

Adsorption at Interfaces

Lesson 7

MSE 304

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Key Topics in the Previous Class

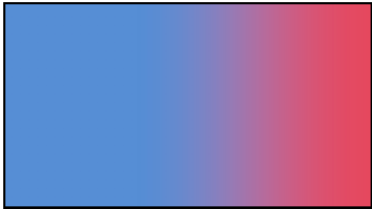
Reading for this Class

Challenges in Defining an Interface

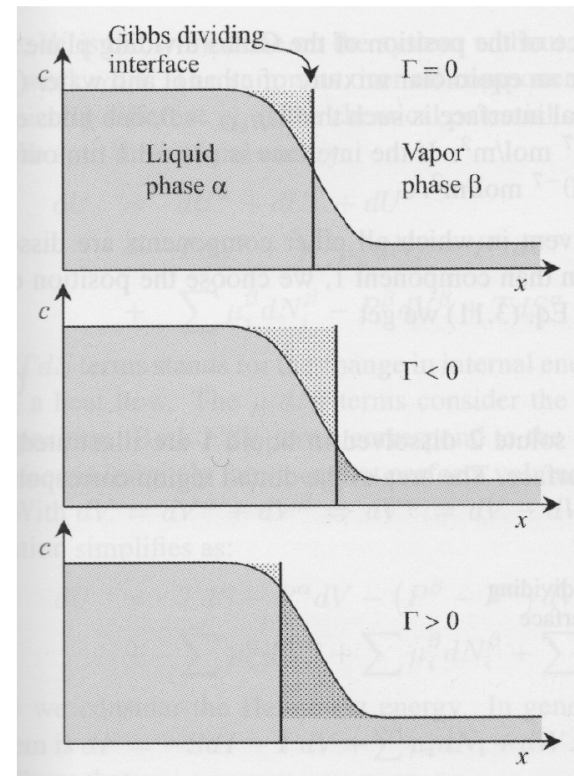
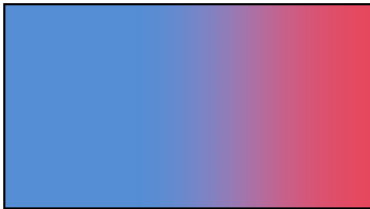
Challenges in Defining an Interface



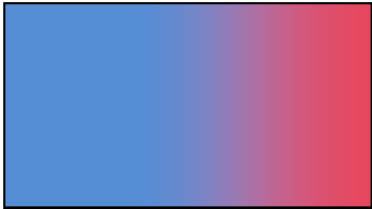
Gibbs Definition



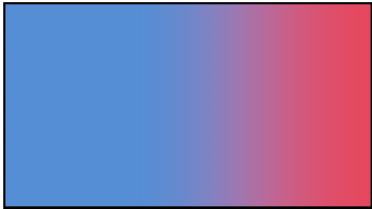
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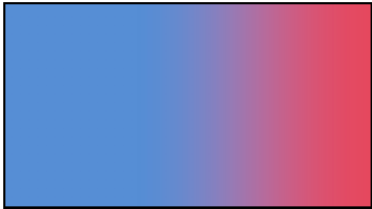
Gibbs Isotherm



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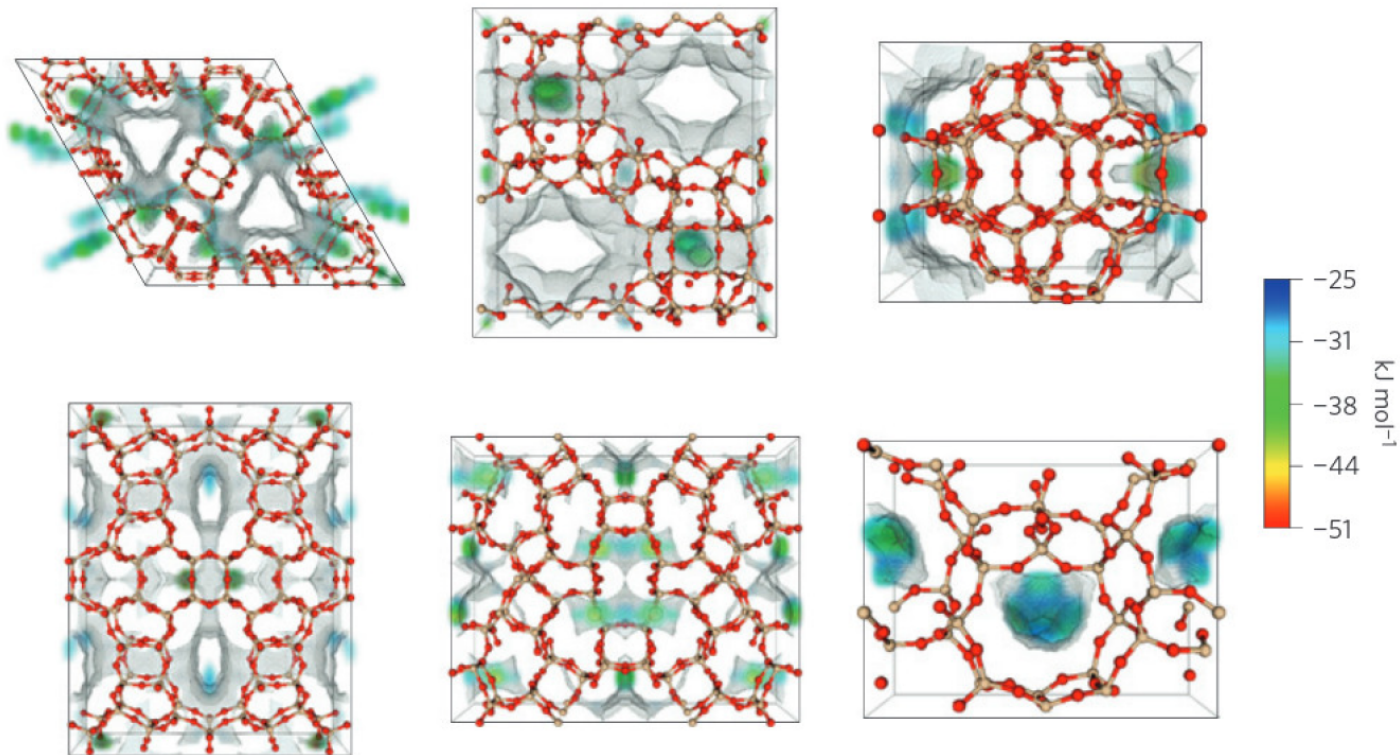


Gibbs Isotherm



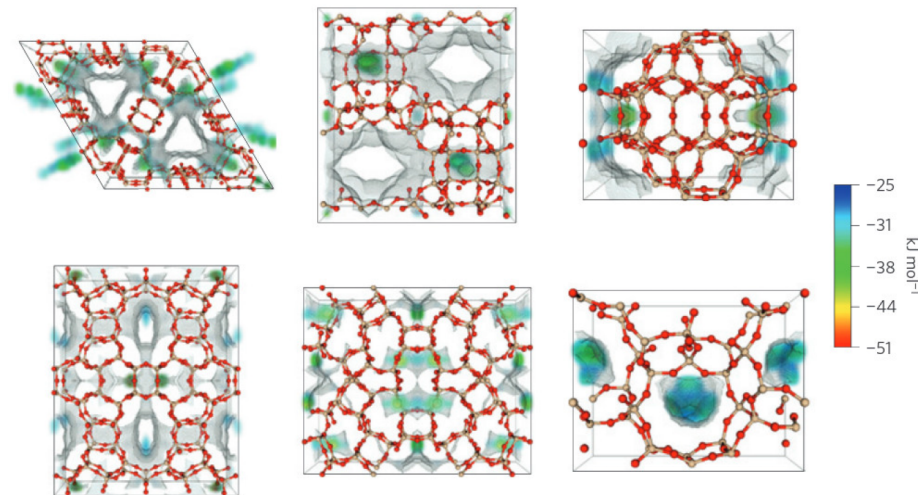
Adsorption at Interfaces

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Adsorption at Interfaces

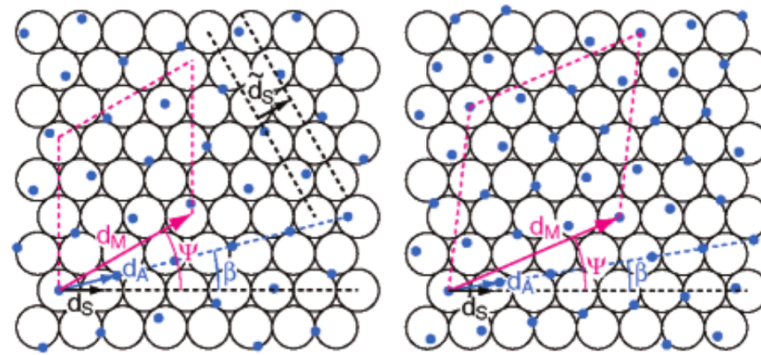
- Adsorption is crucial for catalysis, and storage of gases!
- Phenomenology of adsorption
- Langmuir adsorption interface: one species and competitive
- Different kinds of adsorption isotherms: FFG (correlated), BET (multilayer)



Chemisorption and Physisorption

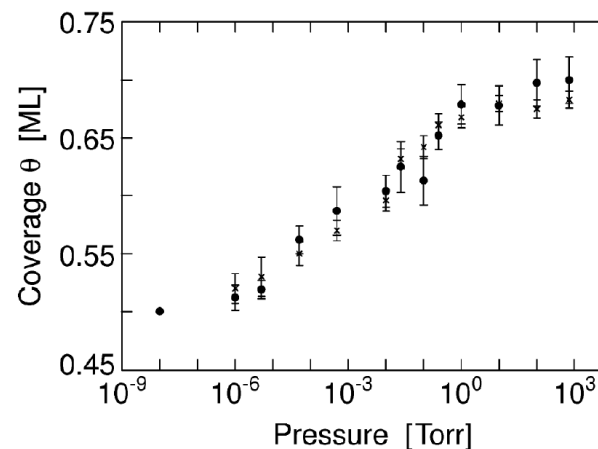
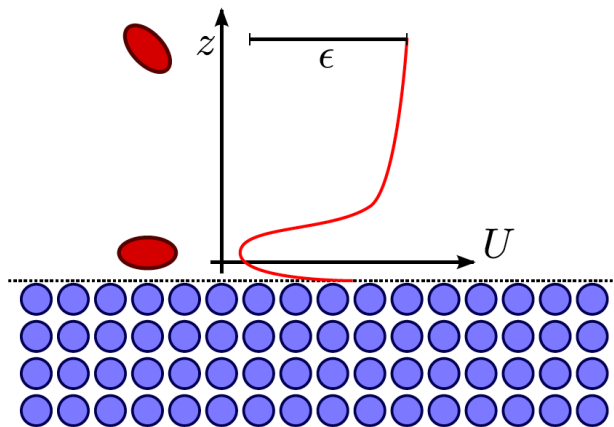
- Real surfaces are often covered in molecules, often with complex/regular arrangements
 - Adsorption lowers the surface energy
- Conventional classification as a function of the adsorption enthalpy
 - **physisorption**: reversible, weak binding (< 40 kcal/mol), mobile species
 - **chemisorption**: irreversible, strong binding (> 40 kcal/mol), immobile species

Monolayers



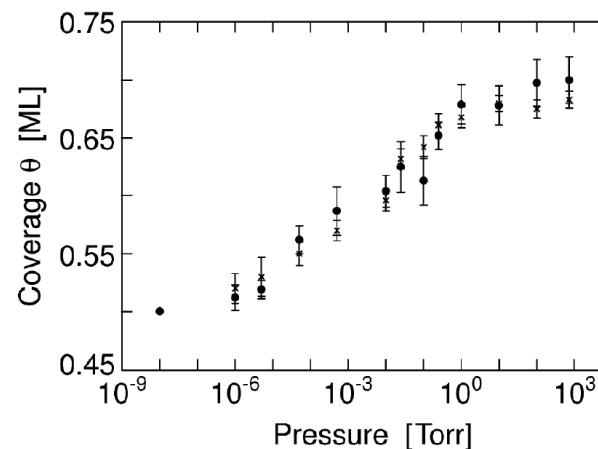
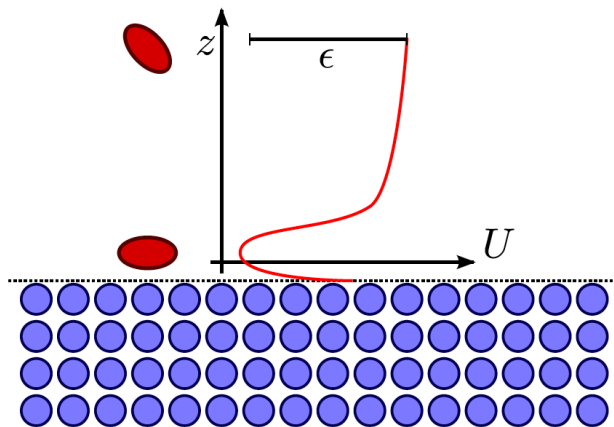
Key Definitions in Adsorption

- An adsorbate molecule often resides in specific adsorption sites (not necessarily one per surface unit cell).
- **Coverage** θ measures the number of occupied sites n relative to the maximum possible number N
- Adsorption energy ϵ : stabilization relative to the gas-phase molecule.
Residence time: $\tau \sim \tau_0 e^{\epsilon/k_B T}$
- Experimental measure: **adsorption isotherm**



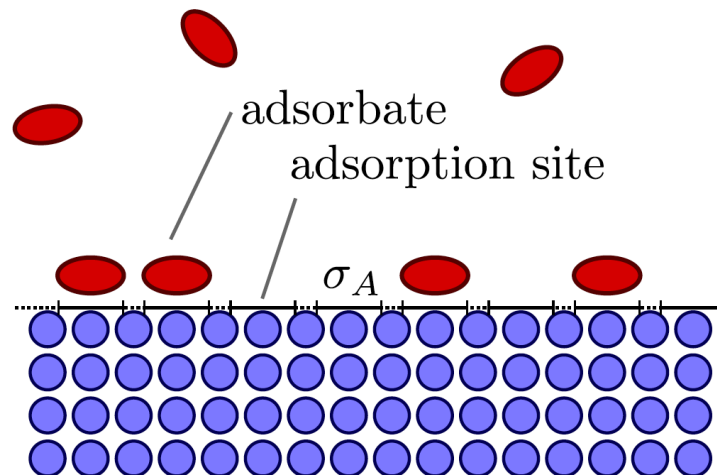
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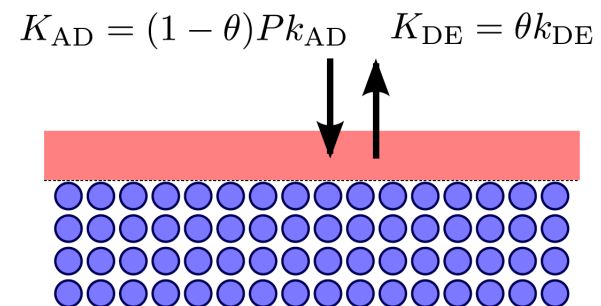
Langmuir Isotherm – Initial Hypotheses

- A simple model for adsorption that leads to the **Langmuir adsorption isotherm**:
 - The surface is covered by *equivalent* adsorption sites, with area σ_A
 - The adsorption energy ϵ is *independent* on the site and on the occupation of nearby adsorption sites
 - The *sticking coefficient* (probability on binding upon a collision with the surface) on an empty site is one



Langmuir Isotherm – Equilibrium Derivation

- Equilibrium between adsorption rate K_{AD} and desorption rate K_{DE}
 - **Desorption rate** proportional to the fraction of occupied sites and the rate for one site
 - **Adsorption rate** proportional to the fraction of empty sites and the collision rate (assuming *sticking coefficient* is one)

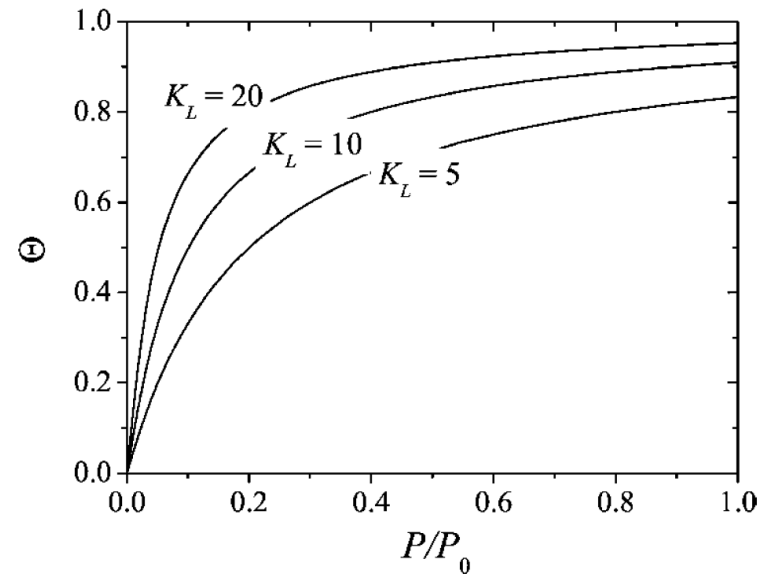


Langmuir Isotherm

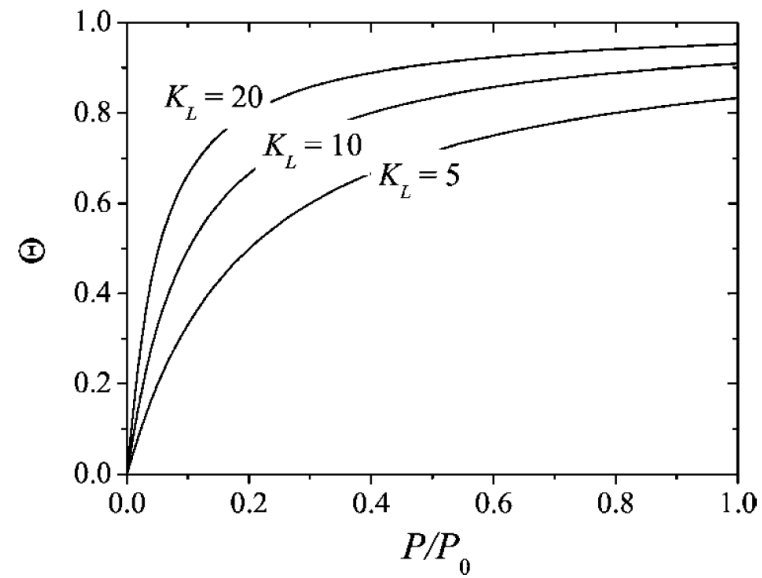
$$\theta = \frac{Pk_L}{Pk_L + 1},$$

$$\boxed{\frac{\theta}{1 - \theta} = \frac{P}{P_0}} = k_L P = \frac{k_{AD}}{k_{DE}} P,$$

$$k_L = \frac{1}{P_0} = \frac{k_{AD}}{k_{DE}} = \frac{\sigma A T_0}{\sqrt{2\pi m k_B T}} e^{\epsilon/k_B T}$$



Langmuir Isotherm - Considerations



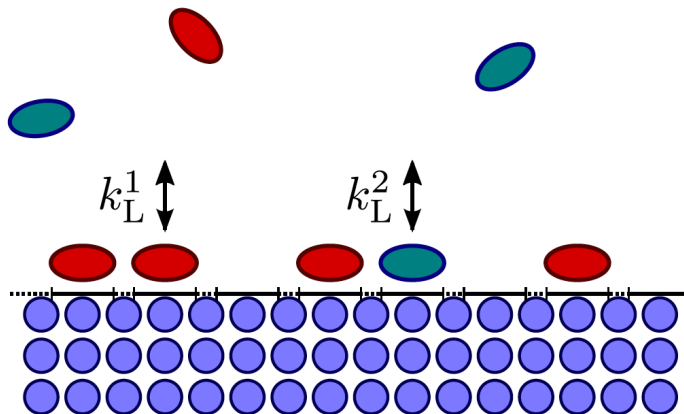
Langmuir Isotherm – Competitive Adsorption

- What if we have multiple molecules in the gas phase? $\theta = \sum_i \theta_i$
- At equilibrium one must have mass balance for each specie separately

$$\theta_i k_{\text{DE}}^i = K_{\text{DE}}^i = K_{\text{AD}}^i = (1 - \theta) k_{\text{AD}}^i P_i$$

$$\frac{\theta}{1 - \theta} = \sum_i k_{\text{L}}^i P_i \rightarrow \theta = \frac{\sum_i k_{\text{L}}^i P_i}{1 + \sum_i k_{\text{L}}^i P_i} \rightarrow 1 - \theta = \frac{1}{1 + \sum_i k_{\text{L}}^i P_i}$$

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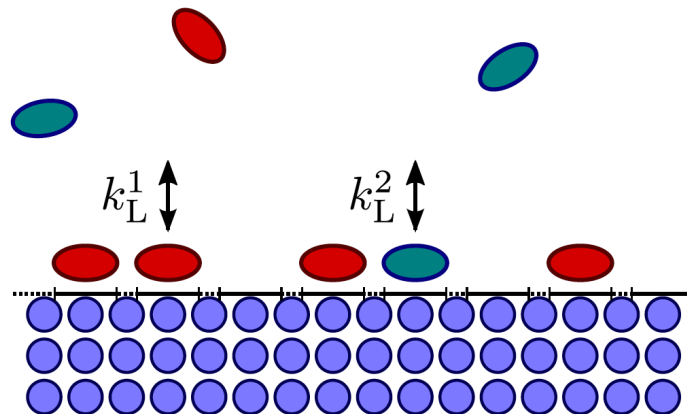
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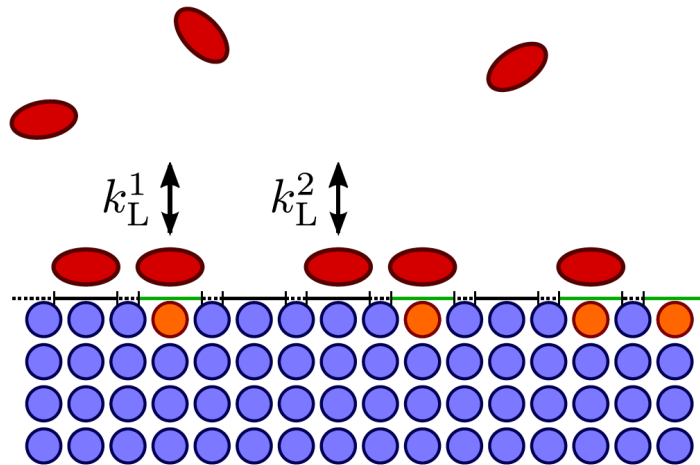


Langmuir Isotherm – Competitive Adsorption

- Multiple adsorption sites, with fraction x_i and different adsorption energies ϵ_i
- Can treat as independent adsorption problems, but $\theta = \sum_i x_i \theta_i$

$$\theta_i x_i k_{\text{DE}}^i = K_{\text{DE}}^i = K_{\text{AD}}^i = x_i (1 - \theta_i) k_{\text{AD}}^i P$$

$$\theta_i = \frac{k_{\text{L}}^i P}{1 + k_{\text{L}}^i P}, \quad \theta = \sum_i \frac{x_i k_{\text{L}}^i P}{1 + k_{\text{L}}^i P}$$

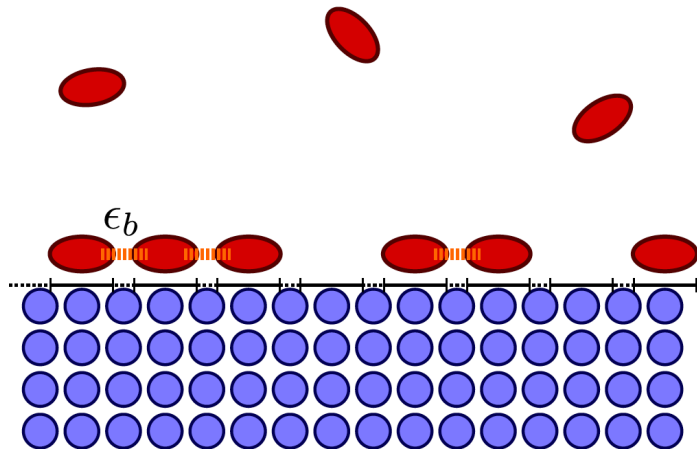


Collaborative Adsorption – FFG Isotherm

- Consider the possibility of bonding between molecules.
- The number of bonds per molecule at full coverage is n , and the energy per bond ϵ_b
- The probability of one neighbor being occupied is θ , so the mean energy of an adsorbed molecule becomes $\epsilon \leftarrow \epsilon + n\theta\epsilon_b$
- Isotherm is given by the (physical) solutions to the implicit equation

$$\frac{\theta}{1 - \theta} = k_L e^{\frac{n\epsilon_b\theta}{k_B T}} P$$

$$k_L = \frac{1}{P_0} = \frac{k_{AD}}{k_{DE}} = \frac{\sigma_A T_0}{\sqrt{2\pi m k_B T}} e^{\epsilon/k_B T}$$



Collaborative Adsorption – FFG Isotherm

$$\frac{\theta}{1 - \theta} = k_L e^{\frac{n\epsilon_b \theta}{k_B T}} P$$

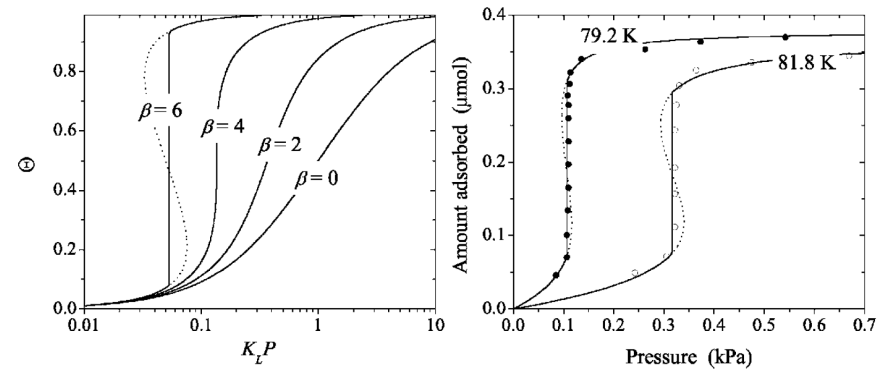
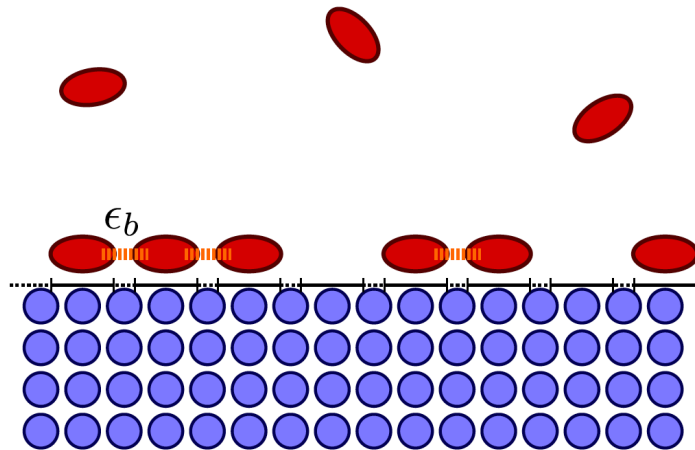
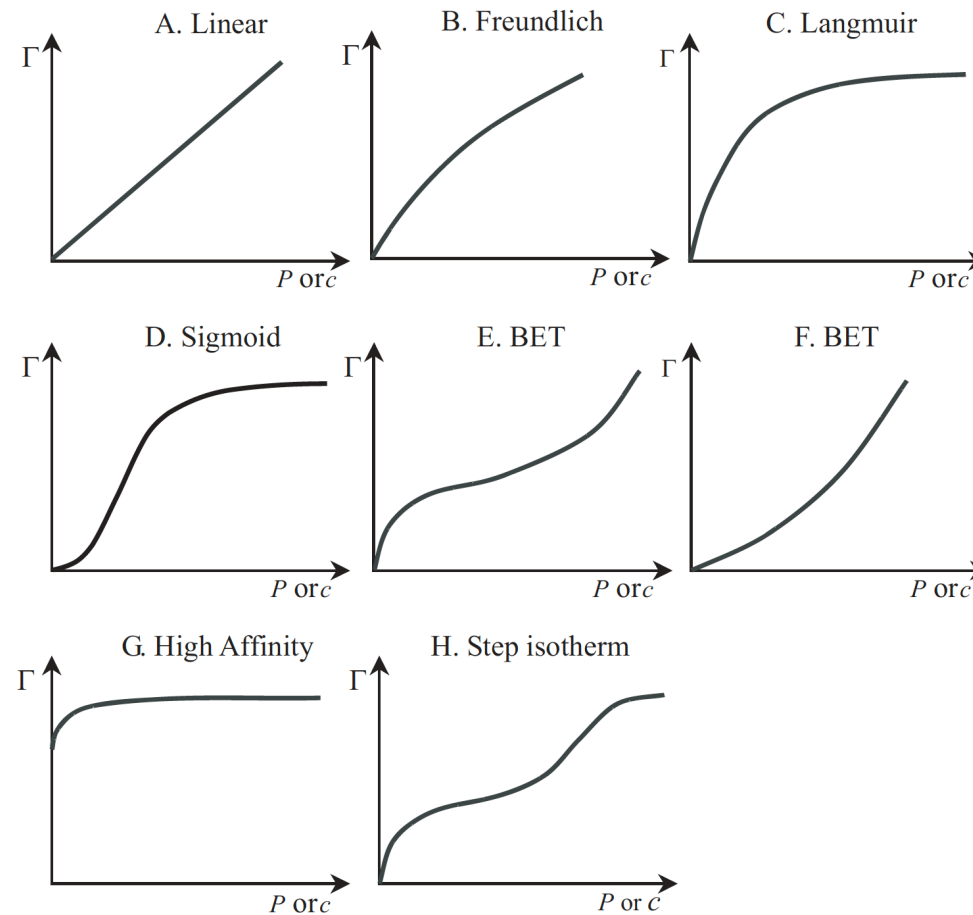


Figure 9.7: Left: Frumkin–Fowler–Guggenheim (FFG) adsorption isotherms (coverage θ versus the pressure in units of K_L^{-1}). The curves were calculated using Eq. (9.35) with $\beta = 0, 2, 4, 6$. For $\beta = 6$ the physically correct adsorption curve is plotted as a continuous curve while the one calculated with Eq. (9.35) is plotted as a dotted curve. Right: Adsorption isotherms for krypton adsorbing to the (0001) plane of graphite at two different temperatures. The dotted curves were fitted using Eq. (9.35) with $\beta = 4.5$. Experimental results were taken from Ref. [377].

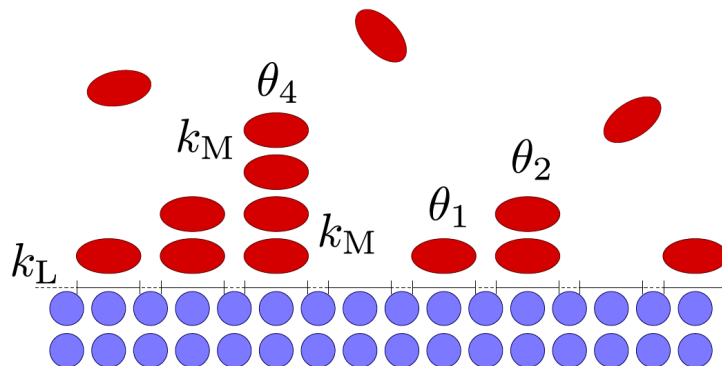
Isotherms



BET

- Random adsorption on multiple layers. Langmuir constant for the first layer is k_L , other layers bind on the previous with $k_M = k_L e^{(\epsilon_M - \epsilon_1)/k_B T}$
- One must equate ad/desorption rate from the sites covered by i layers
- The sums of θ_i 's are geometric series.
- Total coverage (number of molecules per number of *surface* sites)

$$\theta_1 = k_L P \left(1 - \sum_i \theta_i \right), \quad \theta_i = \theta_{i-1} k_M P = \theta_1 [k_M P]^{i-1}$$



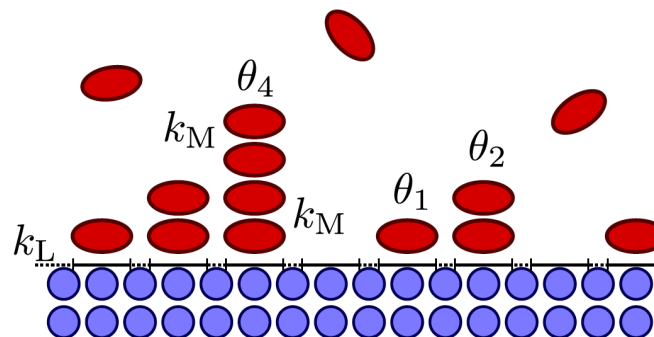
BET - Multilayers

$$\sum_{i=1}^{\infty} [k_M P]^{i-1} = \frac{1}{1 - k_M P}, \quad \sum_{i=1}^{\infty} i [k_M P]^{i-1} = \frac{1}{(1 - k_M P)^2}$$

$$\theta = \theta_1 \sum_{i=1}^{\infty} i [k_M P]^{i-1} = \theta_1 \frac{1}{(1 - k_M P)^2} = \frac{k_L P (1 - k_M P)}{1 + k_L P - k_M P} \frac{1}{(1 - k_M P)^2}$$

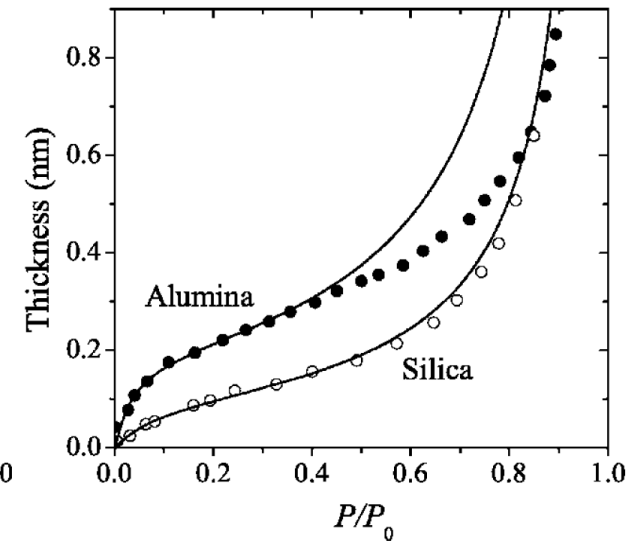
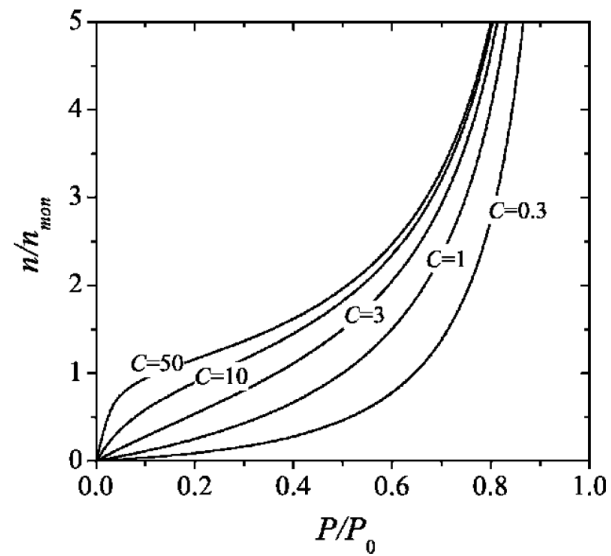
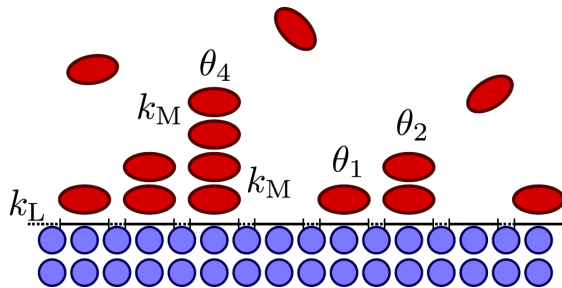
$$\theta \approx \frac{1}{(1 - x_B)} \frac{x_B c_B}{1 + x_B (c_B - 1)}, \quad x_B = k_M P, \quad c_B = k_L / k_M$$

$$\theta = \frac{k_L P}{1 + k_L P - k_M P} \frac{1}{1 - k_M P}$$



BET - Multilayers

$$\theta = \frac{k_L P}{1 + k_L P - k_M P} \frac{1}{1 - k_M P}$$



Conclusions
