

Non-linear frequency conversion I

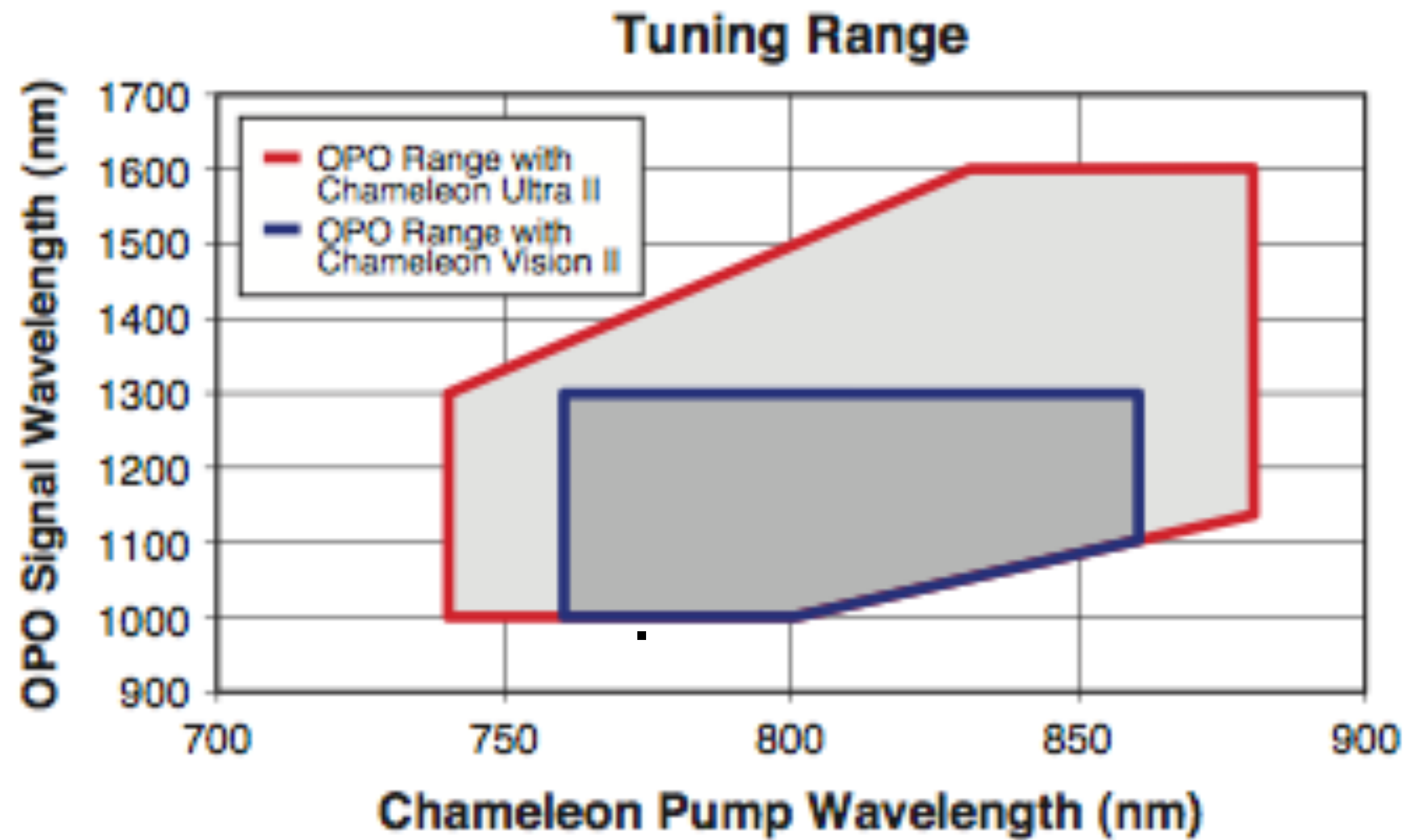
Lasers: theory and applications, lecture 12.1

Christophe Moser

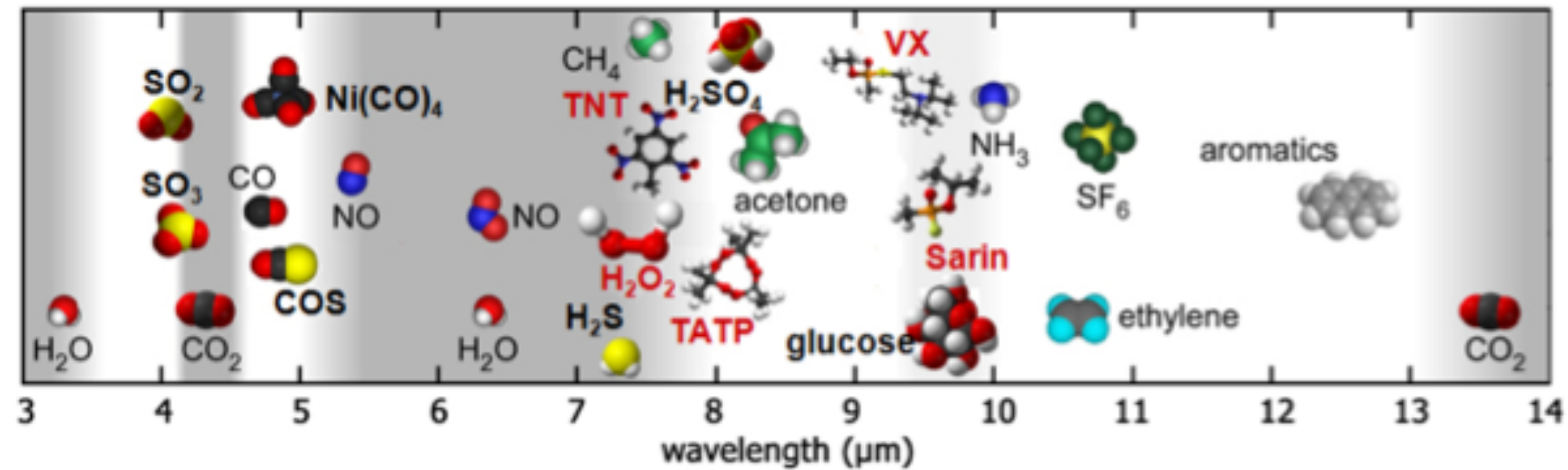
Non-linear frequency conversion I

- Motivation
- Non-linear wave equation

Motivation

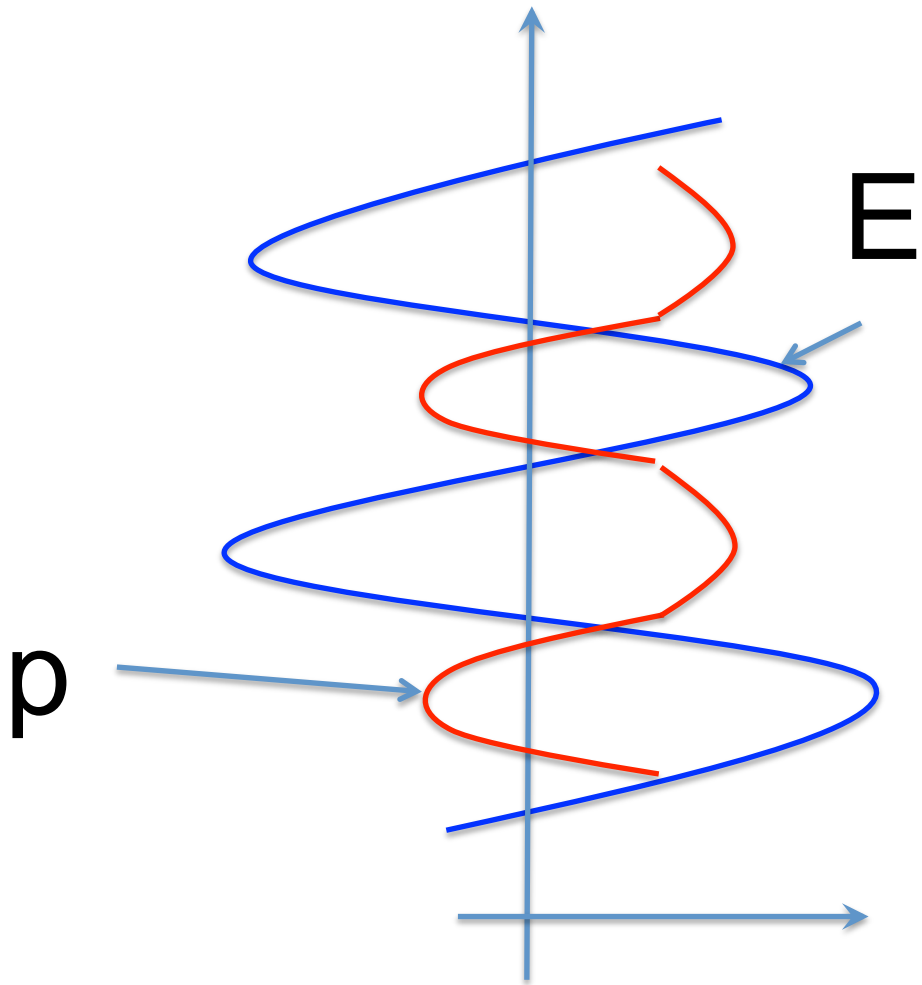
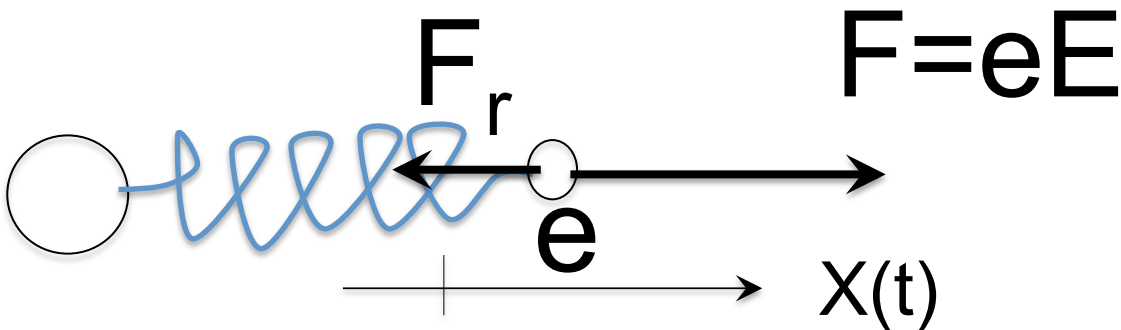


Motivation

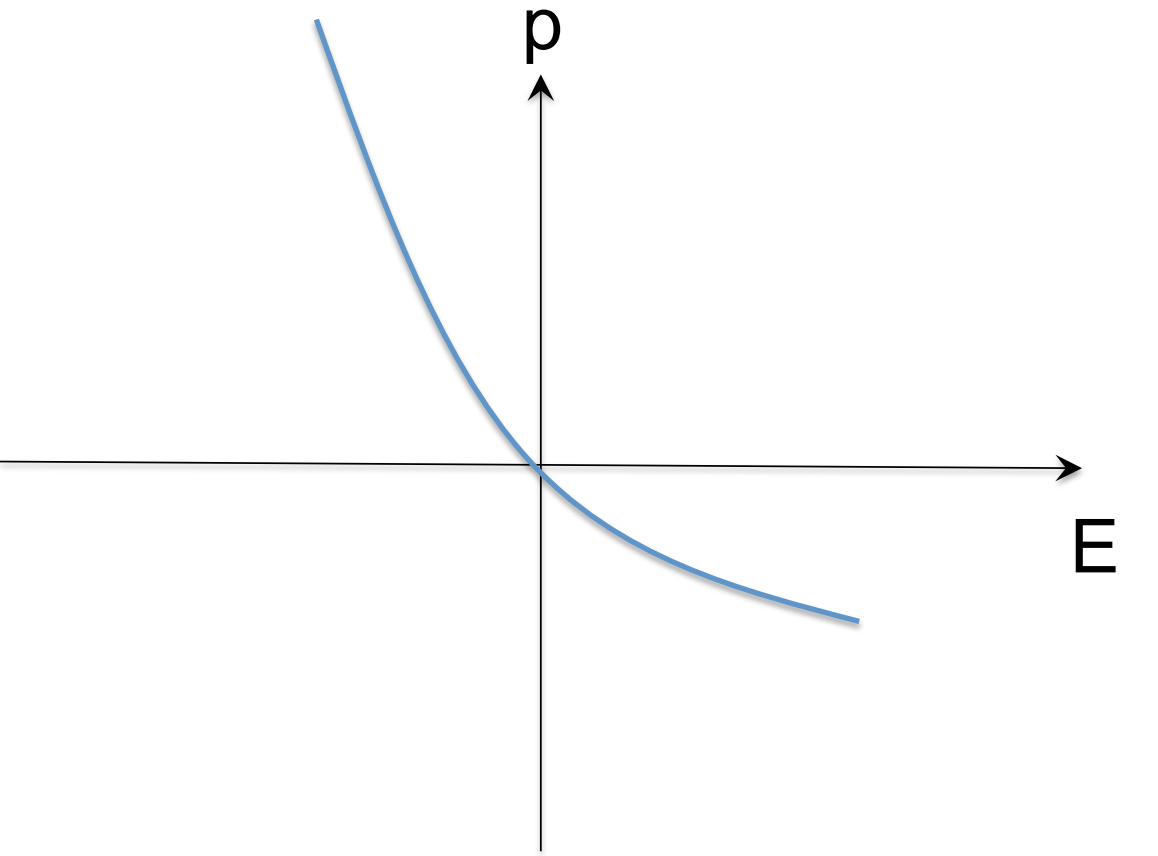
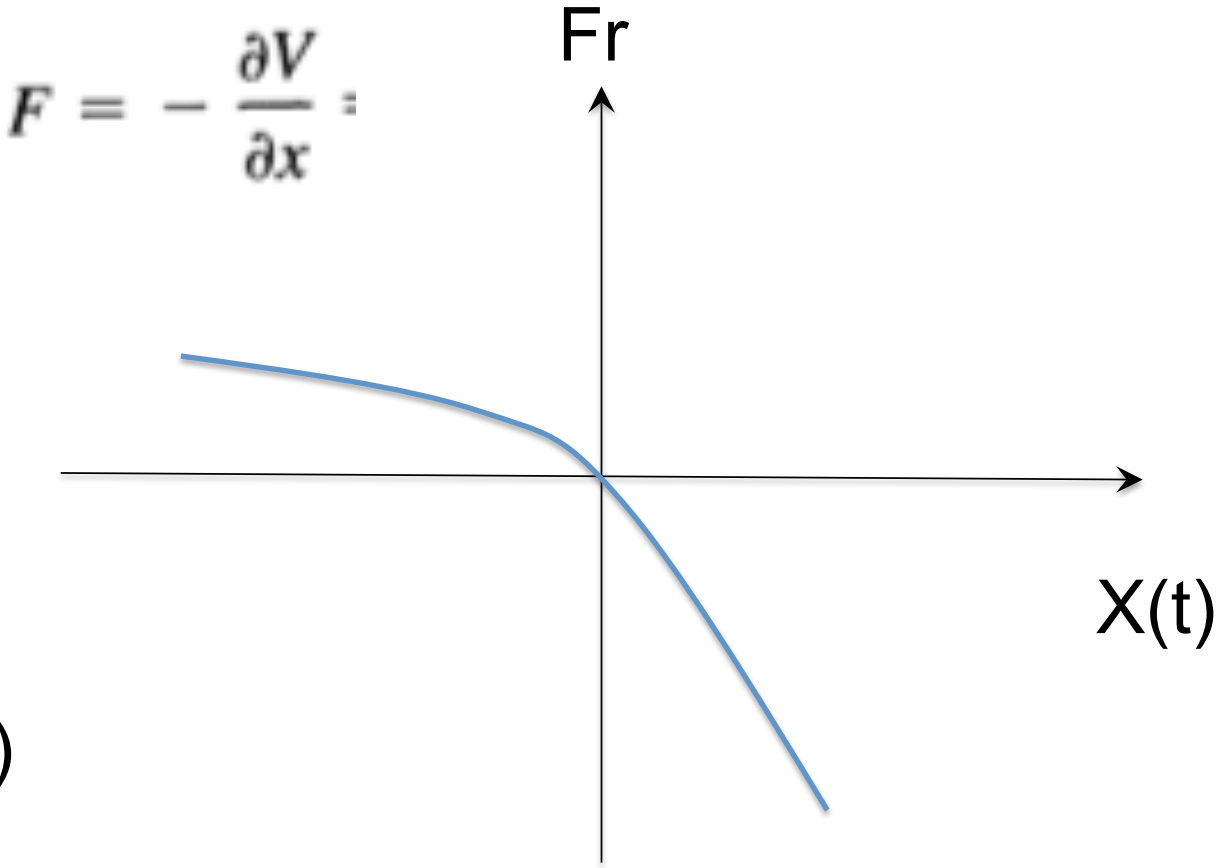
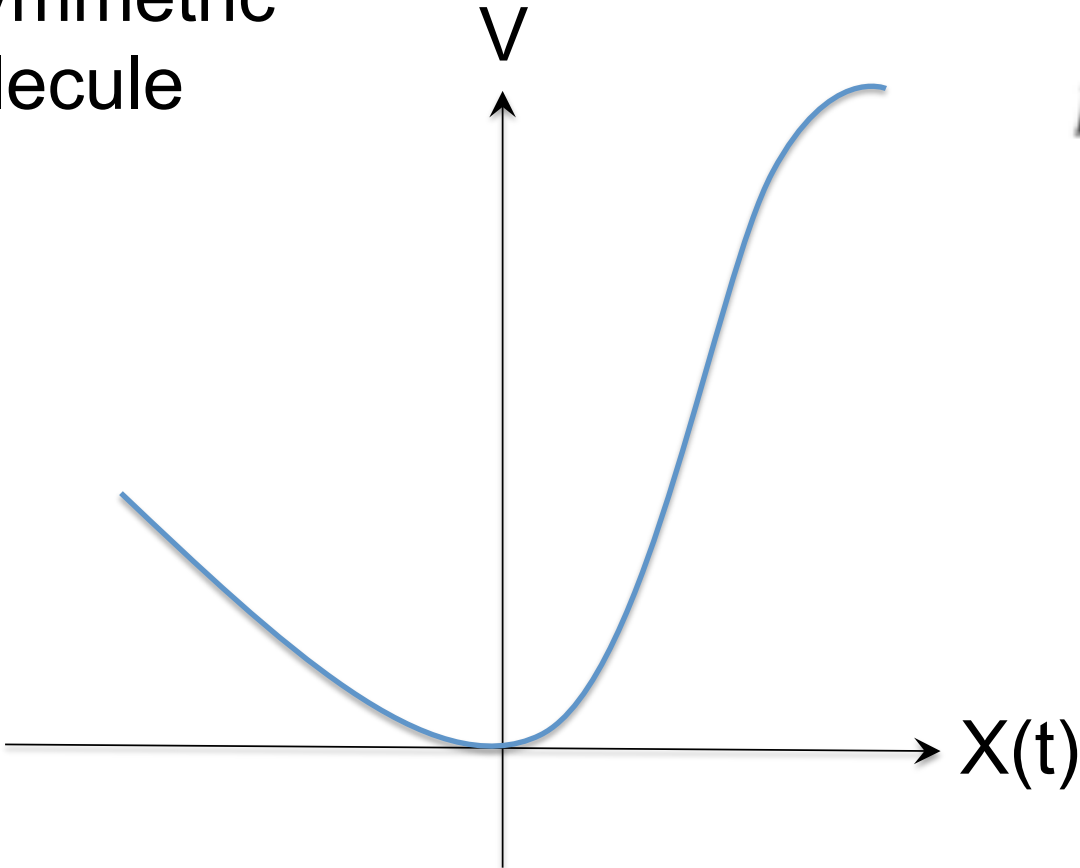


Physical origin

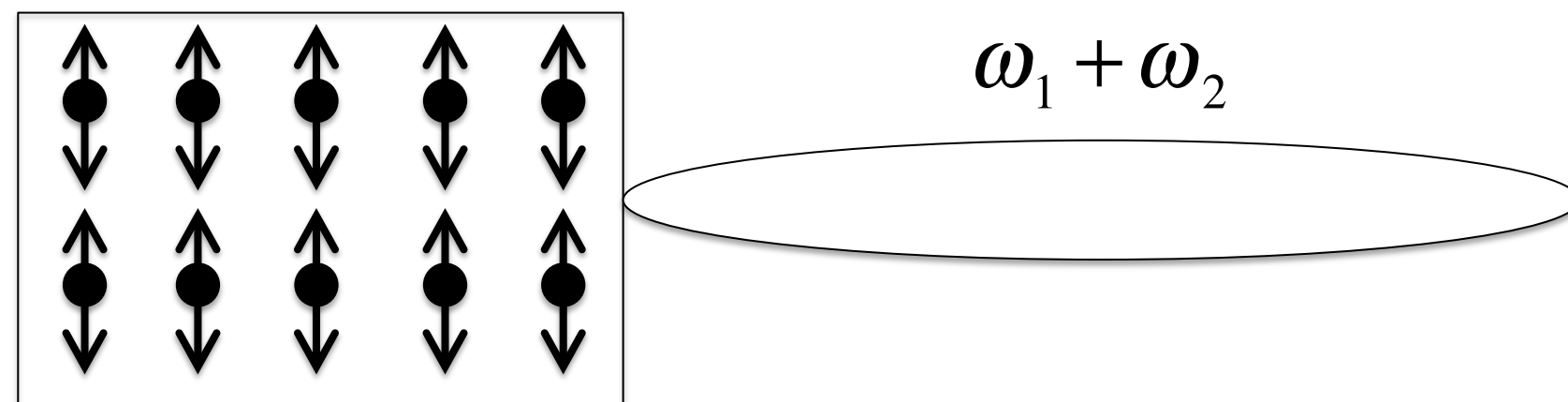
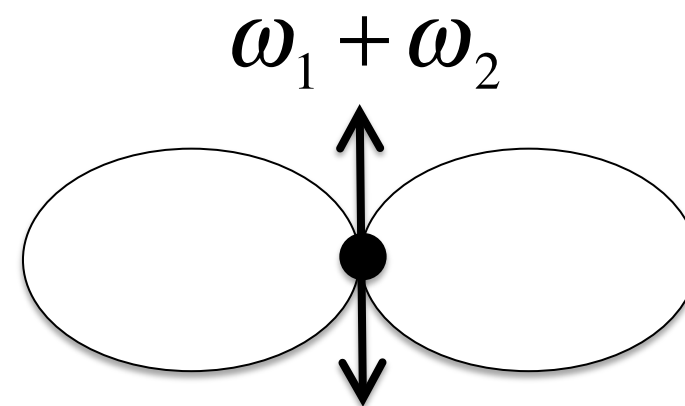
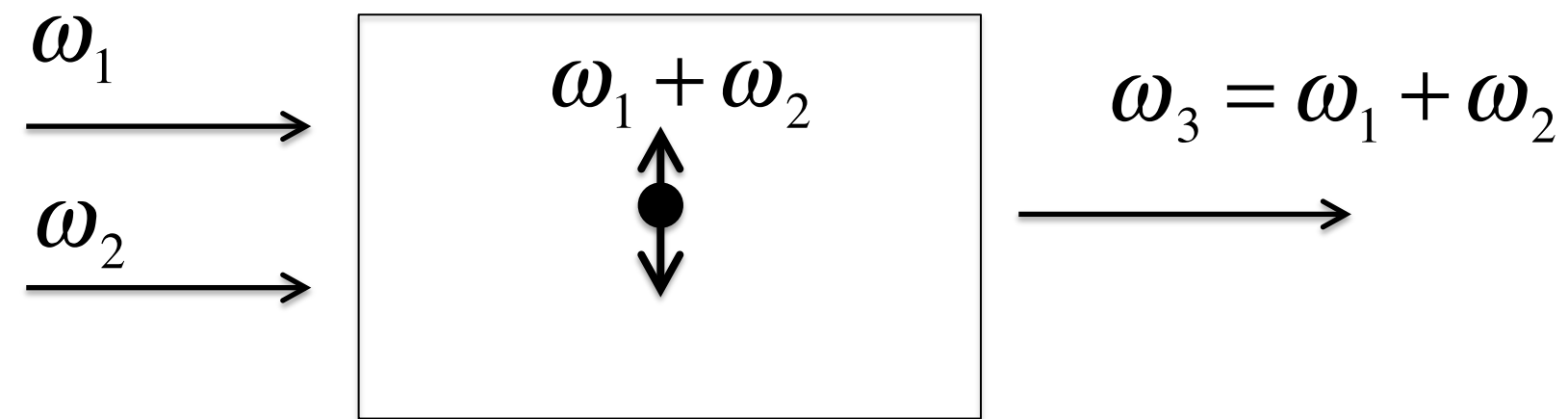
$$p(t) = -Nex(t)$$



Asymmetric
Molecule



Wave equation



Polarizability $\mathbf{P}$:
$$\nabla^2 \vec{E} - \frac{1}{c^2} \frac{\partial^2 \vec{E}}{\partial t^2} = \frac{1}{\epsilon_o c^2} \cdot \frac{\partial^2 \vec{P}}{\partial t^2}$$

$$\mathbf{P} = \epsilon_0 \left(\underbrace{\chi^{(1)} \cdot \mathbf{E}}_{\vec{P}^L} + \underbrace{\chi^{(2)} : \mathbf{E}\mathbf{E} + \chi^{(3)} : \mathbf{E}\mathbf{E}\mathbf{E} + \dots}_{\vec{P}^{NL}} \right),$$

$$\nabla^2 \vec{E} - \frac{1}{c^2} \frac{\partial^2 \vec{E}}{\partial t^2} - \frac{\epsilon_o \chi^{(1)}}{\epsilon_o c^2} \frac{\partial^2 \vec{E}}{\partial t^2} = \frac{1}{\epsilon_o c^2} \cdot \frac{\partial^2 \vec{P}^{NL}}{\partial t^2}$$

$$= \epsilon^{(1)} = n^2$$

$$\nabla^2 \vec{E} - \frac{1 + \chi}{c^2} \frac{\partial^2 \vec{E}}{\partial t^2} = \frac{1}{\epsilon_o c^2} \cdot \frac{\partial^2 \vec{P}^{NL}}{\partial t^2}$$

n and χ depend on optical frequency