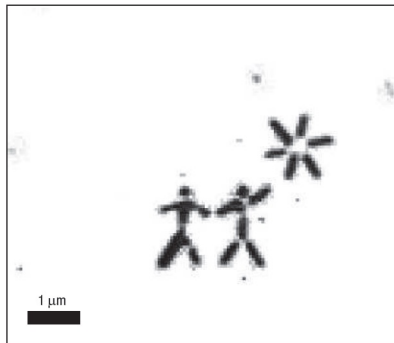
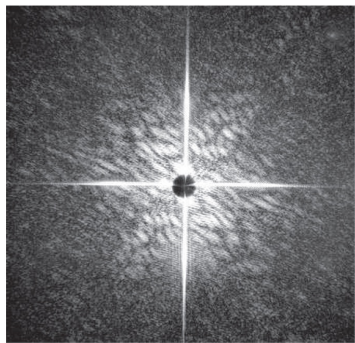
X-ray free electron lasers (X-FELs)

Diffract-before-destroy approach



https://cid.cfel.de/research/single_particle_imaging/
 Henry Chapman, CFEL. Science, 2007, 316, 1444-48.

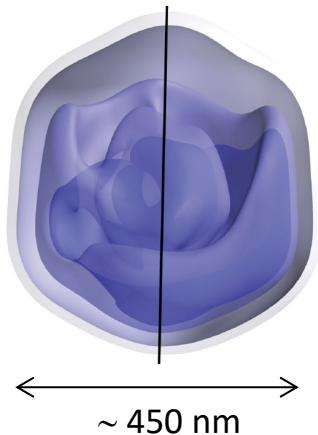
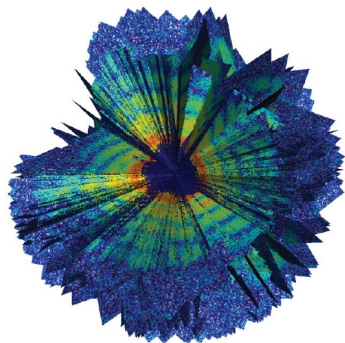
CDI in free electron lasers



Test sample

@ FLASH, $\lambda = 32 \text{ nm}$

H. N. Chapman *et al.*,
Nat. Phys. **2** (2006) 839

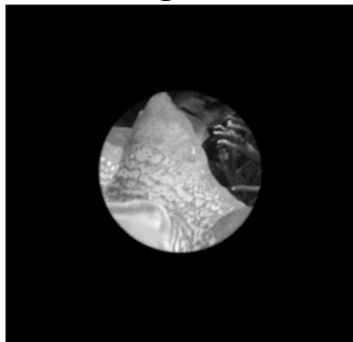


Giant mimivirus particle
@ LCLS, free electron laser

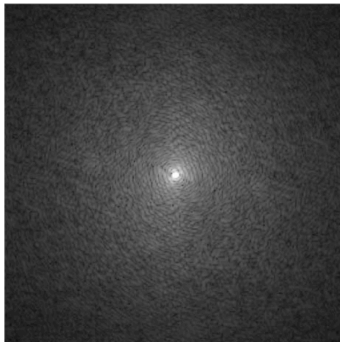
T. Ekeberg *et al.*, Phys. Rev. Lett.
114 (2015) 098102

CDI: Twin-image problem

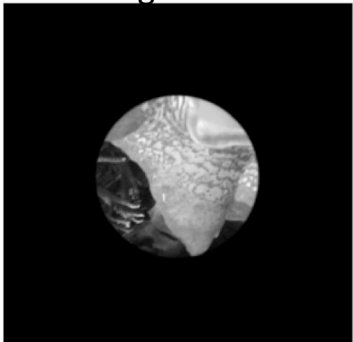
True image



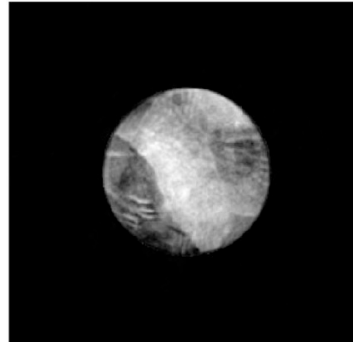
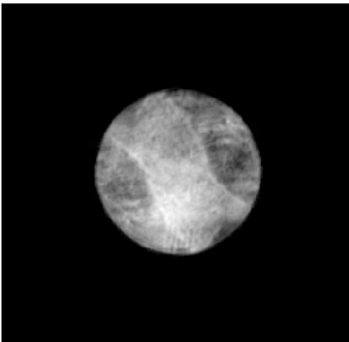
Fourier transform magnitude



Twin image



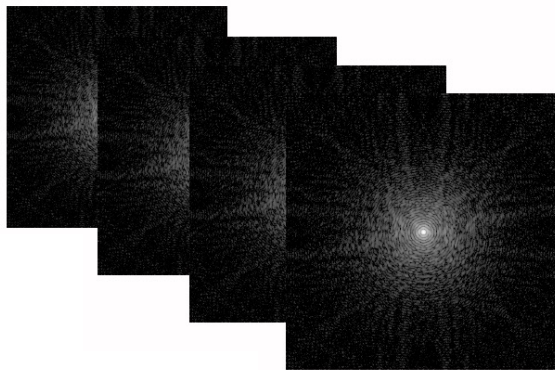
Twin image stagnation



M. Guizar-Sicairos and J. R. Fienup, J. Opt. Soc. Am A **29**, 2367 (2012)

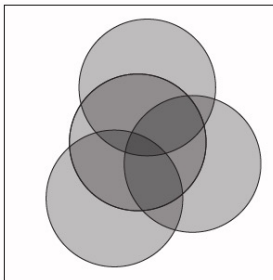
- X-ray microscopy with high resolution not limited by X-ray optics
- In Bragg geometry, it is sensitive to atomic displacements
- The convergence of the phase retrieval algorithms requires:
 - Isolated sample in 3D
 - Sample size limited to a few microns
- Practical consequences (mostly in forward direction)
 - Not robust to realistic sample preparation
 - Convergence issues
 - Typically sample lying on a membrane: missing wedge in 3D reciprocal space
 - Beamstop is often required: missing low frequencies
- CDI is done at FELs, Bragg geometry beamlines with micro- or nano-focus (Argonne, ESRF, Petra III, MAX-IV) and a few beamlines in forward direction (ESRF). Permanent setups exist for both soft and hard X-rays.

Ptychography



**Fourier
constraint**

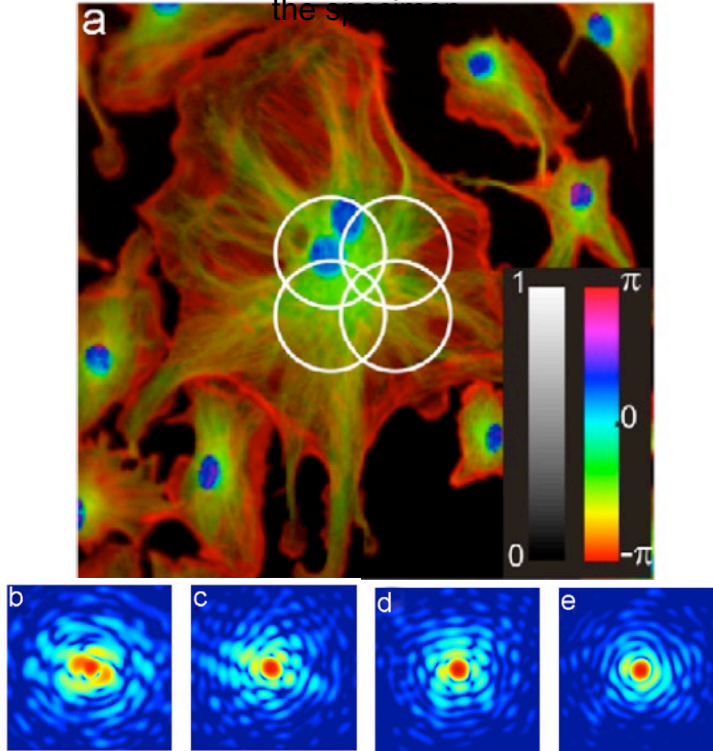
image is consistent with measured intensities



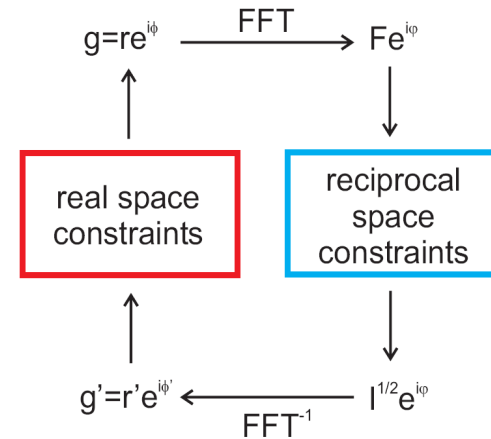
**overlap
constraint**

overlapping regions agree and
incident wave field is unique

oversampling by coherent diffraction patterns from overlapping regions of the specimen

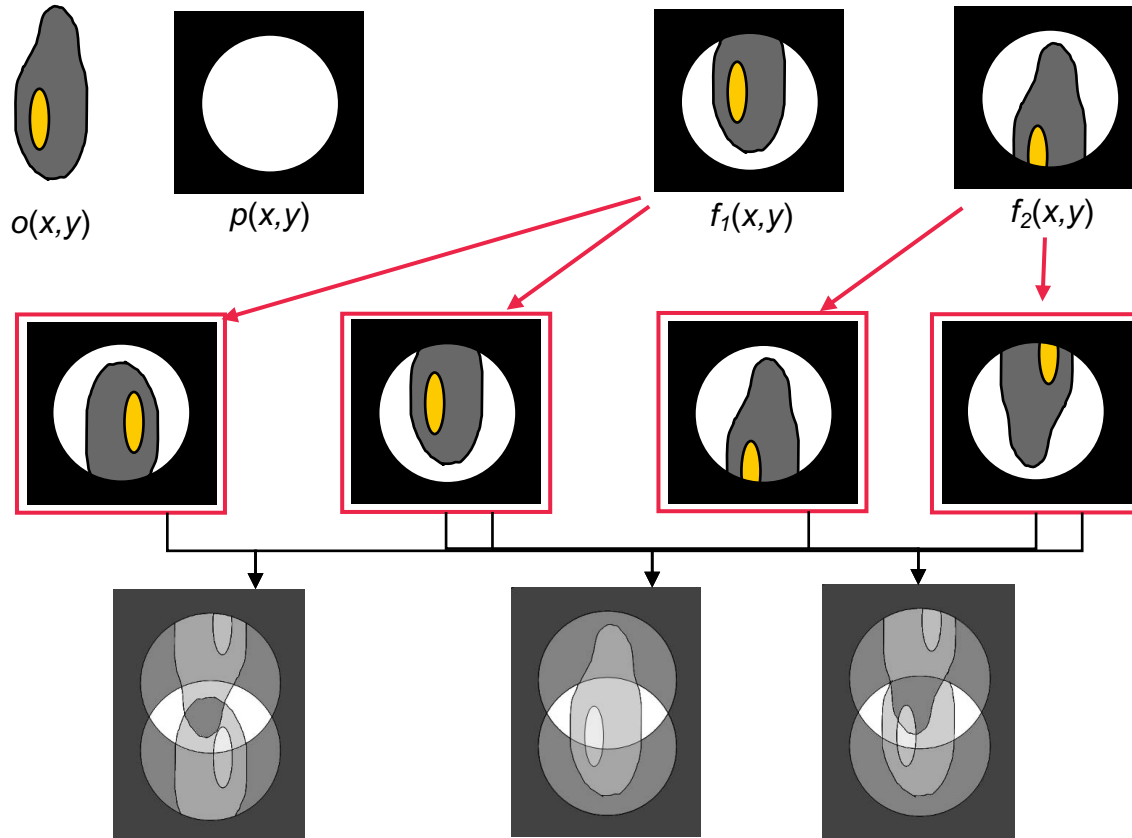


Phase retrieval algorithms to reconstruct complex-valued transmissivity



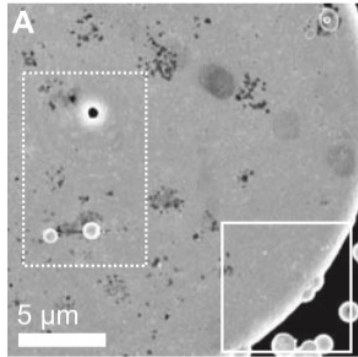
H. M. L. Faulkner & J. M. Rodenburg,
Phys. Rev. Lett. **93** (2004) 023903

Ptychography: overlap constraint



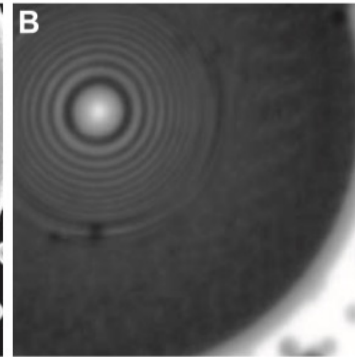
Overlap in ptychography is a crucial constraint for phase retrieval

Ptychography with probe retrieval



electron microscopy

gold layer on top



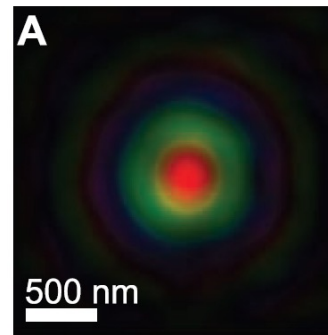
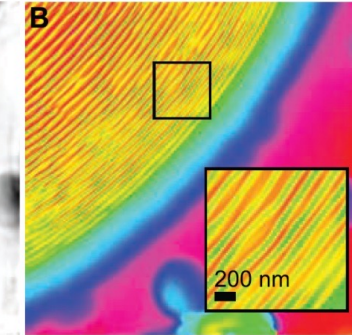
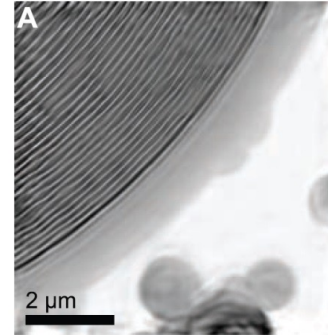
STXM – transmission

300 nm probe size

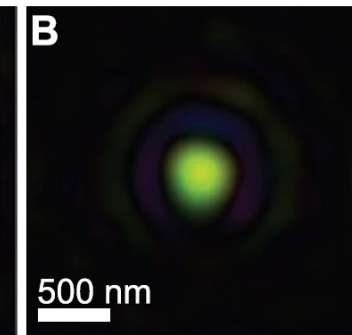
$$\psi_j(\mathbf{r}) = P(\mathbf{r} - \mathbf{r}_j)O(\mathbf{r})$$

Enough information to retrieve complex-valued illumination simultaneously

P. Thibault *et al.*, Science **321** (2008) 379



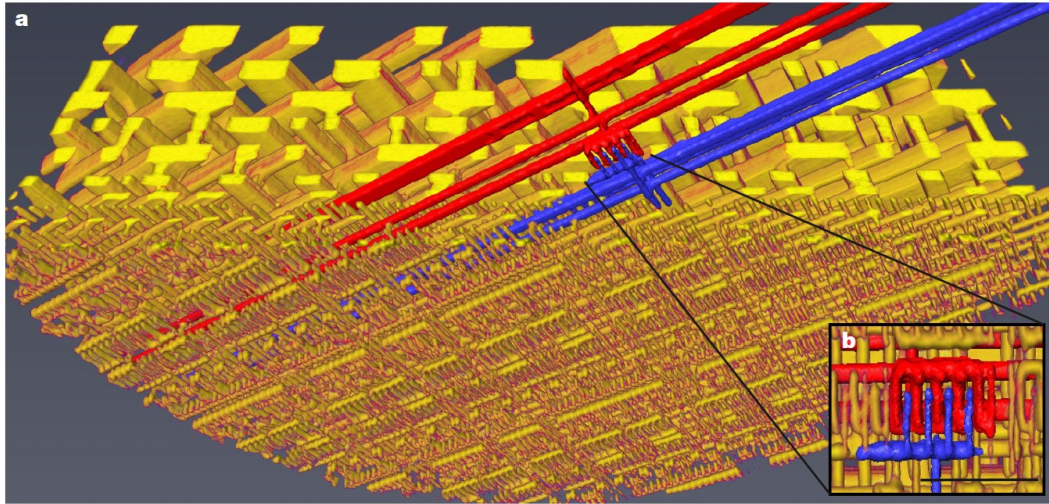
reconstructed
at sample position



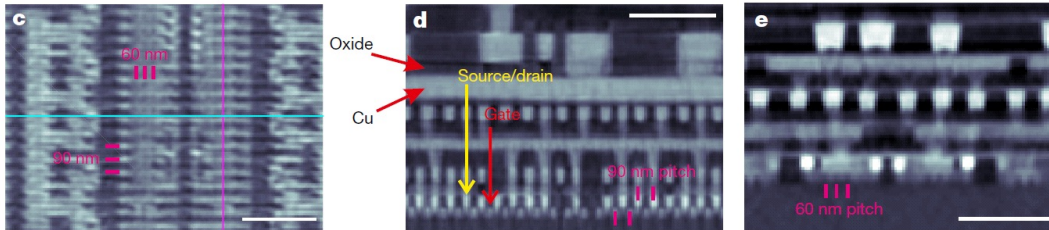
back-projected
to focal plane

Ptychographic nanotomography

Intel chip, 22 nm technology



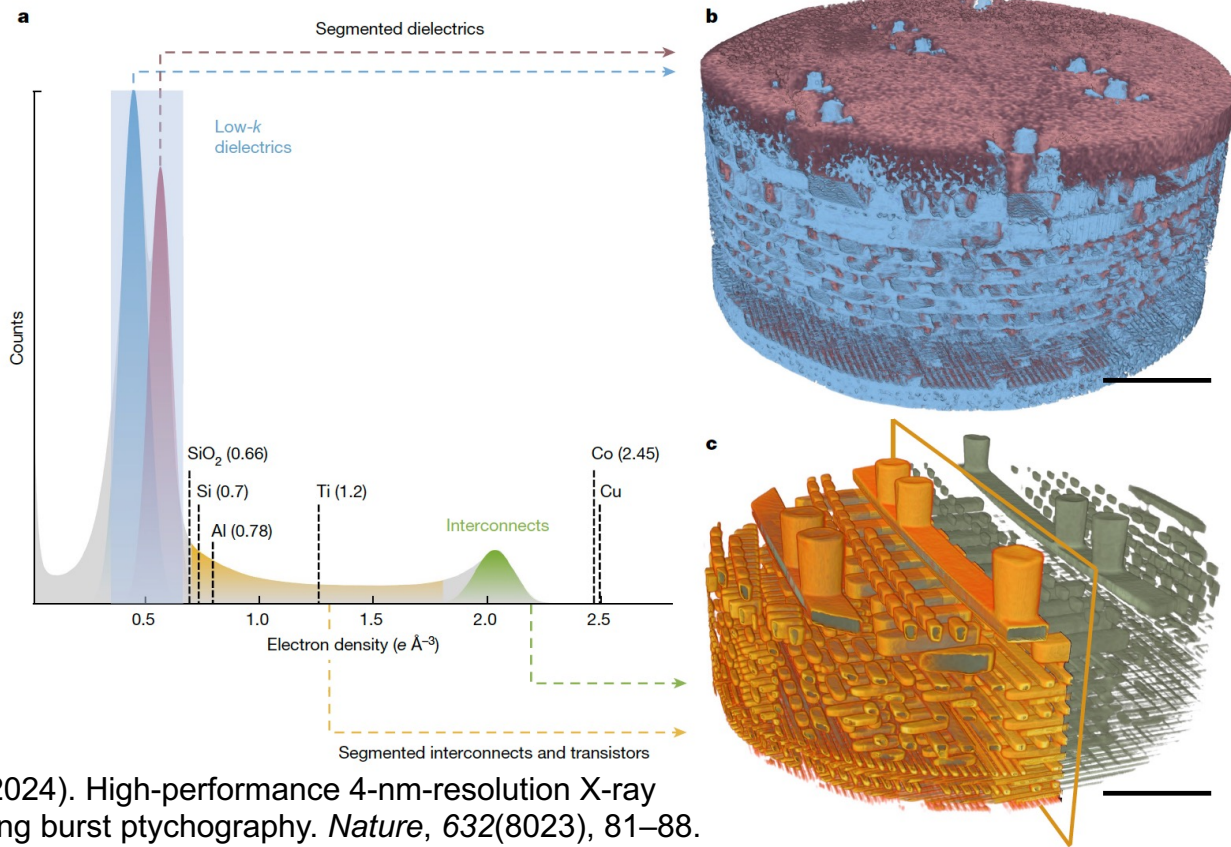
Resolution: new record: 4nm resolution
14.6 nm



Scale bars:
500 nm

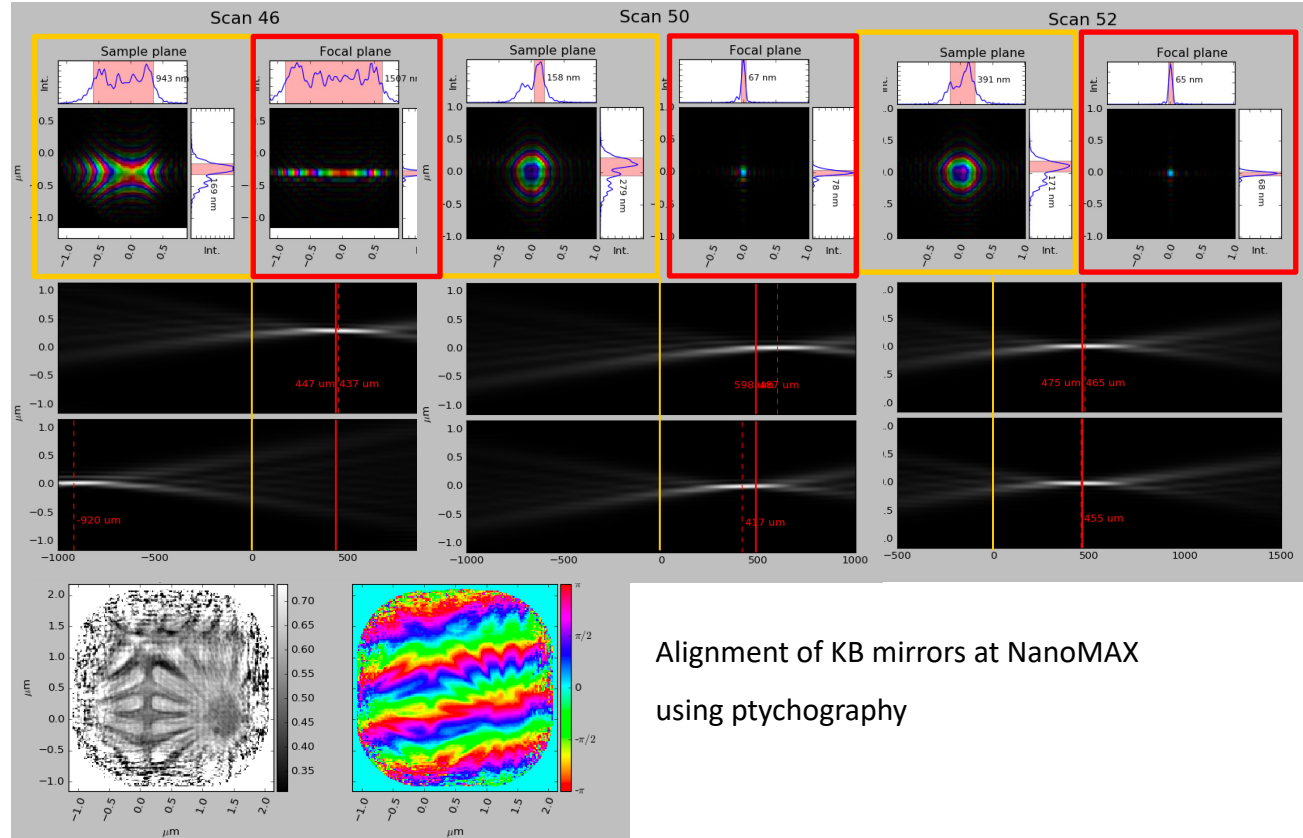
M. Holler *et al.*, Nature **543** (2017) 402

Ptychographic Nanotomography



Aidukas, T., et al. (2024). High-performance 4-nm-resolution X-ray tomography using burst ptychography. *Nature*, 632(8023), 81–88.

X-ray optics characterization with ptychography



Alignment of KB mirrors at NanoMAX
using ptychography

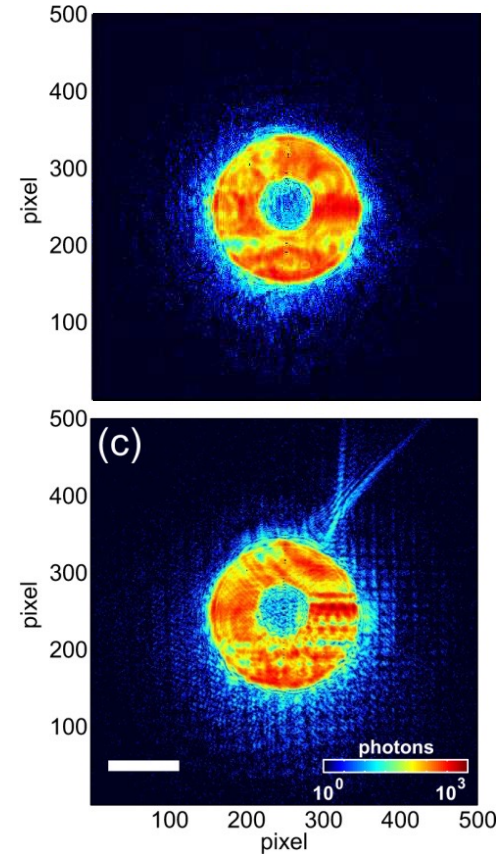
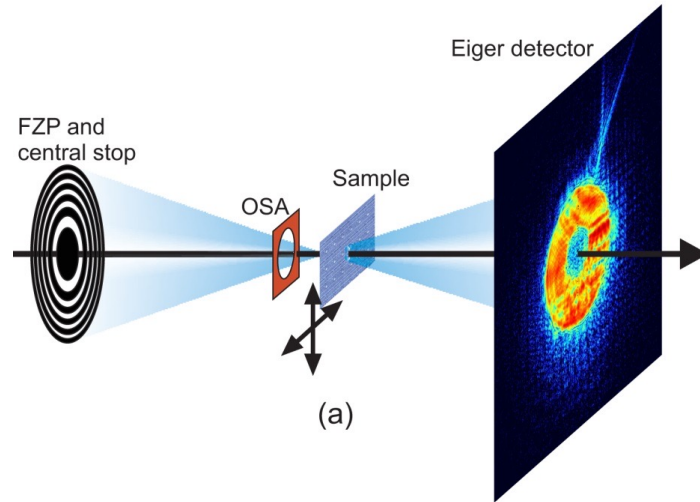
Imaging throughput – The Eiger self portrait

Sample 5 mm downstream of focus

Beam at sample ~ 10 microns

Scanning average step 3.5 microns

Eiger as sample and detector



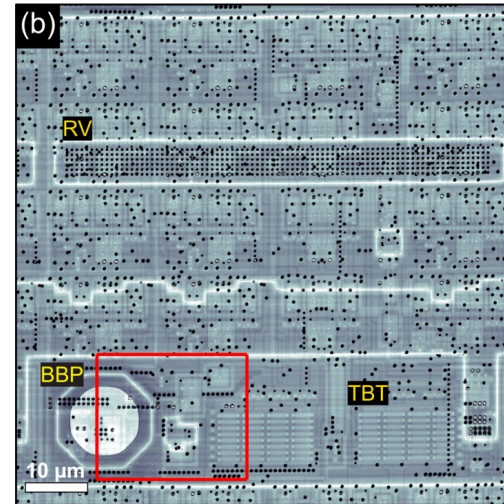
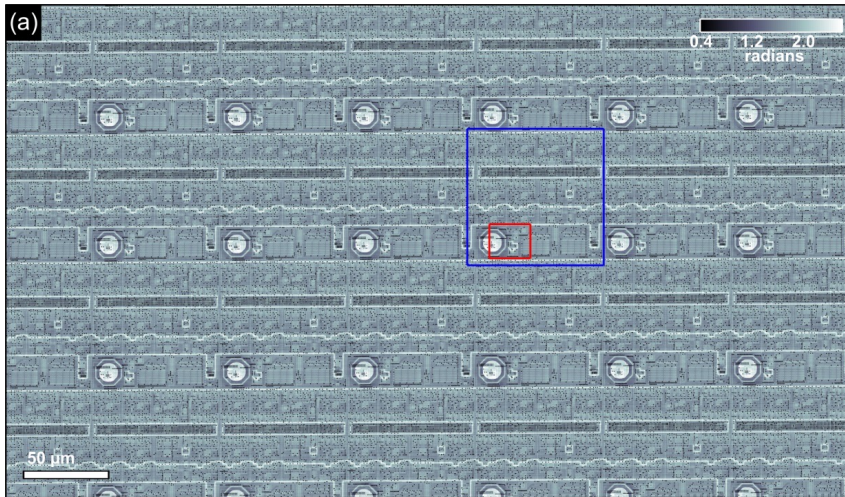
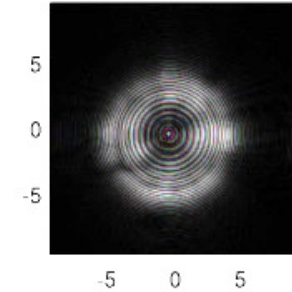
Imaging throughput – The Eiger self portrait

98.4 Mpixel (13,028 x 7,556)

Resolution 41 nm, 38.4 nm pixel

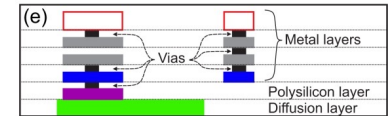
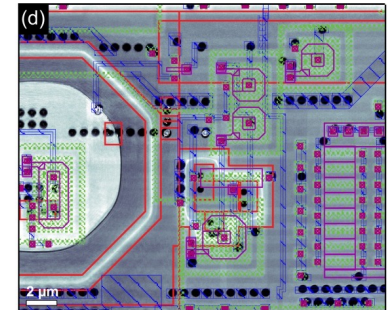
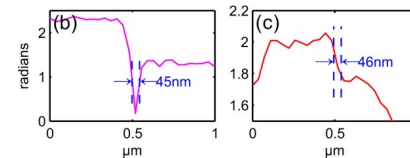
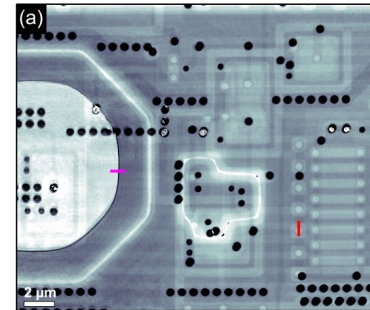
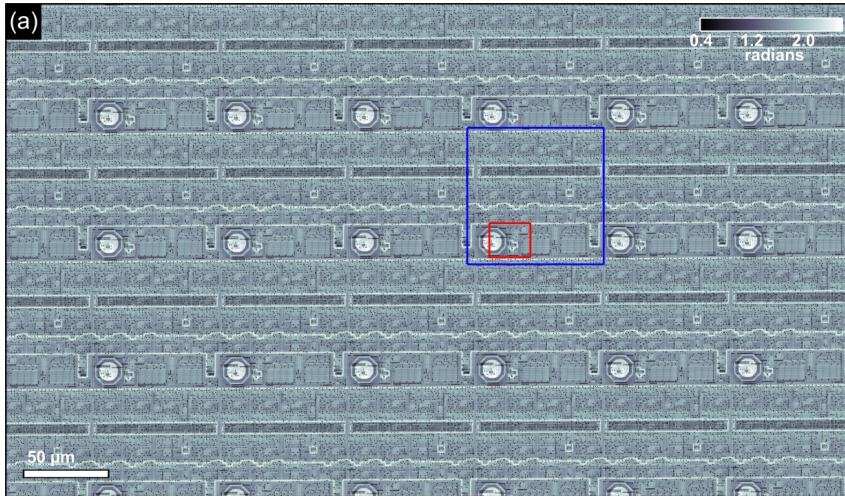
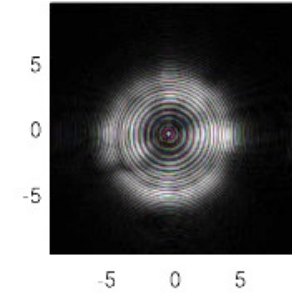
> **25,000** resolution elements / second

40 microsecond per resolution element



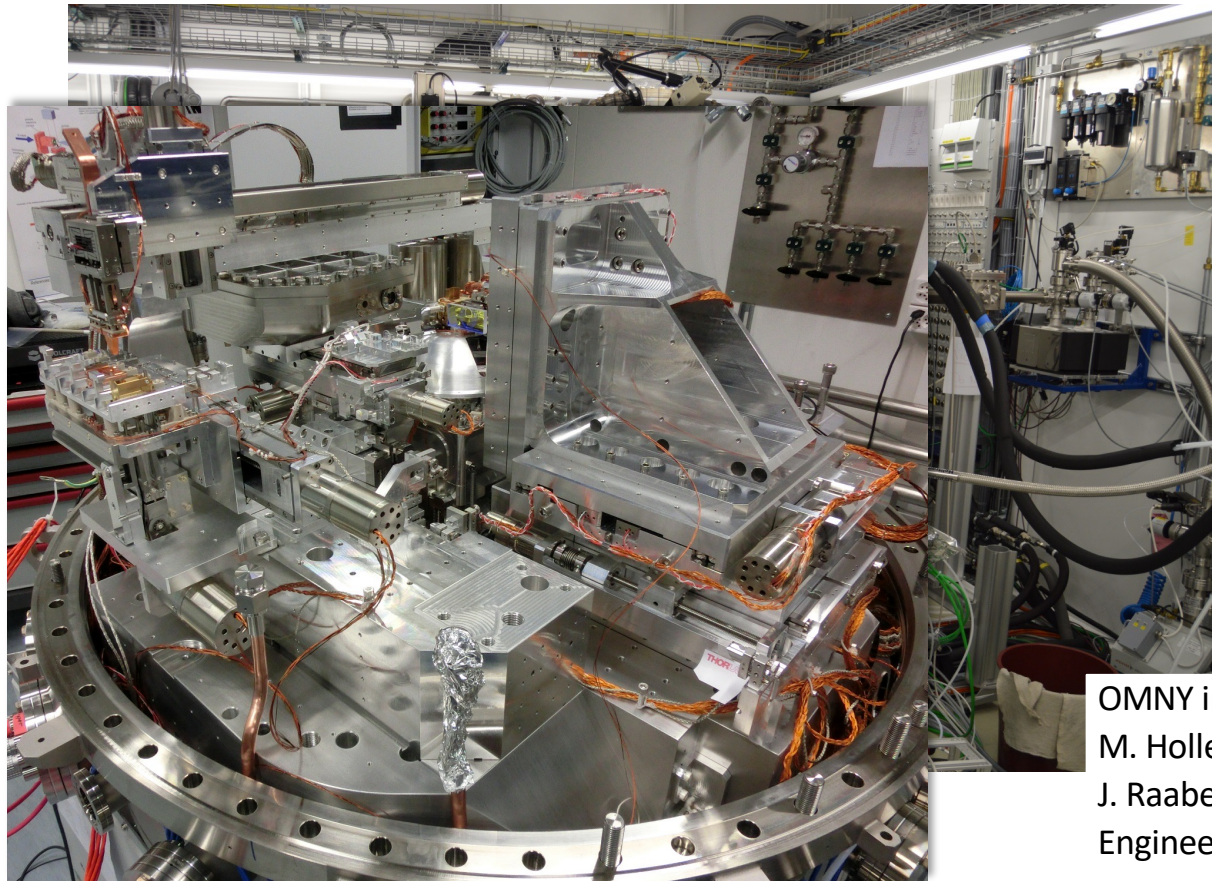
Imaging throughput – The Eiger self portrait

98.4 Mpixel (13,028 x 7,556)
 Resolution 41 nm, 38.4 nm pixel
 > **25,000** resolution elements / second
 40 microsecond per resolution element



- X-ray ptychography is a robust, top-quality imaging technique:
 - very high phase sensitivity
 - quantitative phase and absorption contrast
 - very high spatial resolution
- allows for extended samples (compared to CDI)
- The illumination is separated from the complex-valued transmissivity of the sample and it does not need to be a plane wave
- Requires a stable illumination and position accuracy between illumination and sample equal or better than the aimed resolution
- Practical consequences: sophisticated instrumentation, especially for 3D
- Ptychography is performed nowadays in many 3rd generation synchrotron sources worldwide and its performance is expected to be much better in 4th generation sources..

Ptychography: accurate position control



OMNY instrument SLS
M. Holler
J. Raabe
Engineer team at PSI



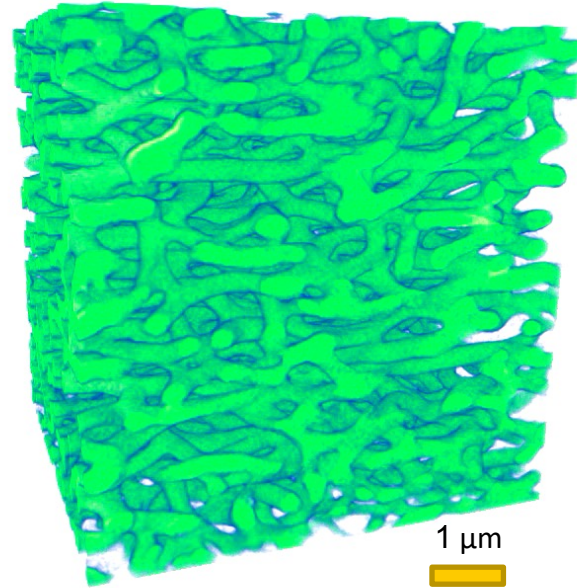
Cyphochilus

Radiation sensitive biological structure – Not measurable under non-cryogenic conditions.

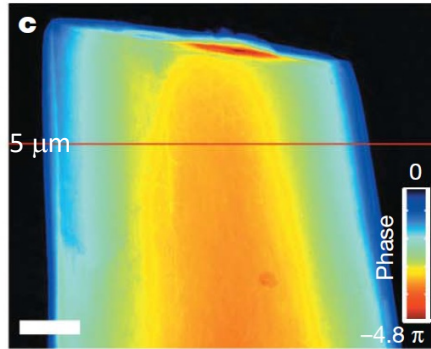
Measured at 92K +/- 0.4 mK

Holler, M. *et al. Review of Scientific Instruments* **89**, 043706, (2018).

Bodo D. Wilts, *et al Advanced Materials*



Ptychography: Quantitative mass density values



phase shift:

$$\phi(x, y) = -\frac{2\pi}{\lambda} \int \delta(\mathbf{r}) dz$$

electron density: $n_e(\mathbf{r}) = \frac{2\pi\delta(\mathbf{r})}{\lambda^2 r_0}$
away from absorption edges!

mass density: $\rho = \frac{n_e A}{N_A Z}$

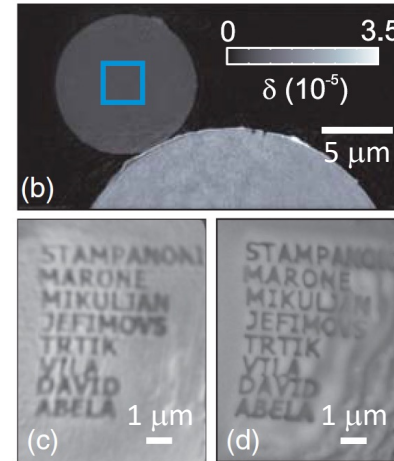
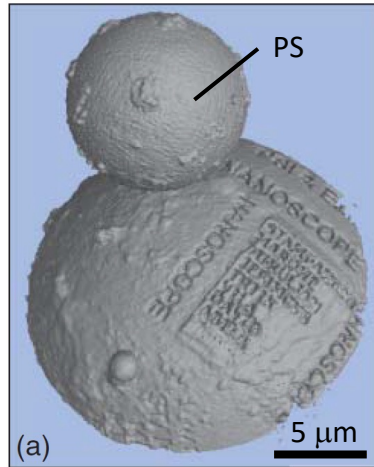
with A: molecular mass

Z: number of electrons in the molecule

Ptychography: Quantitative mass density values

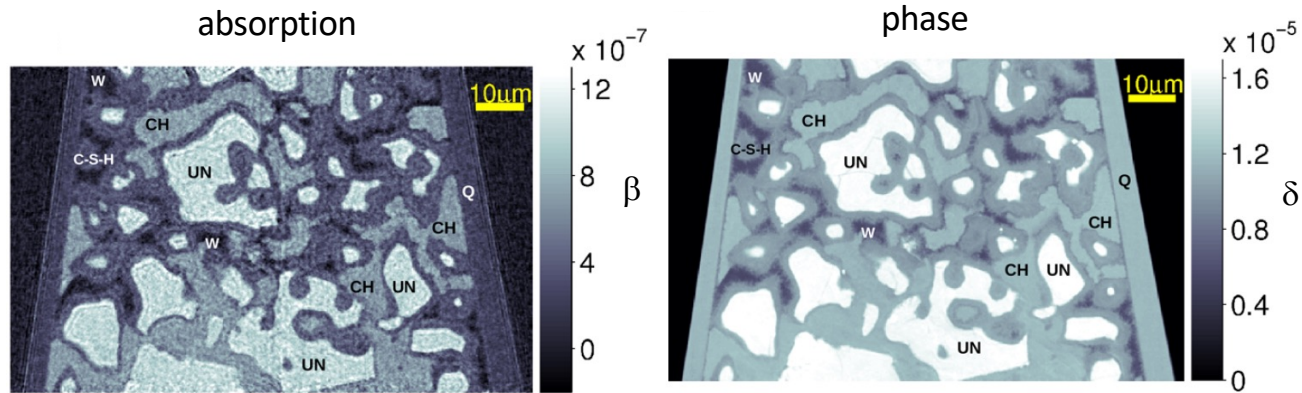
Demonstration of absolute density measurement

A. Diaz *et al.*, Phys. Rev. B **85** (2012) 020104(R)



- Ptychographic tomography on test specimen
- Polystyrene sphere (PS) of 10 μm diameter with homogeneous density of **1.055 g/cm³**
- Measured density on PS based on gray values: **1.048 ± 0.008 g/cm³**
- (c) Spherical tomogram section
- (d) SEM image of the surface

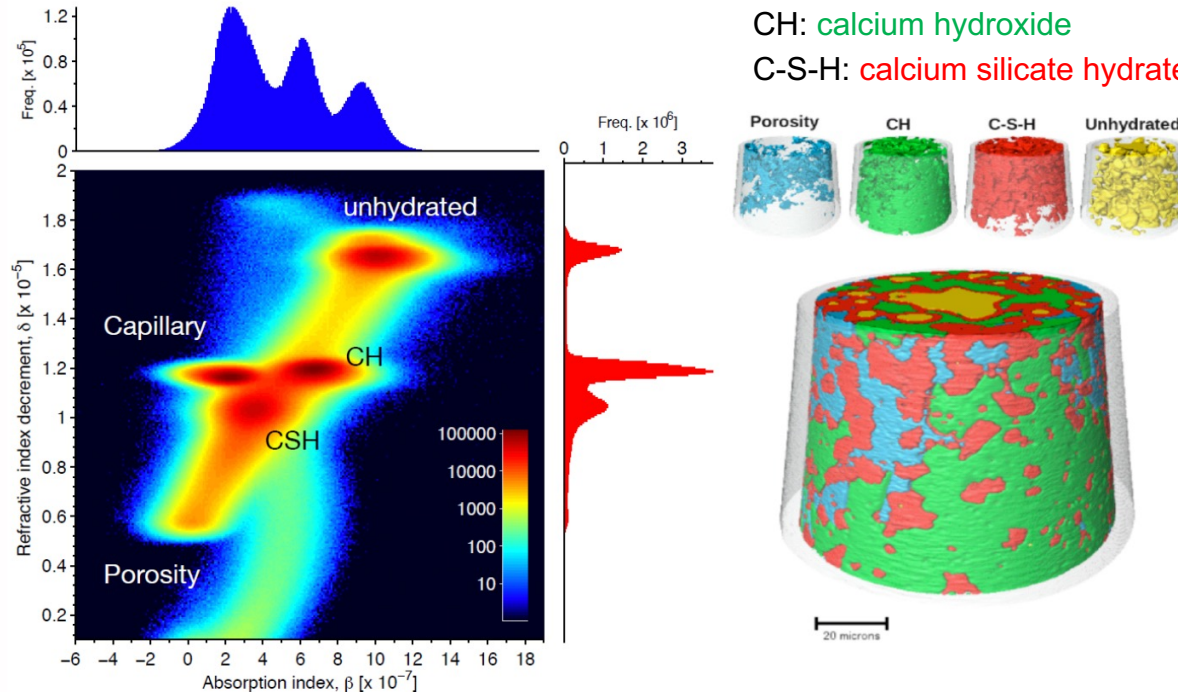
Ptychography on hydrated cement paste



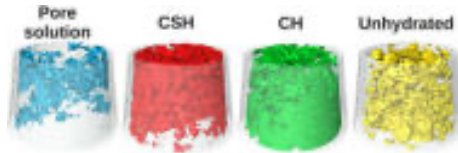
Ptychography on hydrated cement – segmentation

bivariate histogram of absorption and phase information for segmentation

UN: unhydrated alite particles
 W: porosity comprising mostly water
 CH: calcium hydroxide
 C-S-H: calcium silicate hydrates



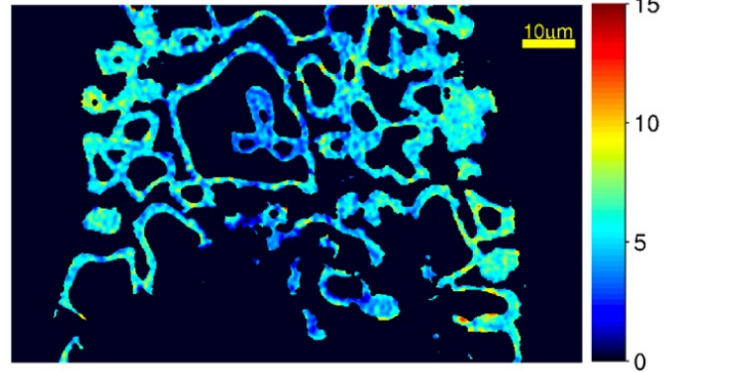
Ptychography on hydrated cement – water content



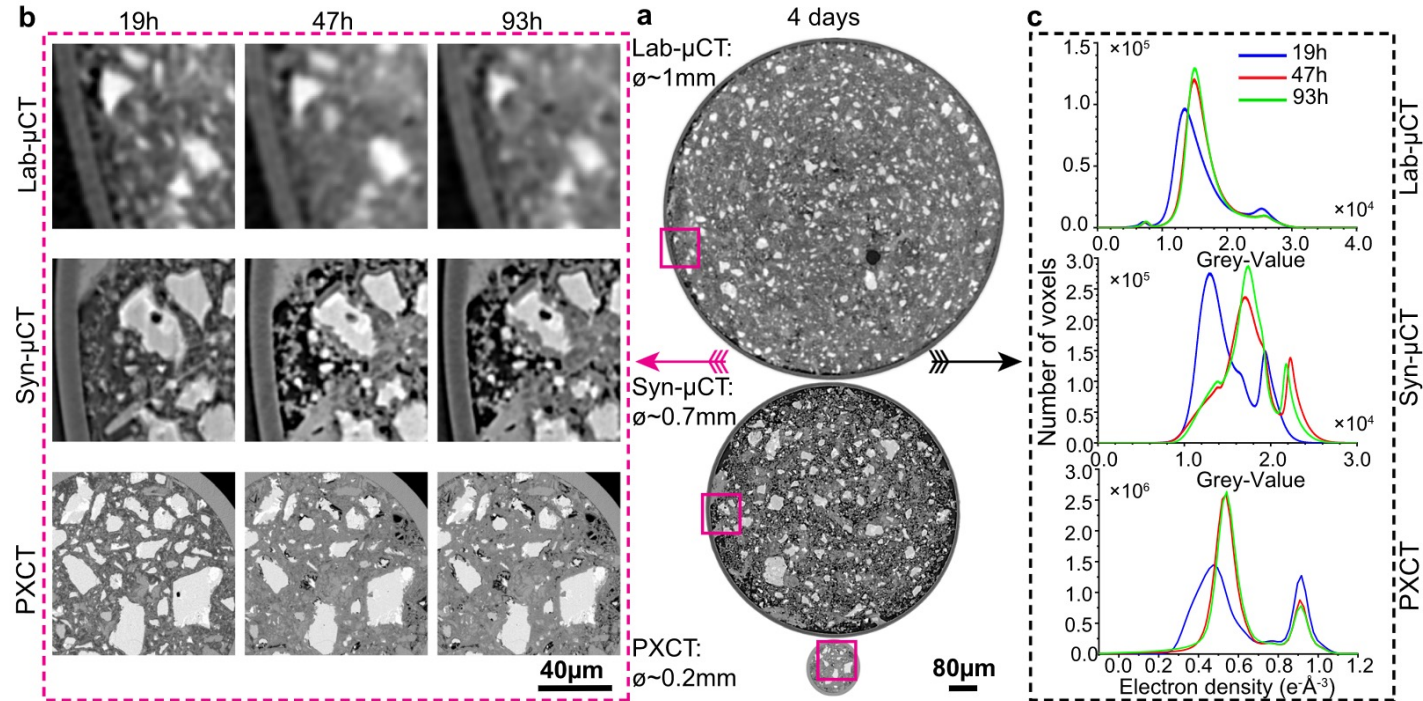
from quantitative mass density and stoichiometry,
the local water content could be determined



site-specific water content

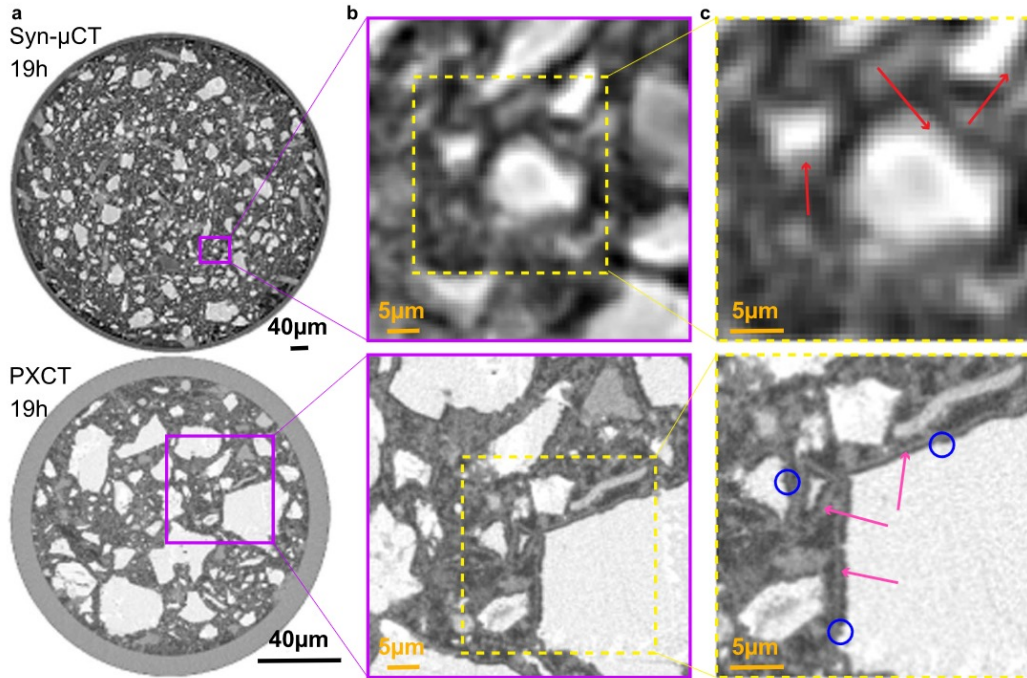


Laboratory/Synchrotron μ CT and Ptychography on cement



Shirani, S., et al. (2023). Nature communications <https://doi.org/10.1038/s41467-023-38380-1>

Laboratory/Synchrotron μ CT and Ptychography on cement

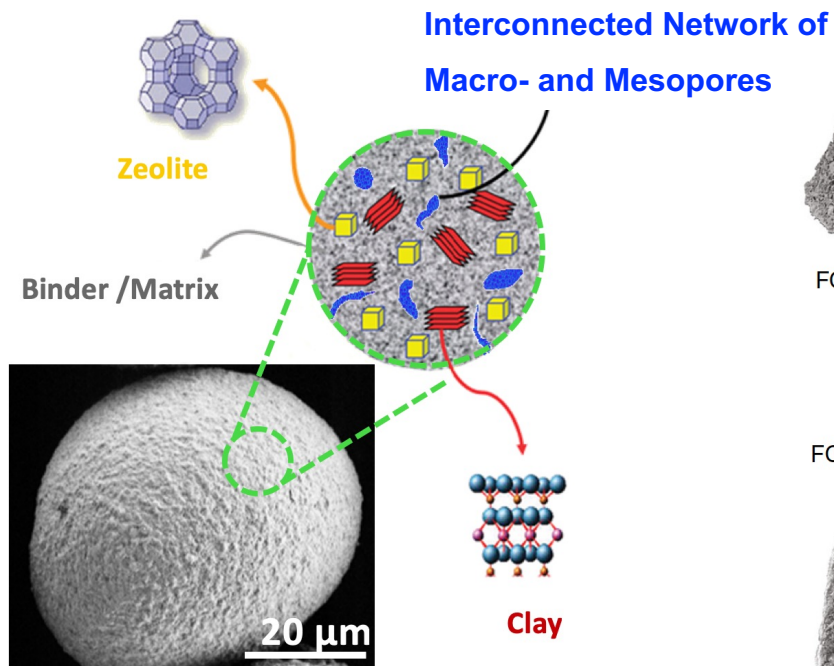


high resolution and contrast allows to resolve the C-S-H gel shells surrounding the alite particles (pink arrows) which is important to understand the mechanisms of cement hydration

Shirani, S., et al. (2023). Nature communications <https://doi.org/10.1038/s41467-023-38380-1>

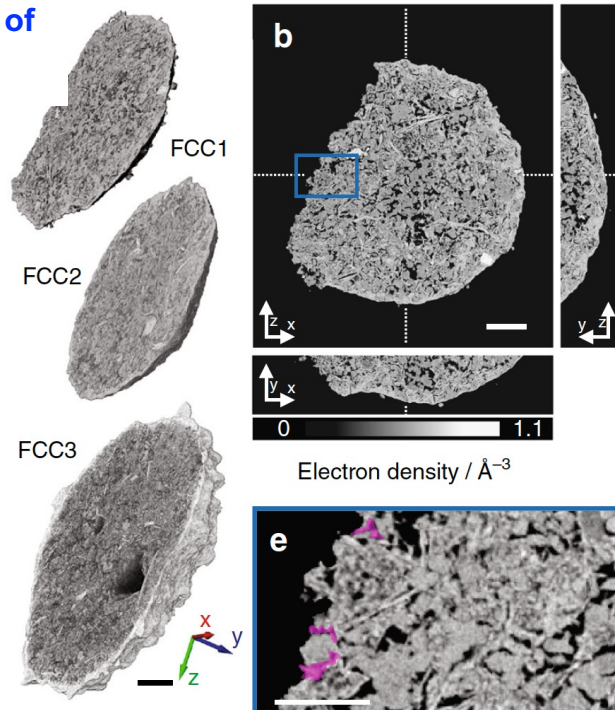
published May 8th 2023

Ptychography on catalytic particles



Adapted Figure- Perego and Millini *Chem. Soc. Rev.*, 2013, 42

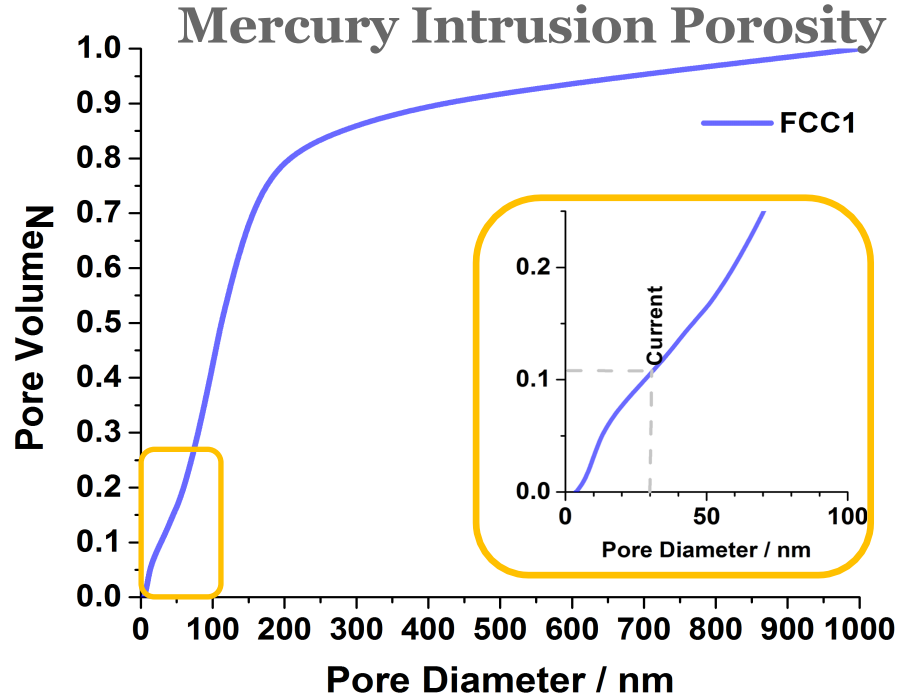
ptychographic nanotomography



J. Ihli et al. *Nature Communication*, 2017, 8, 809

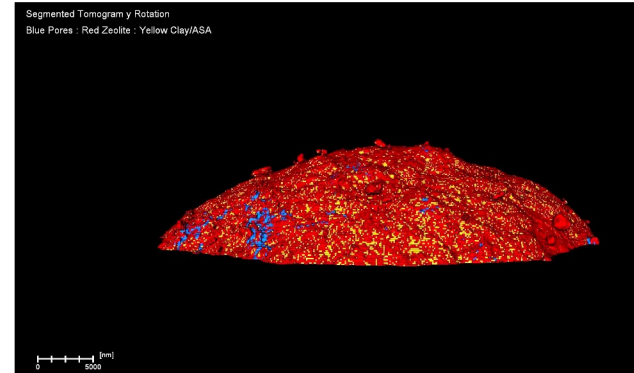
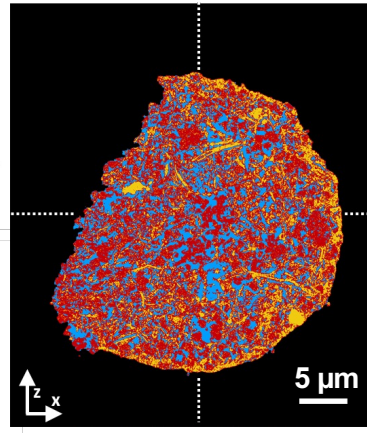
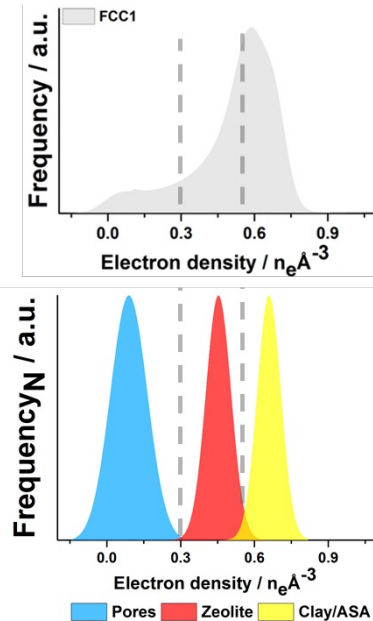
Ptychography – resolution vs. pore size

Resolution by Fourier shell correlations 31 nm



=> Tomograms probe a pessimistic ~90% of the macro and mesopore volume.

Ptychography on catalytic particle – component segmentation

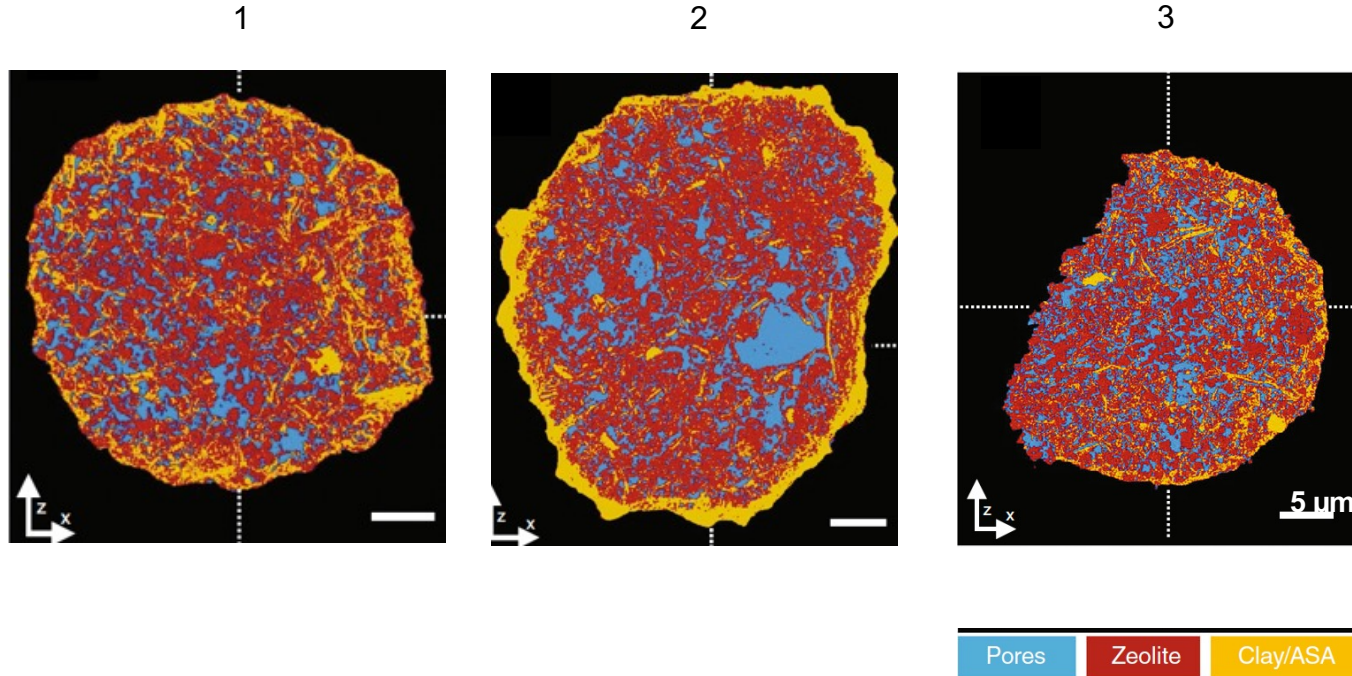


Pores (Grouping of Air and Hydrocarbons)

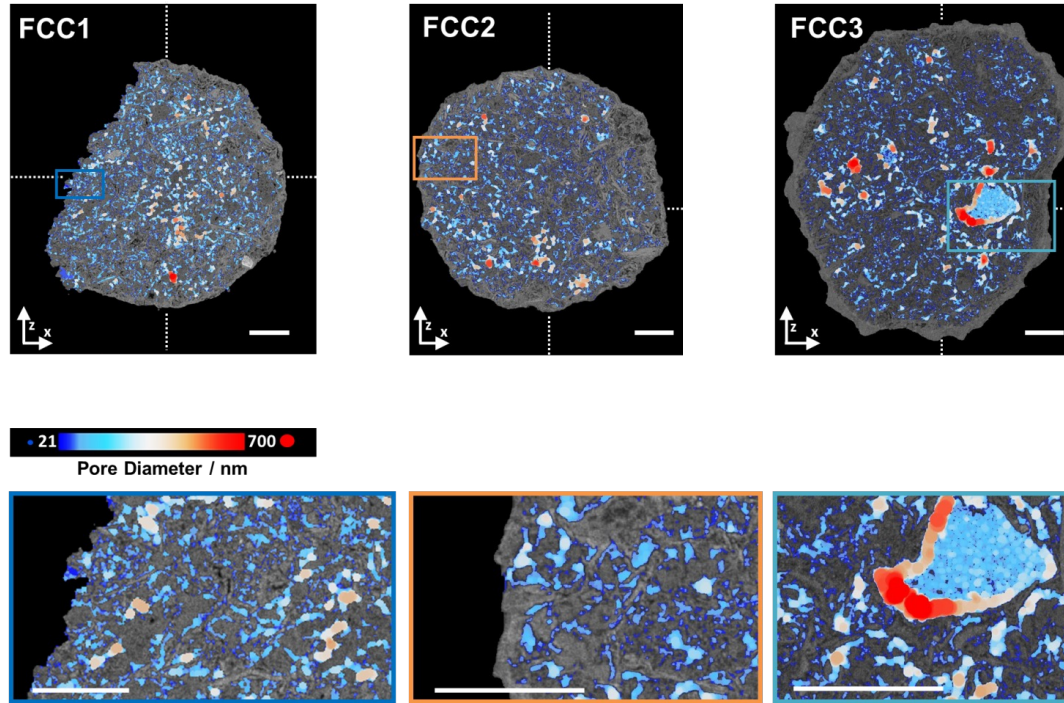
Clay/ASA (TiO_2 , Clay and amorphous silica–alumina)

Zeolite

Which particle is the most deactivated?

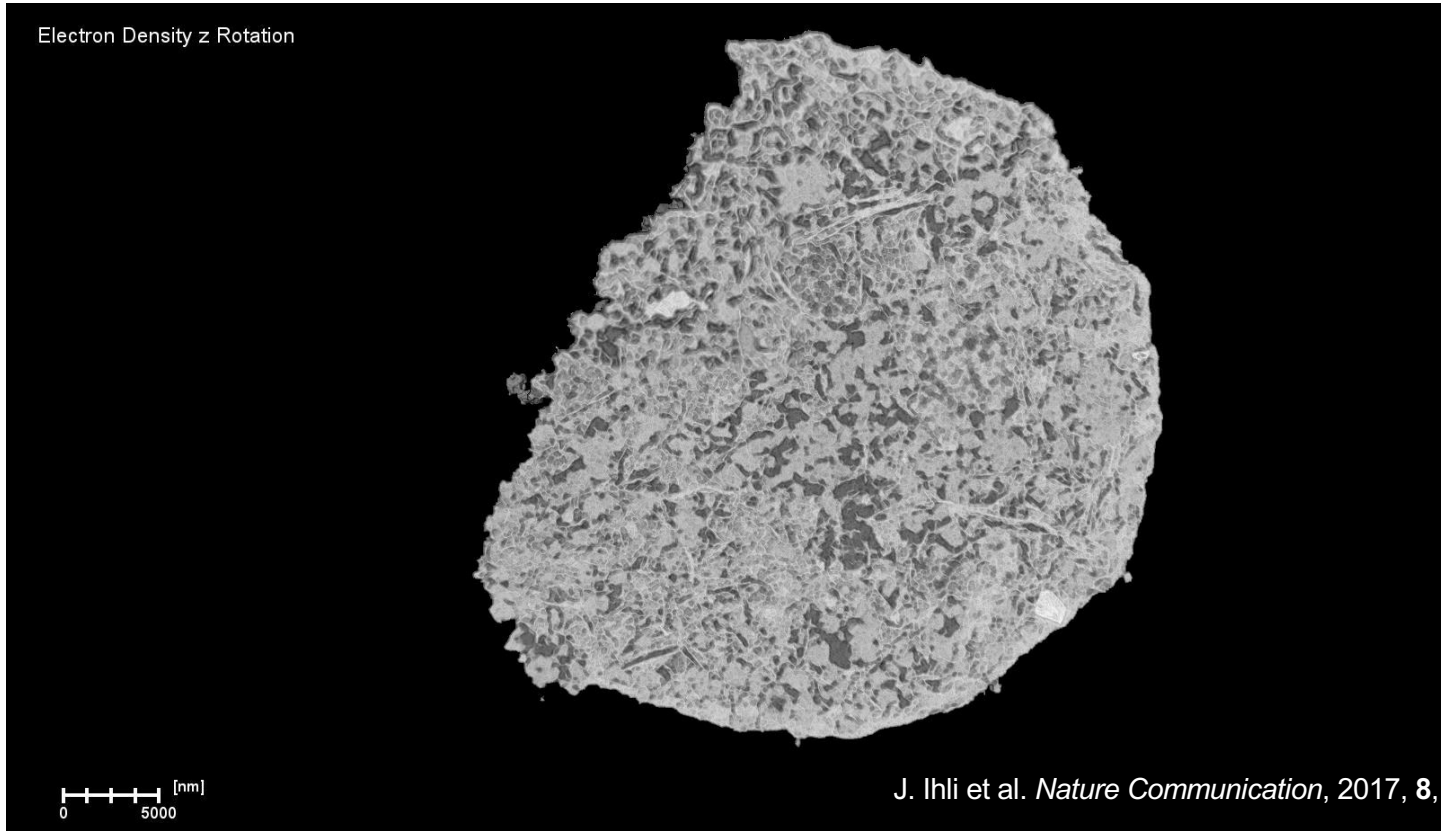


Ptychography on catalytic particle – pore size analysis

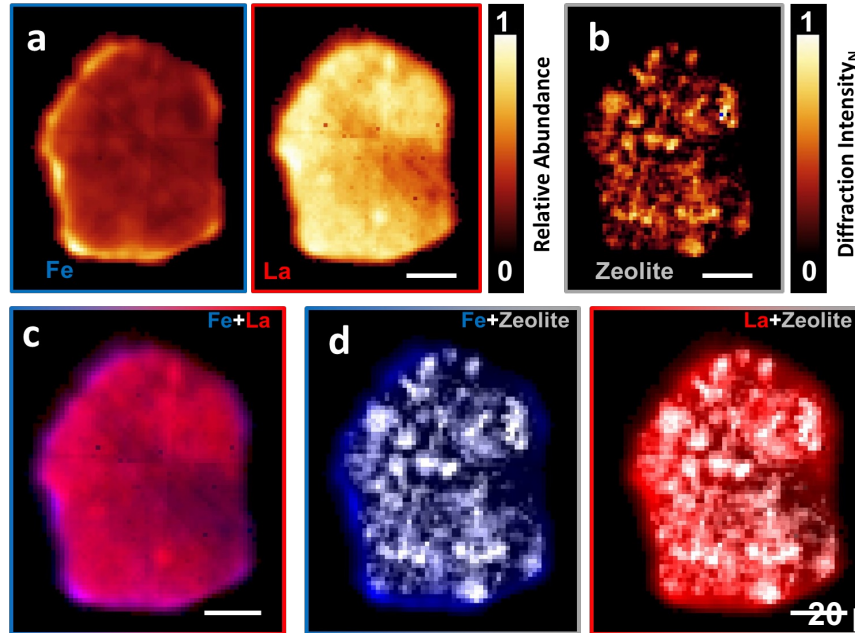


each porous region is fitted with maximal spheres filling this region best

Ptychography on catalytic particle – pore size analysis and diffusion highways



XRD/XRF Tomography – on catalytic particle



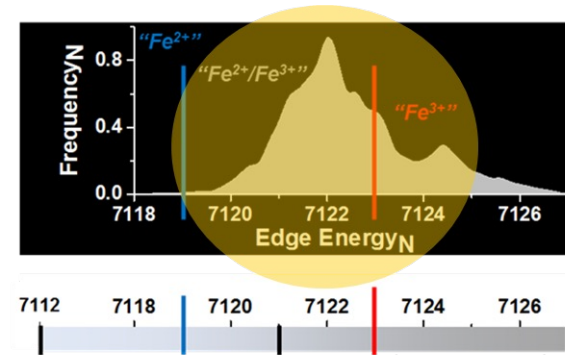
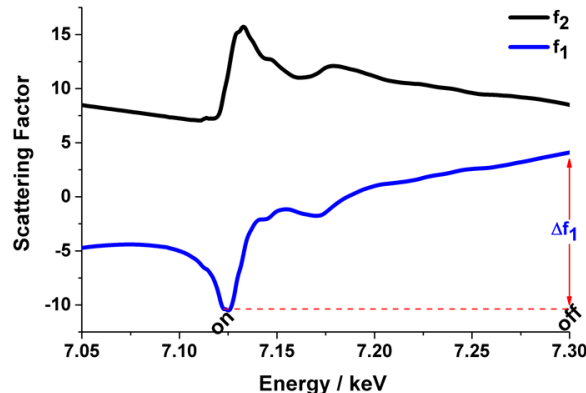
- Iron representative of amorphous silica-alumina shell
- Lanthanum representative of zeolites in pristine state (look into past)
- XRD current location of crystalline components

Resonant Ptychographic Tomography

3D quantitative colocalization of chemical elements with physical features of functional matter with nanoscopic resolution.

Here colocalization of iron impurities within the primary components of a deactivated FCC catalyst. Spatial Resolution ~ 39 nm.

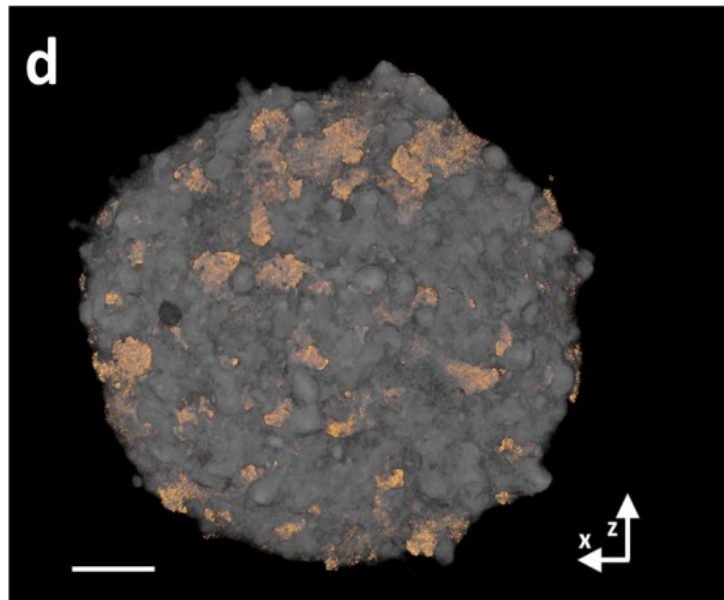
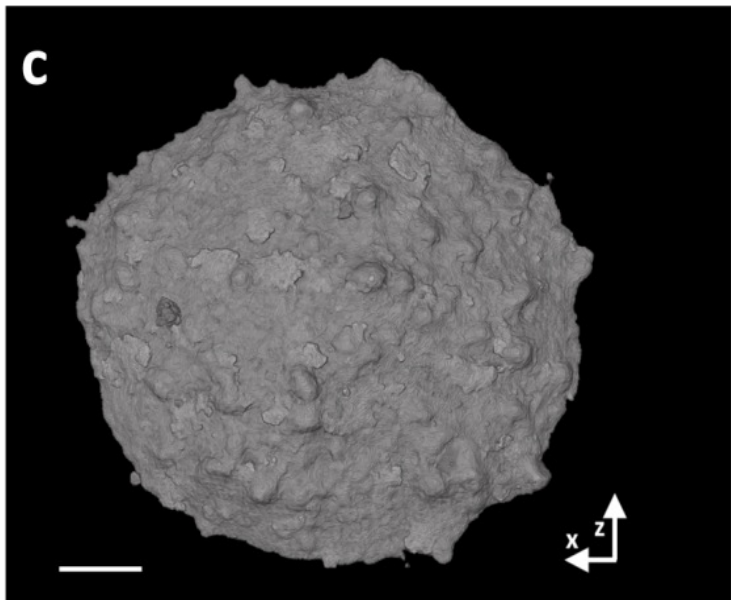
Acquired by means of a comparison of *on* and *off* resonance Fe-K edge ptychographic tomograms.



$\sim 95\%$ of iron species in question posses a resonant energy of ± 2 eV of the selected on-resonance energy !

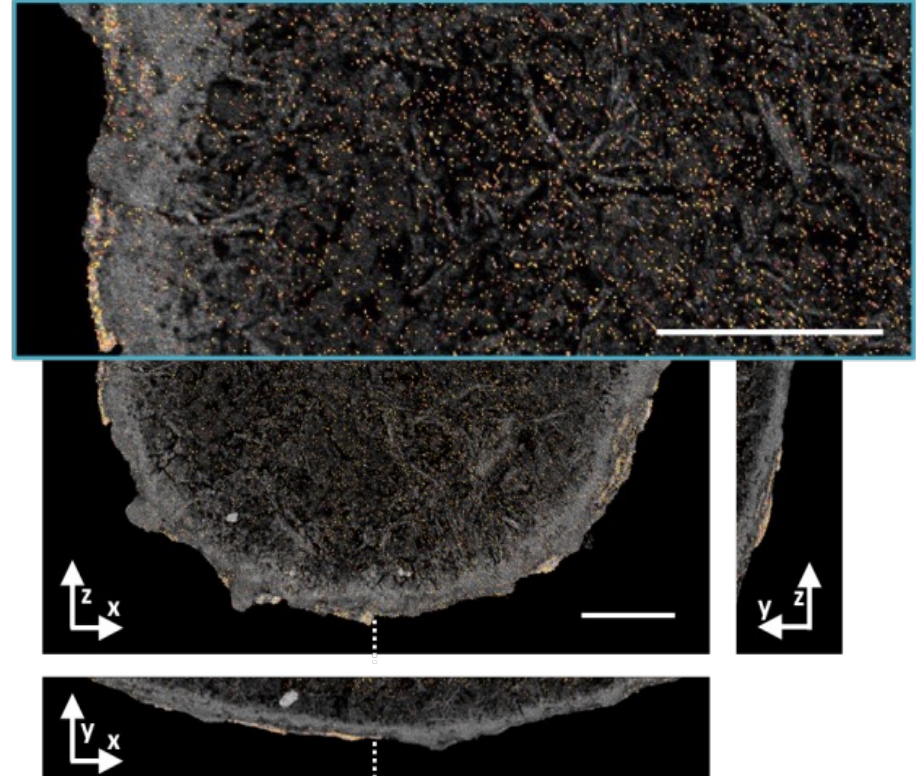
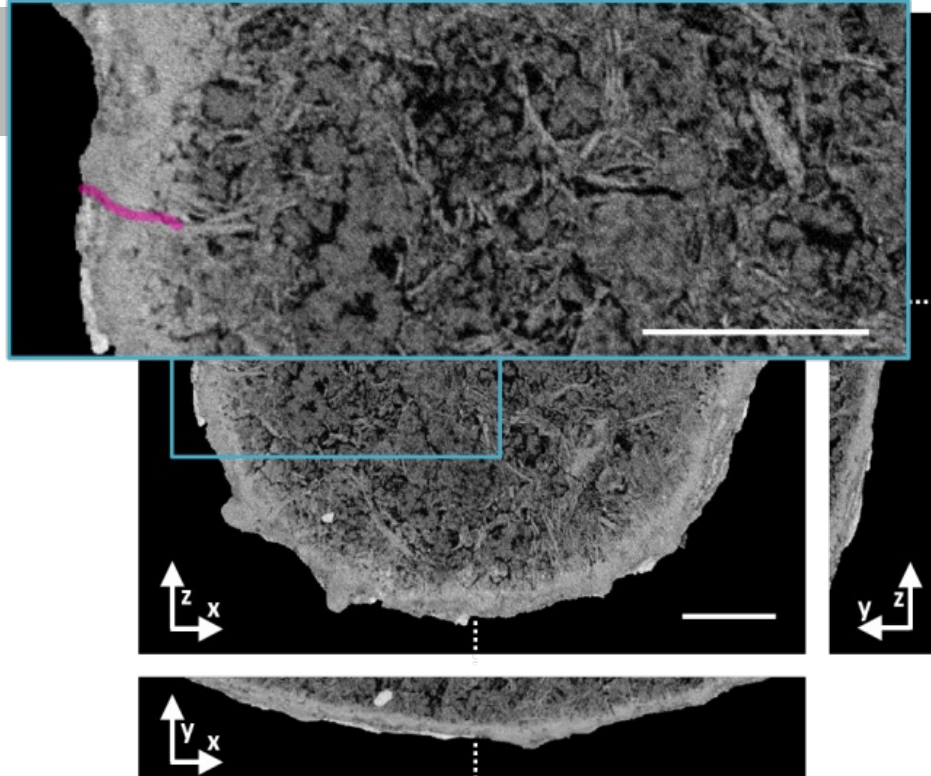
Resonant Fe *K*-Edge Ptychographic Tomography

Deactivated Fluid Catalytic Cracking Catalyst (FCC3) measured electron density tomogram and iron distribution



Resonant Fe *K*-Edge Ptychographic Tomography

Deactivated Fluid Catalytic Cracking Catalyst (FCC3) measured electron density tomogram and iron distribution

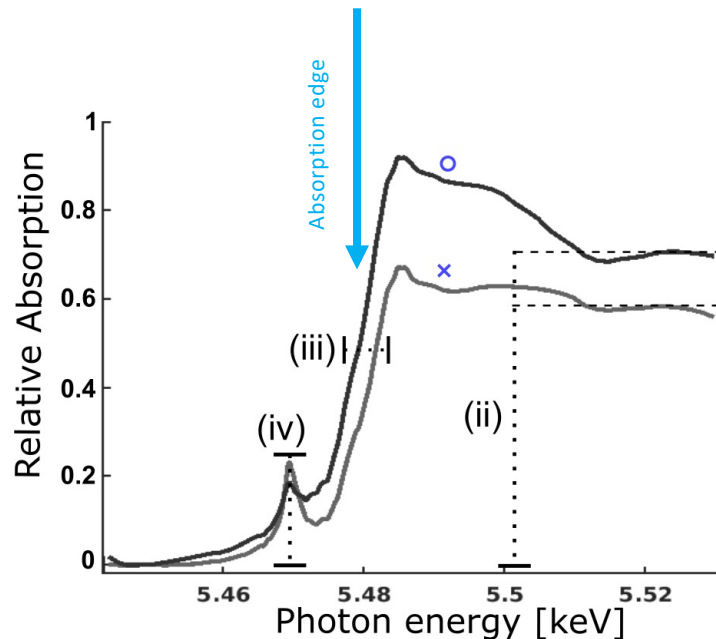


Example spectra across vanadium K-edge

Chemical information

- (ii) Vanadium concentration
- (iii) Oxidation state
- (iv) Coordination geometry (local crystalline order)

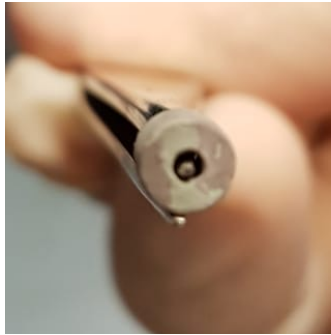
Combine with ptychotomo to obtain
3D nanoscale maps of chemical composition.



Sparse spectral ptychotomography on a VPO catalyst

Vanadium phosphorus oxides catalyst

Used in butane oxidation as prerequisite for household and industrial plastics (biodegradable)



10 micron diameter pillars



Chemical information, such as oxidation state can be obtained by measuring the X-ray transmission spectra

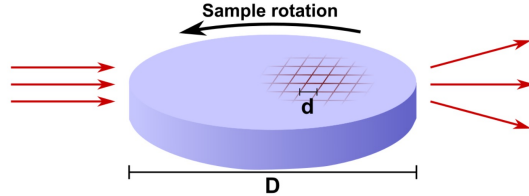
Combine with ptychotomo to obtain 3D nanoscale maps of chemical composition

Measuring one full tomogram per energy would be too slow

Gao *et al*, "Sparse ab initio x-ray transmission spectrotomography for nanoscopic compositional analysis of functional materials", Sci. Adv. **7**, eabf6971 (2021)

Sparse measurements

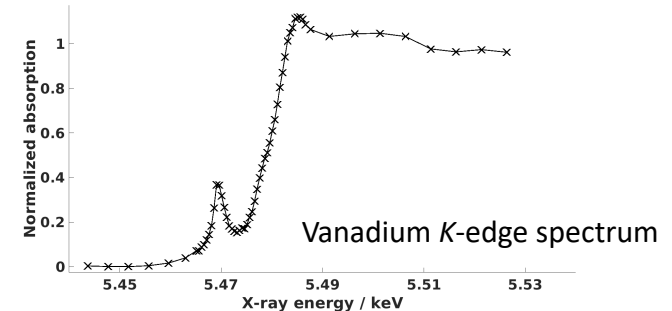
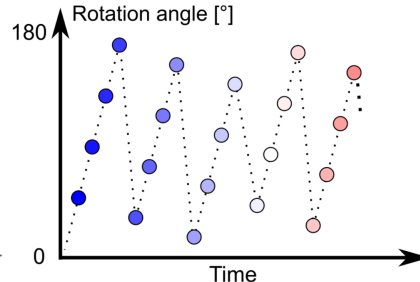
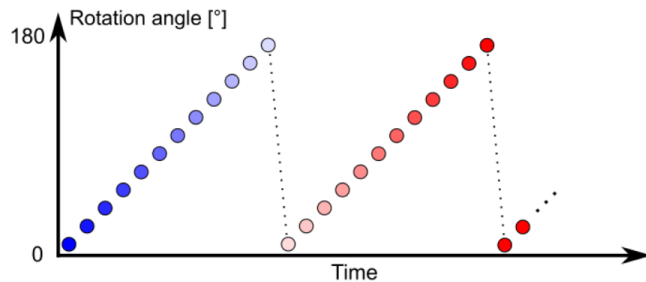
Number of projections needed in a tomography measurement is given by the *Crowther Criterion*:



$$n_p = \frac{\pi D}{2d_{(half-period)}}$$

Conventional sampling of a full tomogram at each time frame / X-ray energy is too long, and not necessary

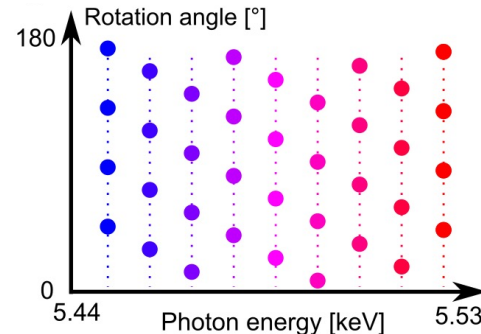
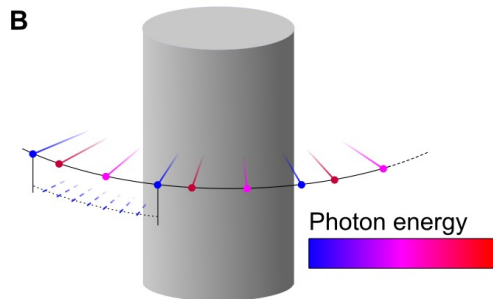
Information is sparse in multidimensional space



Sparse spectral ptychotomography on a VPO catalyst

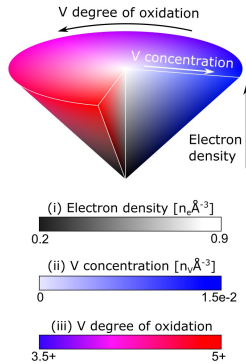
Crucial to reconstruct hyperspectral volume from all projections simultaneously

- Measured at 60 energies between 5.443-5.465 keV, minimum step 0.5 eV
- Sparse angular sampling, **11%** of Crowther sampling criteria. About 1 day of measurement per sample.
- Leverage signal sparsity in the spectral dimension → Only a few spectral modes actually exist
- Novel iterative method for ab initio reconstruction. Combination of PCA and SART. Preserves resolution, quality and SNR

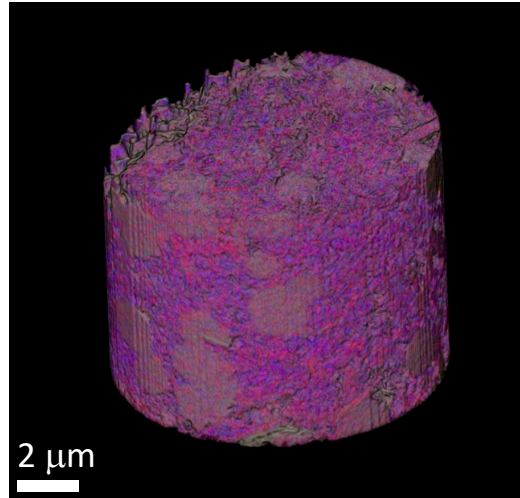


Gao *et al*, "Sparse ab initio x-ray transmission spectrotomography for nanoscopic compositional analysis of functional materials", Sci. Adv. **7**, eabf6971 (2021)

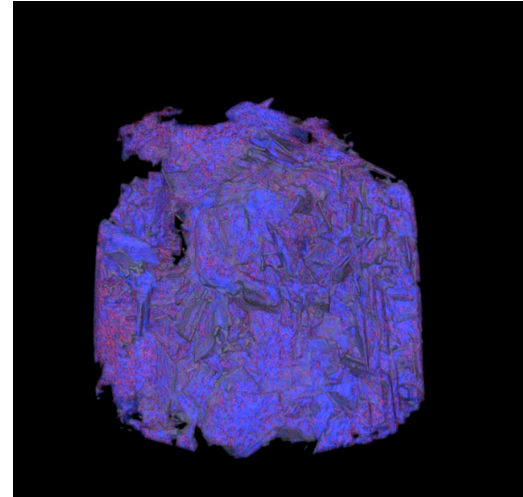
Sparse spectral ptychotomography on a VPO catalyst



Pristine

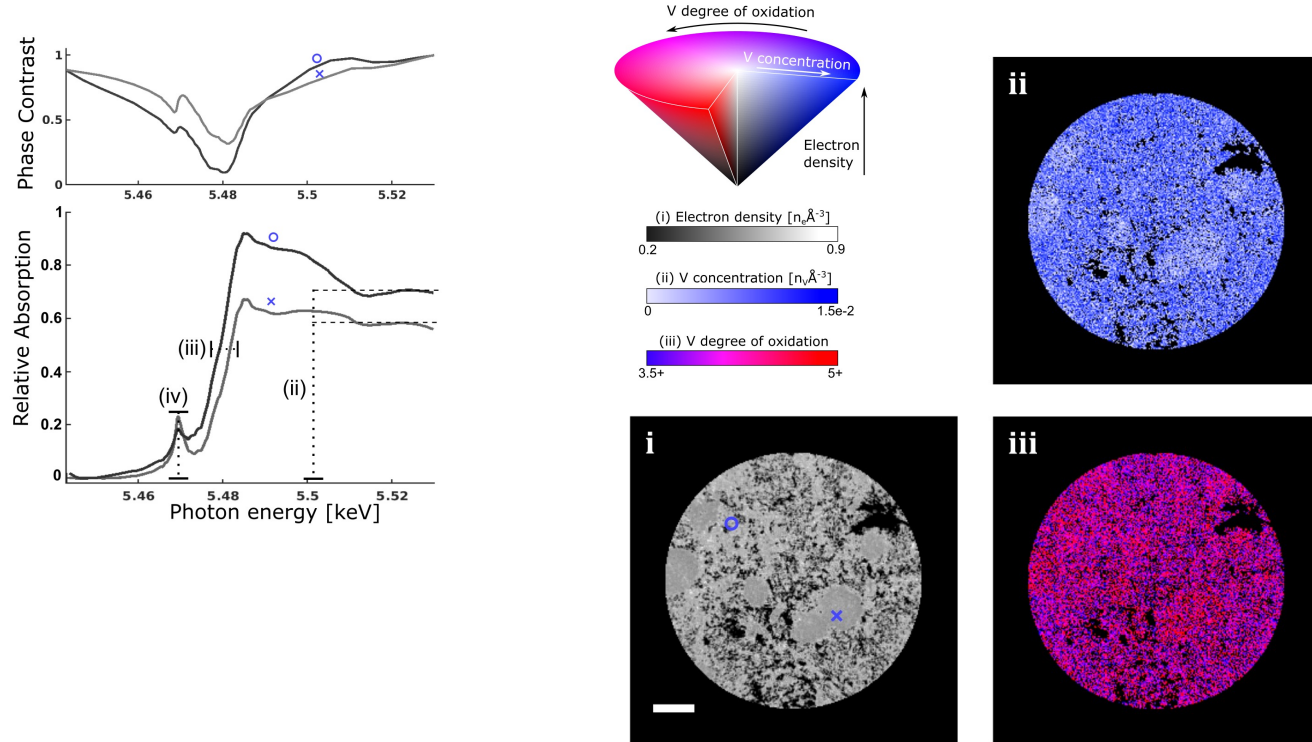


Used (4 years in industrial reactor)



Hyperspectral tomogram resolution 26 nm

Sparse spectral ptychotomography on a VPO catalyst



Gao *et al*, "Sparse ab initio x-ray transmission spectrotomography for nanoscopic compositional analysis of functional materials", *Sci. Adv.* **7**, eabf6971 (2021)

Further analysis reveals **crystal structure defects** (vanadyl deficiencies) in the surface regions of the used catalyst sample. Thus far only theorized to exist as a possible active sites in the catalyzed reaction

