

The Energy Supply System

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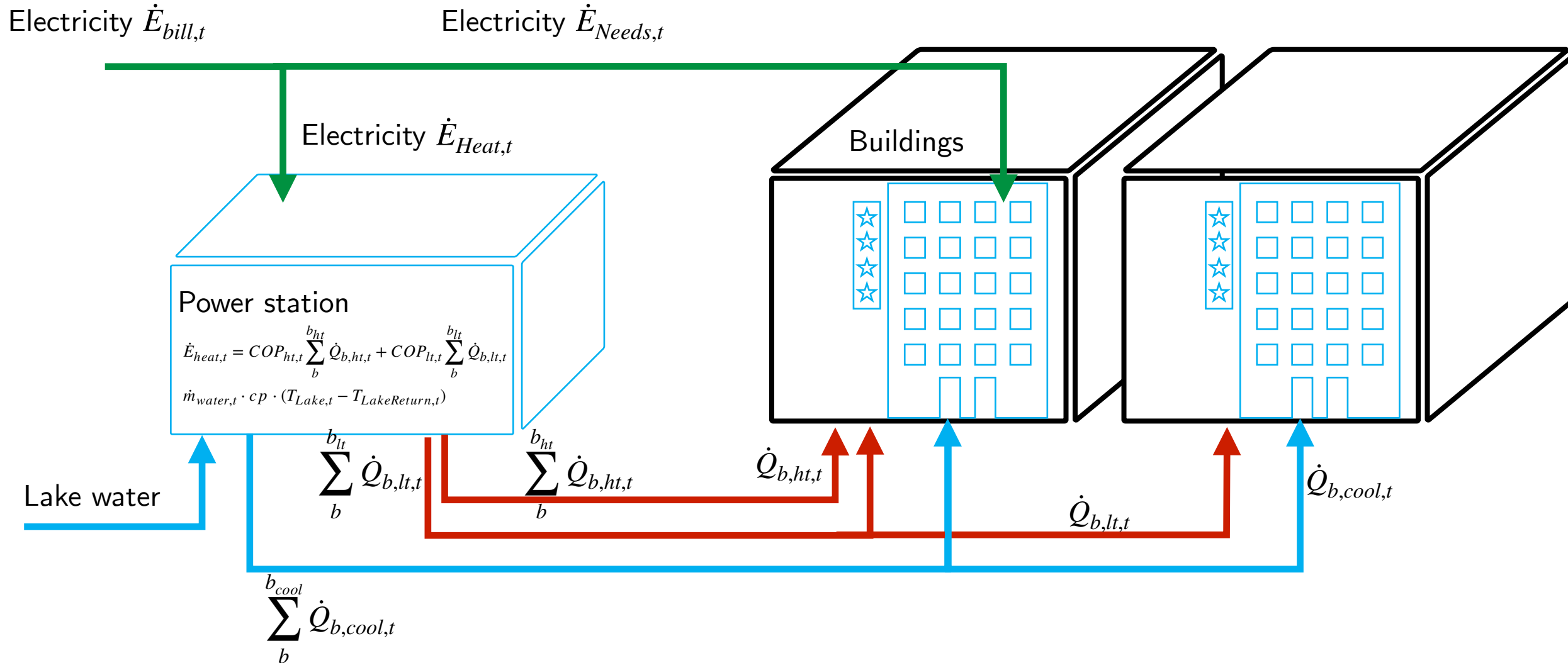
Buildings stock

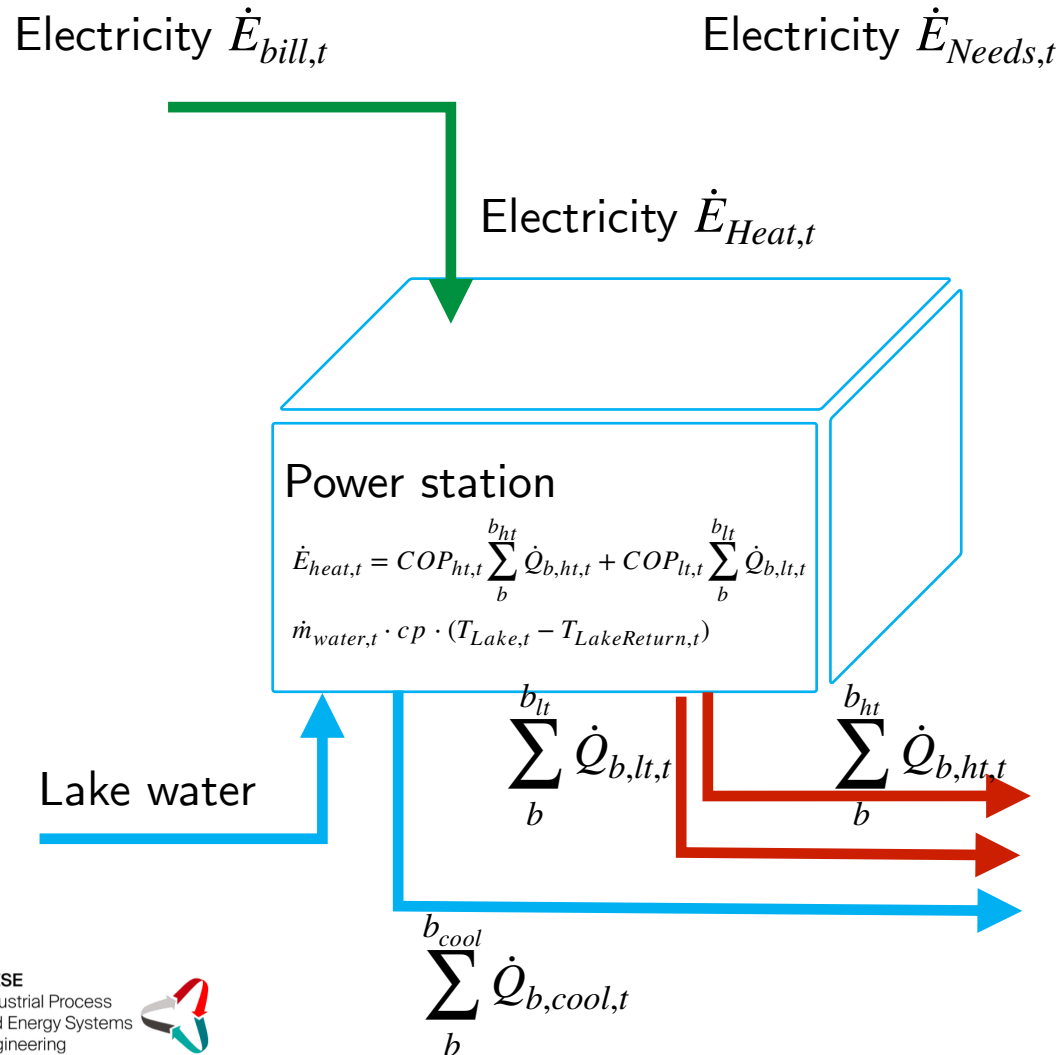


Measures

Table 1.1: EPFL Buildings

Building	Construction period ^a	Heated surface A_{th} [m ²]	Annual heat demand Q_{th} [kWh]	Annual electricity demand Q_{el} [kWh]
BC	2	17480	418,491	1,603,596
CO	2	11901	477,008	943,653
BP	2	10442	457,861	691,031
BS	2	10267	509,183	350,860
TCV	2	6095	318,209	2,067,675





- For each distribution system d (e.g. ht)

- Demand : $\dot{Q}_{d,t} = \sum_b^{n_b} \dot{Q}_{b,d,t} \quad \forall t \in lifetime$

- For each unit u (e.g. heat pump)

- Supply by unit u : $\sum_{u=1}^{n_u} \dot{Q}_{u,d,t} = \dot{Q}_{d,t} \quad \forall t \in lifetime$

- and $\dot{Q}_{u,t} = \sum_d^{n_d} \dot{Q}_{u,d,t}$

- Cost of the supply

- Size of the conversion equipment :

$$\sum_{u=1}^{n_u} \max_{t \in lifetime} (\dot{Q}_{u,d,t}) = \max_{t \in lifetime} (\dot{Q}_{d,t})$$

- $\dot{Q}_{u,max} = \max_{t \in lifetime} (\dot{Q}_{u,t})$

- Buy the resources : $\sum_{r=1}^{n_{res}} \sum_u^{n_u} \left(\int_{t_0}^{lifetime} c_{r,t} \cdot m_{r,u,t} \cdot \dot{Q}_{u,t} \cdot dt \right)$

$$\sum_{r=1}^{n_{res}} \sum_u^{n_u} \left(\int_{t_0}^{lifetime} c_{r,t} \cdot m_{r,u,t} \cdot \dot{Q}_{u,t} \cdot dt \right) \quad [CHF/lifetime]$$

- $c_{r,t}$ $[CHF/unit_r]$ cost of one unit of resource r at time t
 - e.g. kg of water, kg of fuel, kJ of fuel or kWh of electricity
 - $c_{r,t} \leq 0$ for products (e.g. electricity production)
- $m_{r,u,t}$ $[unit_r/kJ_{th}]$ unit of resource r used to deliver one $[kJ_{th}]$ of heat by unit u at time t
- $\dot{Q}_{u,t}$ $[kW]$ heat delivered by unit u at time t
- $lifetime$ $[s]$ expected lifetime of the project

- Operating EXpenditure (we assume a typical year of operation) :

$$\text{Cost of resources} \sum_{r=1}^{n_{res}} \sum_u^{n_u} \left(\int_{t_0}^{year} c_{r,t} \cdot m_{r,u,t} \cdot \dot{Q}_{u,t} \cdot dt \right) \quad [CHF/year]$$

+ Maintenance [CHF/year]

+ Men Power [CHF/year]

+ Taxes [CHF/year] :

fixed : e.g. based on installed power

$$\text{proportional : } \sum_{r=1}^{n_{res}} \sum_u^{n_u} \left(\int_{t_0}^{year} t_{r,t} \cdot m_{r,u,t} \cdot \dot{Q}_{u,t} \cdot dt \right) \quad [CHF/year]$$

with $t_{r,t}$ [CHF/unit_r] tax per unit of r

$$\text{e.g. } t_{r,t} = \tau_{CO_2} [CHF/kg_{CO_2}] \cdot m_{CO_2,r} [kg_{CO_2}/unit_r]$$

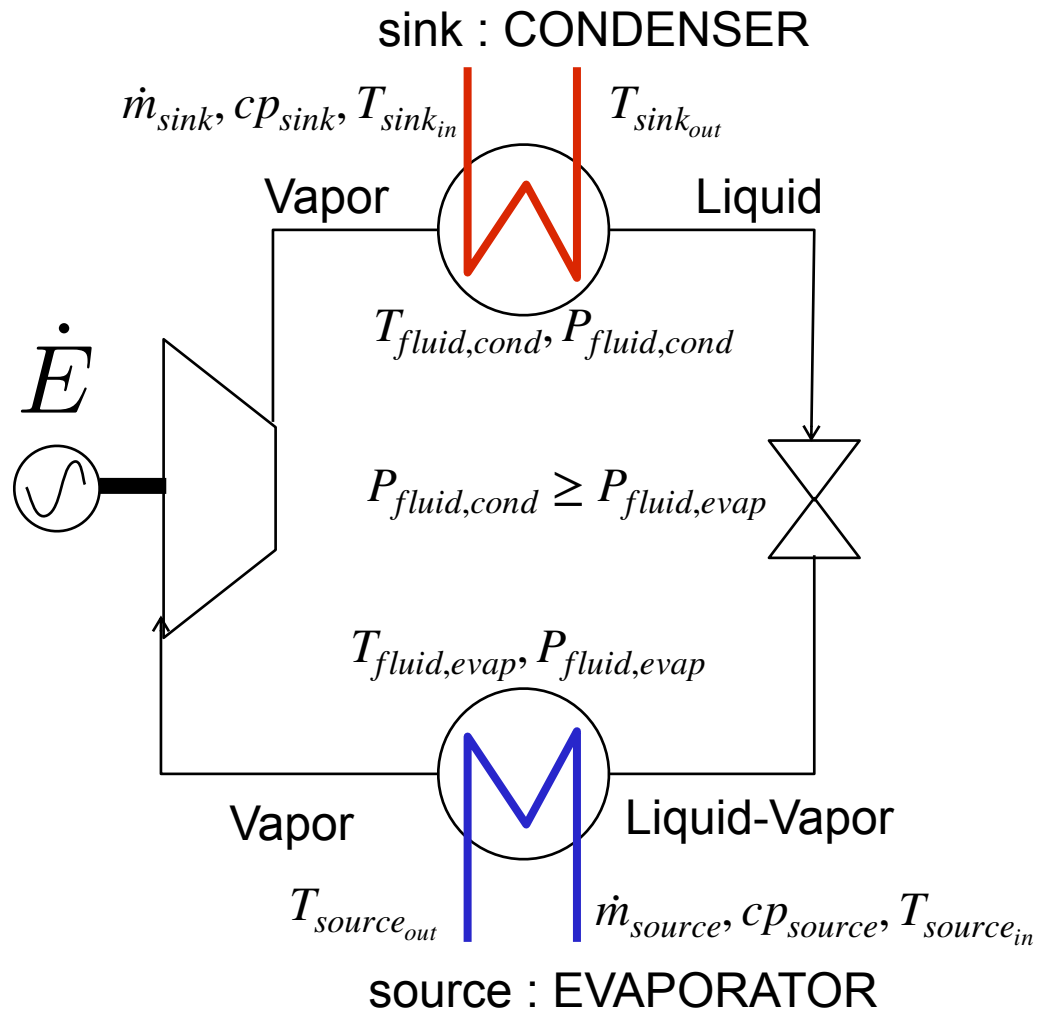
- Assumptions

- Thermal efficiency : $\eta_{th,u} = \frac{\dot{Q}_{th,u}}{\dot{m}_{r,u}}$ [kJ_{th}/kJ_r]

- Electrical efficiency : $\eta_{e,u} = \frac{\dot{E}_u}{\dot{m}_{r,u}}$ [kJ_e/kJ_r]

- $m_{r,u,t} = \frac{1}{\eta_{th,u}}$ [kJ_r/kJ_{th}]

- $\dot{E}_{u,t} = \frac{\eta_{e,u}}{\eta_{th,u}} \cdot \dot{Q}_{u,t}$



$$\dot{Q}_{sink} = \dot{Q}_{u,t} = \dot{m}_{sink,t} \cdot cp_{sink} \cdot (T_{sink_out,t} - T_{sink_in,t})$$

$$\dot{E}_{u,t} = \frac{\dot{Q}_{u,t}}{COP_{u,t}}$$

$$COP_{u,t} = \eta_{COP} \cdot COP_{th,u,t}$$

$$\eta_{COP} = 50\%$$

$$COP_{th,u,t} = \frac{\tilde{T}_{sink,t}}{\tilde{T}_{sink,t} - \tilde{T}_{source,t}}$$

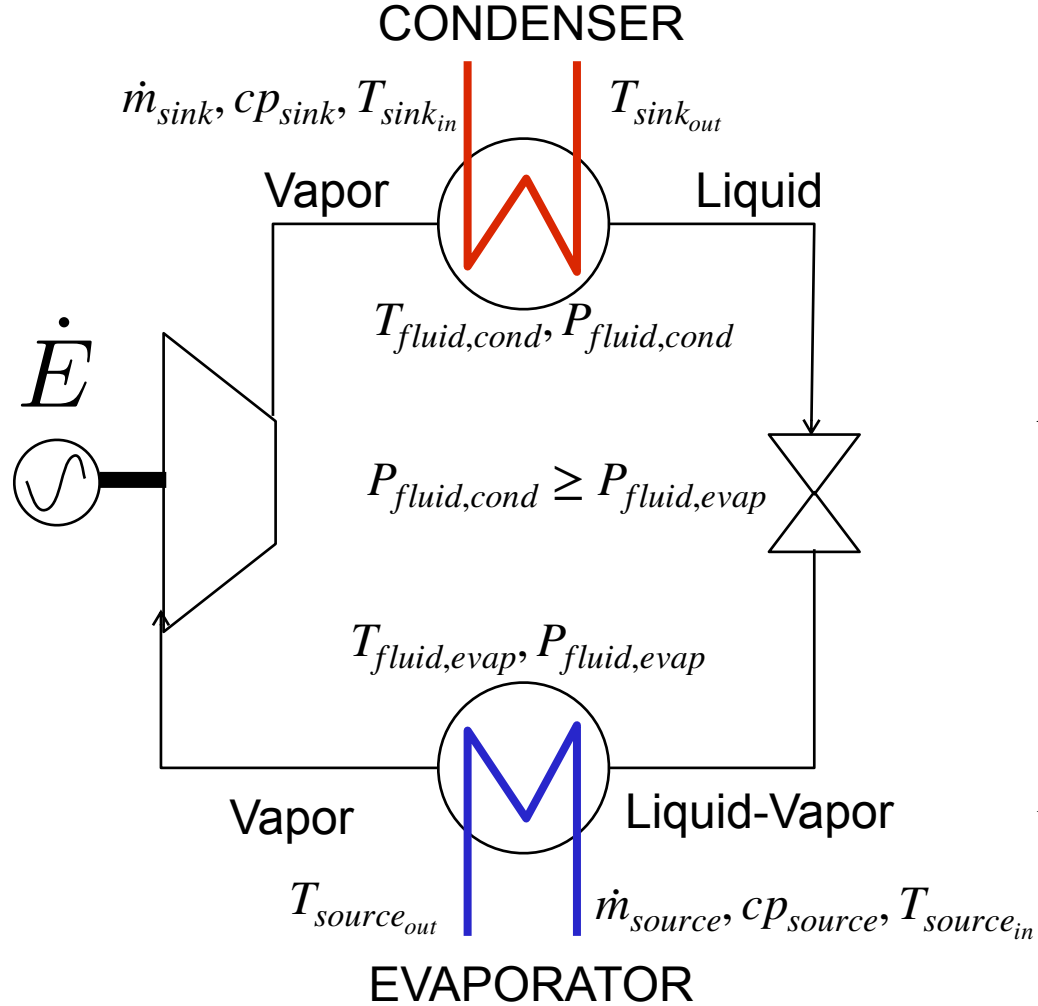
$$\tilde{T}_{sink,t} = \frac{T_{sink_out,t} - T_{sink_in,t}}{\ln(T_{sink_out,t}) - \ln(T_{sink_in,t})}$$

$$\tilde{T}_{source,t} = \frac{T_{source_out,t} - T_{source_in,t}}{\ln(T_{source_out,t}) - \ln(T_{source_in,t})}$$

$$\dot{Q}_{source,t} = \dot{m}_{source,t} \cdot cp_{source} \cdot (T_{source_in,t} - T_{source_out,t})$$

$$\dot{Q}_{source,t} = \dot{Q}_{u,t} - \dot{E}_{u,t}$$

Sizing : condenser, evaporator & compressor



$$\dot{Q}_{u,t} = \dot{Q}_{sink,t} = \dot{m}_{sink,t} \cdot cp_{sink} \cdot (T_{sink_{out},t} - T_{sink_{in},t})$$

$$\dot{Q}_{sink,t} = \dot{m}_{fluid,t} \cdot (h(T_{fluid,cond_{in},t}, P_{fluid,cond_{in},t}) - h(T_{fluid,cond_{out},t}, P_{fluid,cond_{out},t}))$$

$$A_{condenser} = \max_{t \in lifetime} \left(\left(\frac{1}{u_{sink}} + \frac{1}{u_{fluid,cond}} \right) \frac{\dot{Q}_{sink,t}}{\frac{(T_{fluid,cond,t} - T_{sink_{in},t}) - (T_{fluid,cond,t} - T_{sink_{out},t})}{\ln(T_{fluid,cond,t} - T_{sink_{in},t}) - \ln(T_{fluid,cond,t} - T_{sink_{out},t})}} \right)$$

$$\dot{E}_{max} = \max_{t \in lifetime} \left(\frac{\dot{Q}_{u,t}}{COP_{u,t}} \right)$$

$$A_{evaporator} = \max_{t \in lifetime} \left(\left(\frac{1}{u_{source}} + \frac{1}{u_{fluid,evap}} \right) \frac{\dot{Q}_{source,t}}{\frac{(T_{source_{out},t} - T_{fluid,evap,t}) - (T_{source_{in},t} - T_{fluid,evap,t})}{\ln(T_{source_{out},t} - T_{fluid,evap,t}) - \ln(T_{source_{in},t} - T_{fluid,evap,t})}} \right)$$

$$\dot{Q}_{source,t} = \dot{m}_{source,t} \cdot cp_{source} \cdot (T_{source_{in},t} - T_{source_{out},t})$$

$$\dot{Q}_{source,t} = \dot{m}_{fluid,t} \cdot (h(T_{fluid,evap_{out},t}, P_{fluid,evap_{out},t}) - h(T_{fluid,evap_{in},t}, P_{fluid,evap_{in},t}))$$

$$\dot{Q}_{source,t} = \dot{Q}_{sink,t} - \dot{E}_{u,t}$$

- CAPital EXpenditure

$$CAPEX \quad [CHF/year] = \sum_{u=1}^{n_u} \frac{1}{\tau_u} \cdot i_{u\dot{Q}_{u,max}} \cdot \dot{Q}_{u,max}$$

- $i_{u\dot{Q}_{u,max}} \quad [CHF/kW]$ specific investment of unit u for size $\dot{Q}_{u,max}$

- $\dot{Q}_{u,max} = \max_{t \in lifetime} (\dot{Q}_{u,t}) \quad [kW]$ size of unit u

- $\frac{1}{\tau_u} = \frac{1}{\tau(i, lifetime_u)} \quad [year^{-1}]$: annualisation factor of unit u

- TOTal EXpenditure :

$$TOTEX \text{ [CHF/year]} = OPEX \text{ [CHF/year]} + CAPEX \text{ [CHF/year]}$$

it assumes that the unit will be operated with the same power profile over the lifetime of the equipment

We assume a mean year and the associated costs as being representative of the lifetime of the project