

Solutions to sample exam questions Soft Matter (MSE425)

Question 1: Intermolecular forces (2 points)

- a) Hexane: only **VdW forces**, or **no H-bonds**. (1/2 point)
 Water: Can form **H-bonds**: stronger intermolecular force (1/2 point)
- b) T_m hexanol: -53°C to -41°C , T_m pentanol: -78°C Pentanol has 5 C atoms, hexanol 6 C atoms. Hence **pentanol is shorter (or less C atoms)**, (1/2 point) and thus has **weaker VdW** interactions than hexanol. (1/2 point)

Question 2: Phase diagram (5 points)

a) $\frac{\Delta G}{RT} = \frac{(1-\phi)}{N_1} \ln(1-\phi) + \frac{\phi}{N_2} \ln\phi + \chi\phi(1-\phi)$

$$\phi_c = \frac{1}{1 + \sqrt{\frac{N_2}{N_1}}}$$

$\phi_c = 0.24$ (1 point)

b) $\chi_c = \frac{1}{2N_2} \left(1 + \sqrt{\frac{N_2}{N_1}}\right)^2$ (1 point), $\chi_c = 0.00866$ or 0.0087 (1 point)

c) $\chi = 0.67$ (1 point)

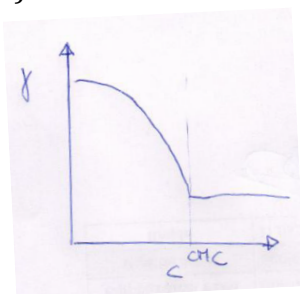
$\chi = 0.67 > \chi_c \rightarrow$ **yes**, the two polymers will phase separate (1 point)

Question 3: Liquid crystals (5 points)

- a) Mesogen A has a **shorter aliphatic chain** (1/2 point) $\rightarrow$ **weaker VdW interactions** (1/2 point) $\rightarrow$ lower transition temperature
- b) $\delta = \frac{2\pi}{\lambda} \Delta n d \rightarrow$ Mesogen A: $d = 389$ nm (1 point),
 Mesogen B: $d = 308$ nm (1 point)
- c) **Nematic (1 point): Two brush schlieren texture** (1 point)

Question 4: Gibbs adsorption isotherm (5 points)

a)



Axis correct: 1/2 point

Initial decrease in gamma: 1 point

Constant gamma at $c > \text{CMC}$: 1 point

CMC indicated correctly: 1/2 point

- c) A molecule with a **longer aliphatic chain or bulkier monomer with larger r** (1 point). $\text{CMC} \approx e^{-\alpha} \approx e^{-\frac{1\pi r l}{k_B T}}$ (1 point).

Question 5: Micelles (5 points)

- a) $CMC \approx e^{-\frac{\Delta E}{k_B T}}$ (1/2 point) Excess free energy = $2.04 k_B T$ or $2 k_B T$. (1/2 point).
- b) $\alpha = \frac{v}{a_0 l_c}$
 $v = 0.2157 \text{ nm}^3$ (1 point), $l = 0.913 \text{ nm}$, $\alpha = 0.39$ (1/2 point) -> slightly elliptical (or cylindrical) micelle (1 point)
- c) maximum packing density = $1/0.6 \text{ nm}^2 = 1.667 \text{ nm}^2$. (1 point)
- d) SDS: **longer aliphatic chain** (1/2 point) -> smaller CMC (lower solubility in water) $CMC \approx e^{-\alpha} \approx e^{-\frac{1\pi r l}{k_B T}}$ (1/2 point)

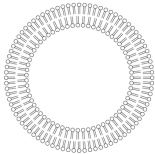
Question 6: Vesicles (5 points)

- a) **Micelle: Amphiphilic molecules** that are arranged into a sphere. Micelles are **monolayers** of self-assembled molecules that form a sphere (1/2 point).



(1/2 point)

Vesicle: Bilayer of amphiphilic molecules (1/2 point). Much larger than micelles.



(1/2 point)

- b) Micelles are formed if the ratio of the hydrophilic headgroup area : cross-section of the hydrophobic part, α , is $< 1/3$ whereas vesicles form if α is approximately unity. Hence, molecules that form micelles typically have a higher solubility and thus a **higher CMC (1/2 point)**. **The mean lifetime of a molecule is inversely proportional to the CMC (1/2 point)** -> the mean lifetime of molecules in vesicles is longer as their CMC is lower.
- c) For vesicles to form: $\alpha = 1$ (1/2 point)

$$R_g \text{ PDMS} = R_g \text{ PMOxa. (1/2 point)}$$

$$N = \frac{6R_g^2}{l^2} = 24 \text{ (1/2 point)}$$

$$M_w = 24 * 83 \text{ Da} = 1992 \text{ Da (1/2 point)}$$

Question 7: Polymers (5 points)

a) I) $N = (128241-2)/28 = 4580$. $a = 2 \cdot \sin(109.5/2) \cdot 0.154 \text{ nm} = 0.25 \text{ nm}$ (1/2 point)

II) $L_{cont} = Na$ (1/4 point) $= 1145 \text{ nm}$ (1/2 point)

III) $\langle r^2 \rangle_0 = Na^2 \left(\frac{1+\cos\theta}{1-\cos\theta} \right)$ (1/4 point) $r = 24 \text{ nm}$ (1/4 point)

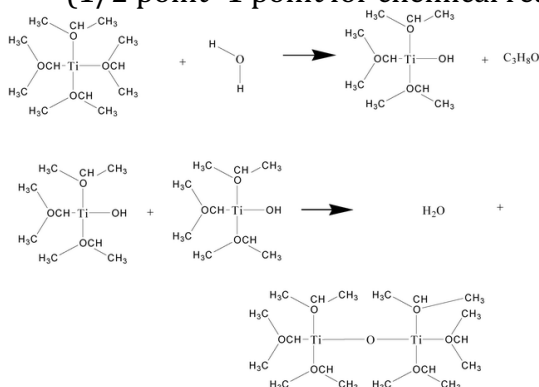
IV) $\sqrt{\langle R_g^2 \rangle} = \sqrt{\frac{\langle r^2 \rangle_0}{6}}$ (1/4 point) $R_g = 10 \text{ nm}$ (1/4 point)

b) $c_m = \frac{6^{1.5}}{l^3} N^{1-3\nu} \rightarrow N^{1-3\nu} = \frac{c_m l^3}{6^{1.5}} \rightarrow N = 10$ (1 point) $\rightarrow M_w = 830 \text{ Da}$ (1 point)

c) **Thermoplast** (1/2 point) $\rightarrow$ can be **heated, shaped, cooled down** (1/4 point) and it keeps its shape as it is **physically crosslinked** (1/4 point). However, this is a reversible process and it can be molten again.

Question 8: Gels (5 points)

a) 1. **Hydrolysis** (1/2 point+1 point for chemical reaction), 2. **Condensation** (1/2 point+1 point for chemical reaction), 3. Drying



Ref: Effect of hydrocarbon tail-groups of transition metal alkoxide based amphiphilic catalysts on transesterification, Gayan Nawaratna, Ronald Lacey and Sandun D. Fernando *

b) A sol transfers into a gel when a **percolating network forms** (1 point). Characterization: With rheology (1/2 point). When a percolating network forms **$G' > G''$, before $G'' > G'$** or sol-gel transition at **$G' = G''$** (1/2 point)

Question 9: Polymers at interfaces (5 points)

a) (2.5 points) (i) The **brush regime** is the regime where the **average interchain distance become less than 2 x the solution radius of gyration of the polymer**. Alternatively, one can also compare the **footprint** of a surface grafted polymer (1/grafting density) with the **projected 2D area** from the solution R_g (see the answer to question b).

b) (2.5 points) (i) Sample I: 100 nm^2 per chain (0.5 points); Sample II: 1.4 nm^2 per chain (0.5 points). R_g of 5 nm corresponds to a projected 2D

footprint of $(\pi r^2) = 79 \text{ nm}^2$ (0.5 points). Conclusion: in sample I the chains are in the mushroom regime and in Sample II in the brush regime (1 points).

Question 10: Mechanochemistry (5 points)

- a) (i) the middle of the chain is where the forces are highest (0.75 points);
(ii) incorporate a mechanophore at the desired position. (0.75 points)
- b) yes it does (0.5 points). At **pH 5** polylysine is **charged** and at **pH 12** **uncharged** (1 points). Due to **electrostatic repulsions** (0.5 points) the **forces** acting at pH 5 are larger (0.5 points) and thus the cleavage yield at a given point of time will be **higher** (0.5 points) and/or it **takes less time** to reach 100% cleavage. (0.5 points)

Question 11: Emulsions (5 points)

- a) Emulsions can be stabilized with **surfactants** (1/4 point) or **nanoparticles** (1/4 point).
 - I. **Surfactants: lower interfacial tension** (1/2 point) and therefore the interfacial energy $\Delta E = \gamma A$. They have a **high mobility** and **quickly adsorb** at the liquid-liquid interface. (1/4 point if one of them is mentioned) However, their adsorption is reversible $\rightarrow$ drops can **coalesce** if the system is not optimized (1/4 point).
 - II. **Nanoparticles:** Reduce the **interfacial area** (1/2 point) and therefore the interfacial energy. If adsorbed at the liquid-liquid interface, they are strongly bound. It typically takes more than $100 k_B T$ to remove them $\rightarrow$ for practical purposes irreversibly bound $\rightarrow$ **more stable dispersion** (1/4 point). **Slower adsorption** (1/4 point).
- b) Sauce hollandaise: **oil in water emulsion** (1/2 point): surfactant with **HLB value between 10 and 20** (1/2 point). Surfactant must be food grade: **nonionic surfactant** (1/2 point). Hydrophobic chain: aliphatic, hydrophilic for example sugar e.g. Span 80.
- c) $\Delta E = \gamma \pi r^2 \rightarrow 1.6 \times 10^{-16} \text{ J}$ (1/4 point) $\rightarrow 3820 k_B T$ (1/4 point). Particles are for practical purposes irreversibly adsorbed at the liquid-air interface $\rightarrow$ the foam is very stable, foam does not coalesce. (1/2 point).

Question 12: Particles (5 points)

Au nanoparticles:

- a) Thiols (1 point)
- b) $N = \frac{l_0}{\frac{5}{3}\Gamma^3} = 37 \text{ or } 38$ (1/2 point) $\rightarrow M_w = 1636 \text{ Da or } 1680 \text{ Da}$ (1/2 point)
- c) PEG then acts as a **depletant** and particles agglomerate because of the **attractive depletion forces**. (1 point)
- d) DLS (1/2 point): measure the **intensity of the scattered light at time 0 and time Δt** (1/4 point). The **correlation** (1/4 point) of the intensity

pattern is calculated and plotted as a function of Δt . This correlation function is fitted to extract a **diffusion coefficient (1/4 point)**. Using the **Stokes Einstein equation (1/4 point)**, this allows calculation of the hydrodynamic radius (diameter). The scattering intensity scales with r^6 -> you almost only see the **larger aggregates** and you overestimate the size of the particles (1/2 point)