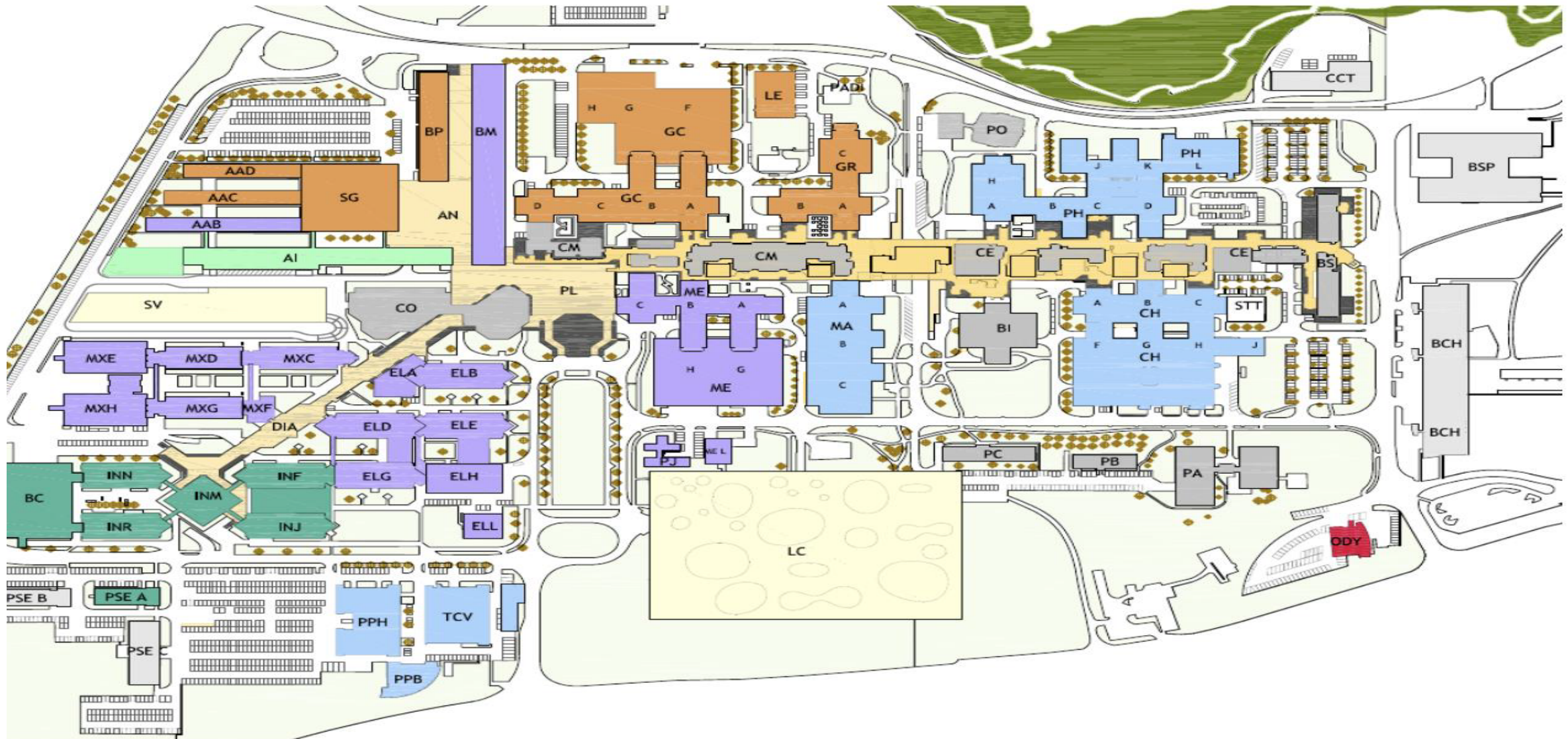


Part 1 : defining the heating needs of a building stock

Prof François Marechal

EPFL Buildings stock



■ Analyse

- What we want ?
 - define variables (x_i) : give a textual description
 - define physical units : e.g. $[kJ_e/kJ_{th}]$
 - define order of magnitude of expected value of x_i : $x_{i_{min}} \leq x_i \leq x_{i_{max}}$
- What we know : Write equations defining your knowledge !
 - write the knowledge as a set of equations $f_k(x_i, \pi_{k,j}) = 0$
 - $\pi_{k,j}$ are parameters of equation k
- What we have : collect the data :
 - values of $\pi_{k,j} \Rightarrow$ reference, [physical units], comments
 - add assumptions : $f_a(x_i, \pi_{a,j}) = 0$ so that $\#k + \#a = \#i$

■ Generate

- Find numerical value of x_i by solving the set of equations : $f_e(x_i, \pi_{e,j}) = 0$, with $x_{i_{min}} \leq x_i \leq x_{i_{max}}$ and $f_e = \{f_k, f_a\}$
 - define the solving method
 - define the convergence criteria

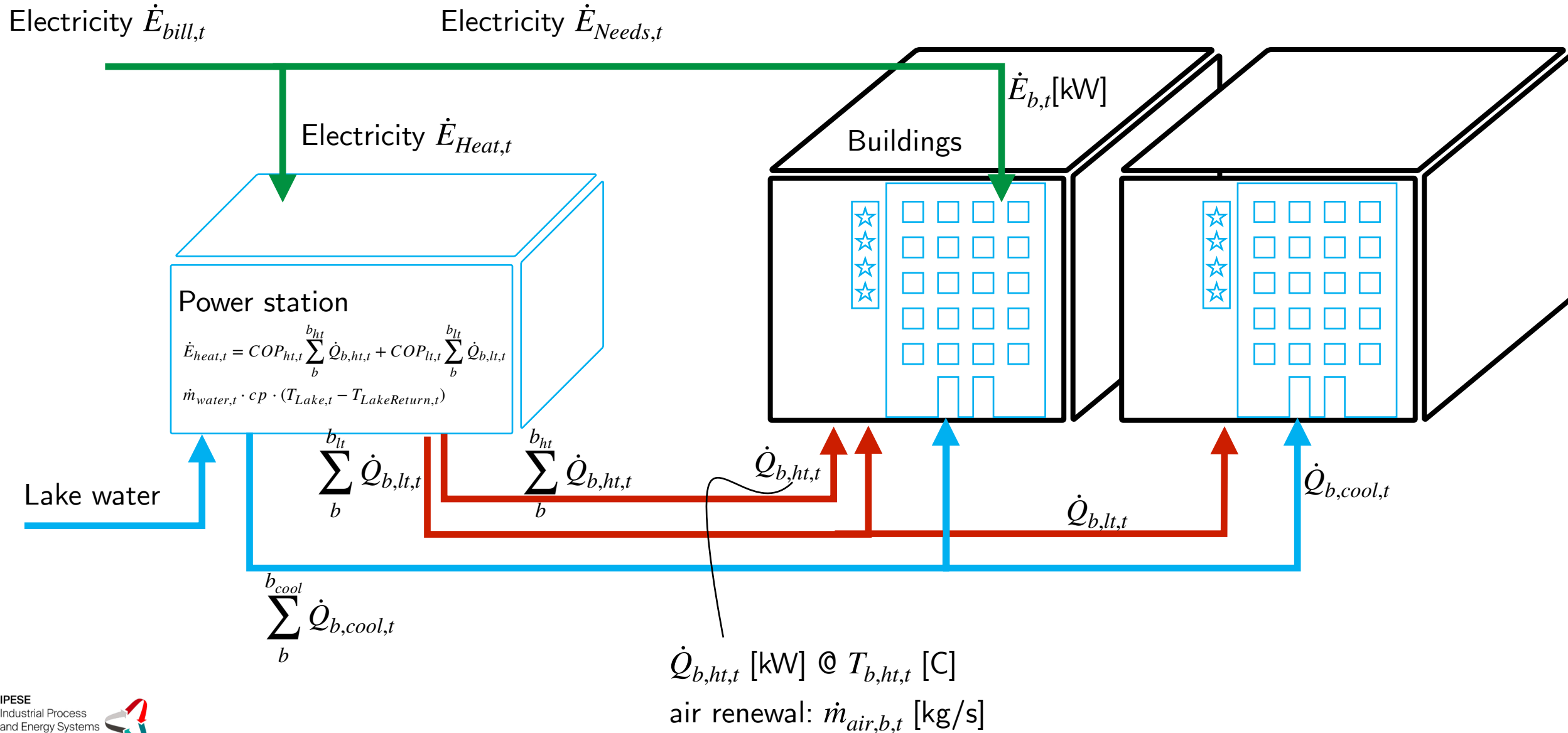
■ Interpret

- Verify that the value of x_i is meaningful for the application

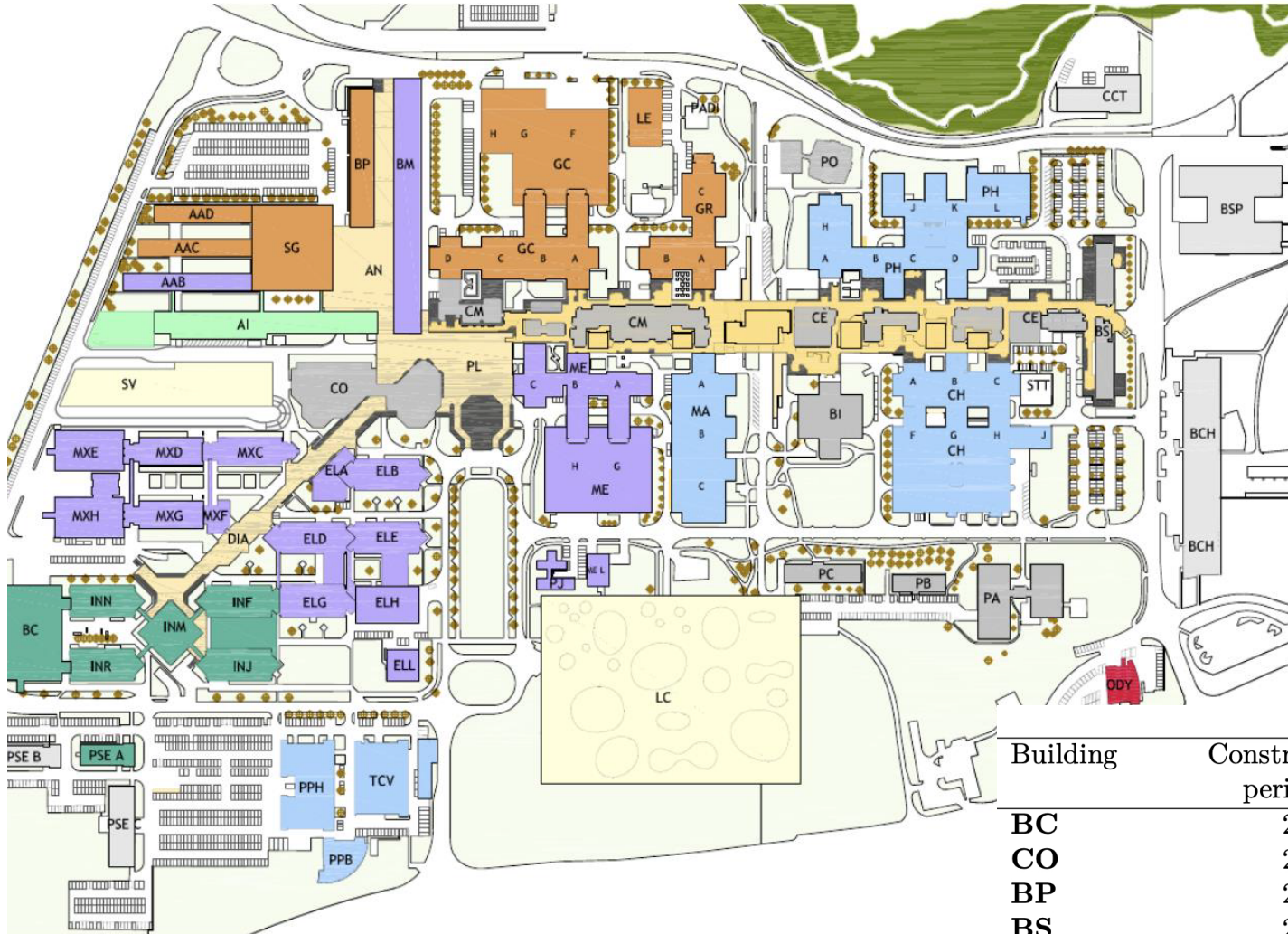
■ Report

- Report the values (plots, tables, validity check)

EPFL What are the needs ?



Buildings stock



Heating needs are defined by :

- $\dot{Q}_{b,t} \quad \forall b \in \{1..n_b\}$ [kW]
heat required by building b
at time t of the year

- $T_{b,t}^{supply} \quad \forall b \in \{1..n_b\}$ [°C]
Minimum temperature
of the heat supply of building b
at time t of the year

Available :

Table 1.1: EPFL Buildings

Building	Construction period ^a	Heated surface A_{th} [m ²]	Annual heat demand Q_{th} [kWh]	Annual electricity demand Q_{el} [kWh]
BC	2	17480	418,491	1,603,596
CO	2	11901	477,008	943,653
BP	2	10442	457,861	691,031
BS	2	10267	509,183	350,860
TCV	2	6095	318,209	2,067,675

- $\dot{Q}_{b,t}[kW]$: Heat load of building b at time t of its life time

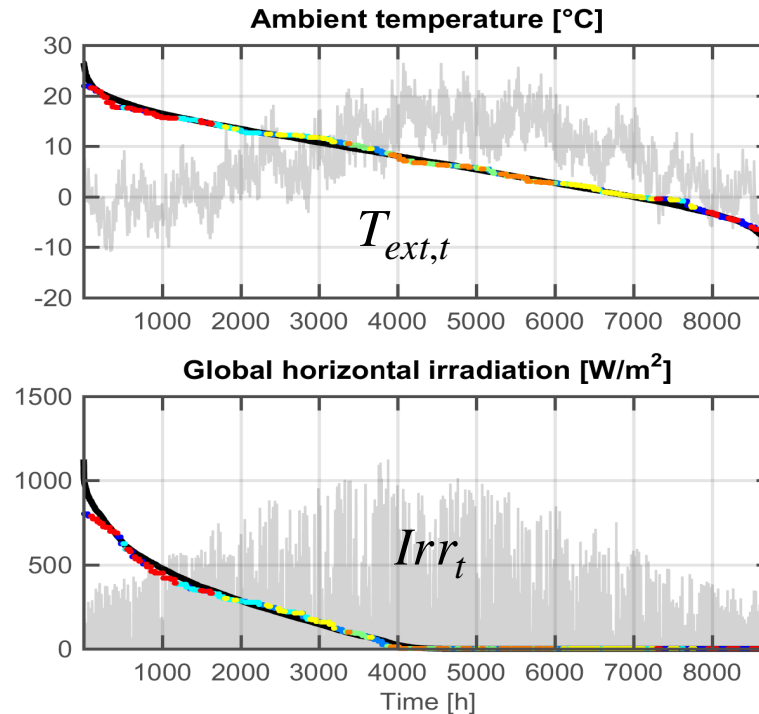
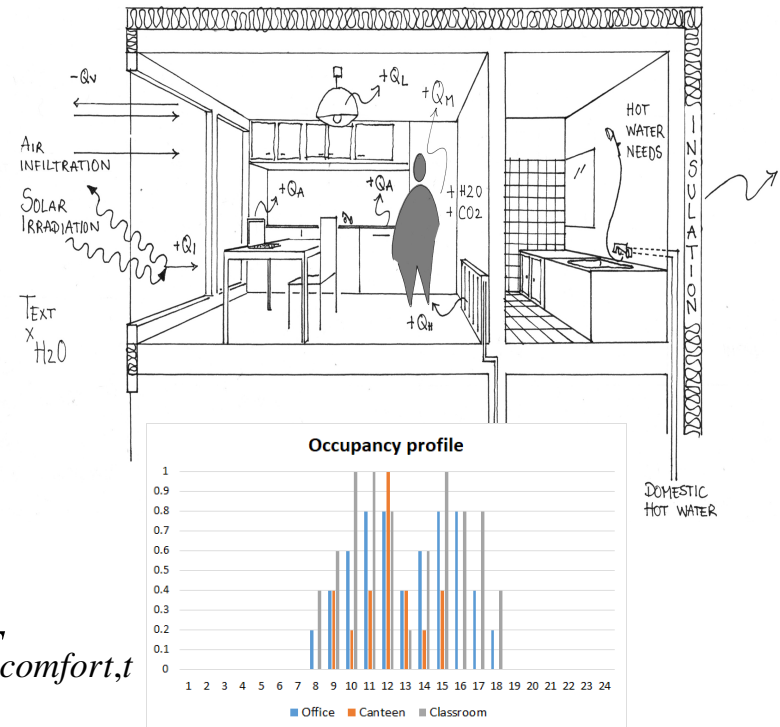
Building envelope

S [m²]

h [m]

People presence cap_t

Comfort Temperature $T_{comfort,t}$

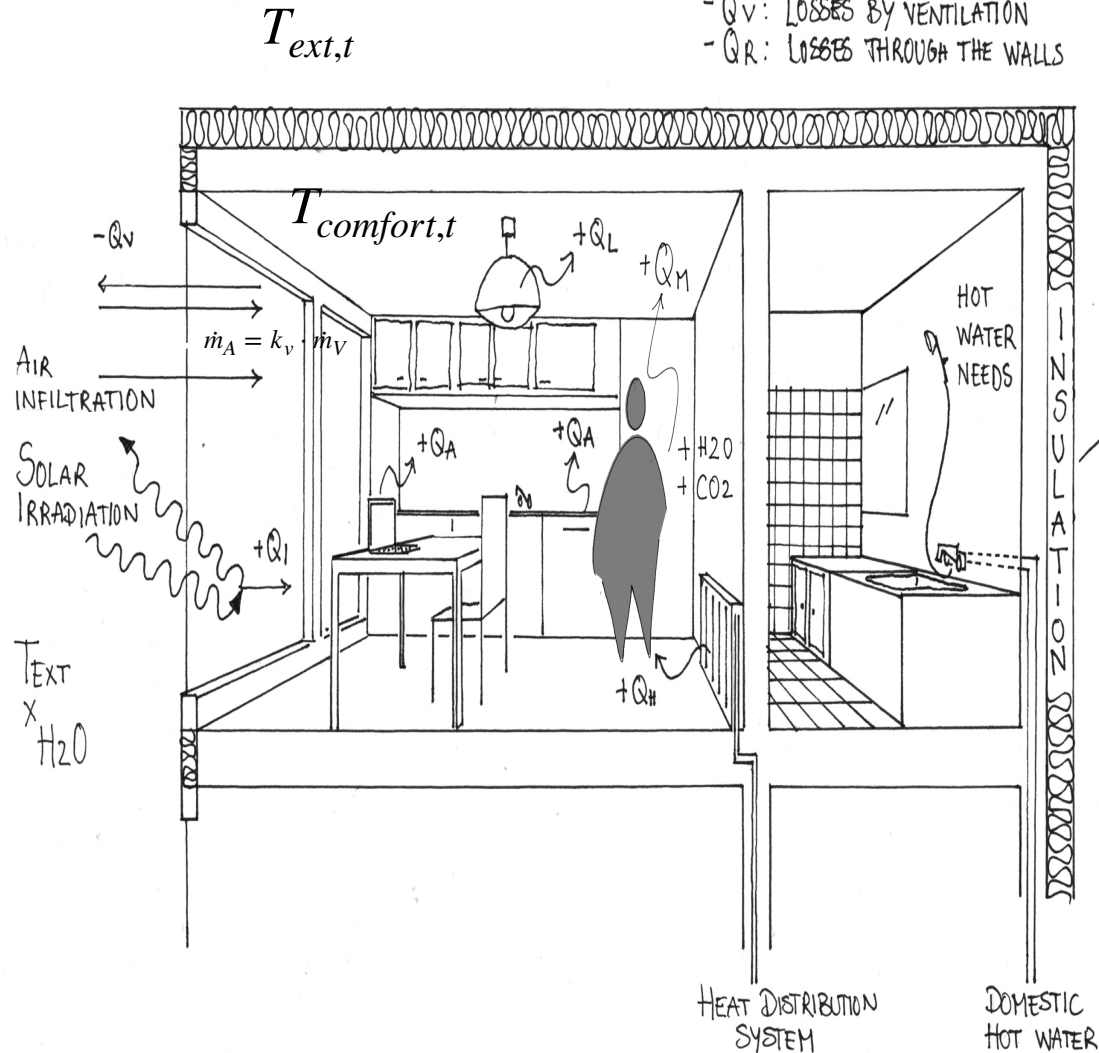


Measurement

Table 1.1: EPFL Buildings

Building	Construction period ^a	Heated surface A_{th} [m ²]	Annual heat demand Q_{th} [kWh]	Annual electricity demand Q_{el} [kWh]
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- +Q_A : GAIN BY APPLIANCES
- +Q_H : HEAT TO COMPENSATE LOSSES
- +Q_L : GAIN BY LIGHTING SYSTEM
- +Q_M : GAIN BY HUMAN
- +Q_I : GAIN BY IRRADIATION
- Q_V : LOSSES BY VENTILATION
- Q_R : LOSSES THROUGH THE WALLS



Our knowledge :

The model of the building envelop heat balance

$$\dot{Q}_{A,t}[\text{kW}] = \dot{E}_{A,t}$$

$$\dot{Q}_{L,t}[\text{kW}] = \dot{E}_{L,t}$$

$$\dot{Q}_{M,t}[\text{kW}] = \dot{q}_{cap} \cdot \sum_{cap} cap_t$$

$$\dot{Q}_{I,t}[\text{kW}] = Irr_t \cdot k_{sun}$$

$$\dot{Q}_{V,t}[\text{kW}] = \dot{m}_V \cdot cp_{air} \cdot (T_{comfort,t} - T_{ext,t})$$

$$\dot{Q}_{R,t}[\text{kW}] = \sum_{wall} k_{wall} \cdot S_{wall} \cdot (T_{comfort,t} - T_{ext,t})$$

$$\dot{Q}_{V,t} + \dot{Q}_{R,t} = k_{th}(T_{comfort,t} - T_{ext,t})$$

Gains

Losses

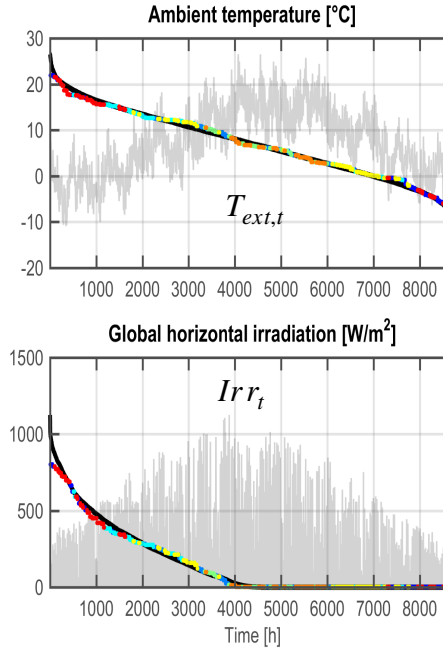
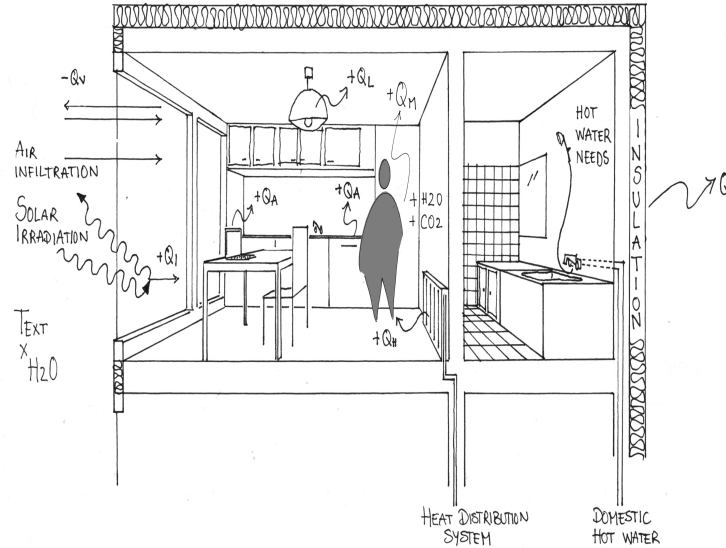
Heat balance :

what is the load to maintain the comfort temperature ?

$$\dot{Q}_{H,t}[\text{kW}] = \max(0, \dot{Q}_{V,t} + \dot{Q}_{R,t} - (\dot{Q}_{A,t} + \dot{Q}_{L,t} + \dot{Q}_{M,t} + \dot{Q}_{I,t}))$$

What we want : $\dot{Q}_b(t)[kW] = \dot{Q}_H(t)$

- + $\dot{Q}_A$: GAIN BY APPLIANCES
- + $\dot{Q}_H$: HEAT TO COMPENSATE LOSSES
- + $\dot{Q}_L$: GAIN BY LIGHTING SYSTEM
- + $\dot{Q}_M$: GAIN BY HUMAN
- + $\dot{Q}_I$: GAIN BY IRRADIATION
- $\dot{Q}_V$: LOSSES BY VENTILATION
- $\dot{Q}_R$: LOSSES THROUGH THE WALLS



$$\dot{Q}_{A,t} = \dot{E}_{A,t}$$

$$\dot{Q}_{L,t} = \dot{E}_{L,t}$$

$$\dot{Q}_{M,t} = \dot{q}_{cap} \cdot \sum_{cap} cap_t$$

$$\dot{Q}_{I,t} = Irr_t \cdot k_{sun}$$

$$\dot{Q}_{V,t} = \dot{m}_V \cdot cp_{air} \cdot (T_{comfort,t} - T_{ext,t})$$

$$\dot{Q}_{R,t} = \sum_{wall} k_{wall} \cdot S_{wall} \cdot (T_{comfort,t} - T_{ext,t})$$

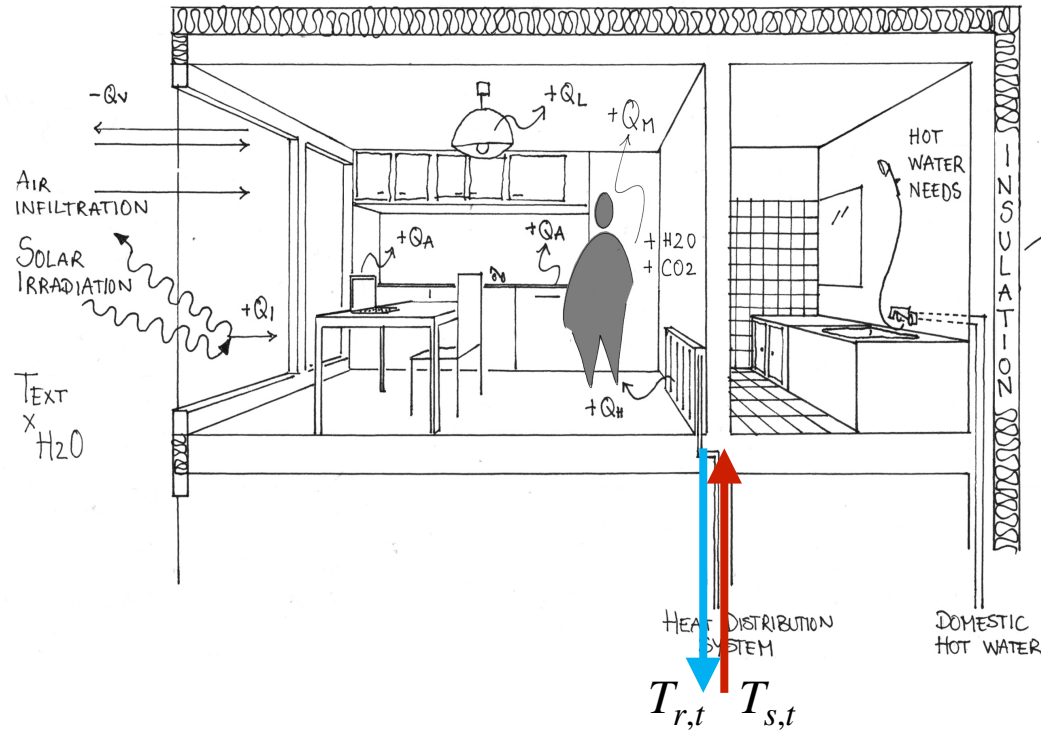
$$\dot{Q}_{H,t} = \max(0, \dot{Q}_{V,t} + \dot{Q}_{R,t} - (\dot{Q}_{A,t} + \dot{Q}_{L,t} + \dot{Q}_{M,t} + \dot{Q}_{I,t}))$$

$$\dot{Q}_H(t) = \max(0, k_{th} \cdot (T_{comfort,t} - T_{ext,t}) - k_{sun} \cdot Irr_t - \dot{Q}_{gain,t})$$

$$Q_H(t_0, t_{end}) = \int_{t_0}^{t_{end}} \dot{Q}_{H,t} \cdot dt = \int_{t_0}^{t_{end}} \max(0, k_{th} \cdot (T_{comfort,t} - T_{ext,t}) - k_{sun} \cdot Irr_t - \dot{Q}_{gain,t}) \cdot dt$$

- $Need_{k,t} = f(\pi_k, x_{k,i,t})$
 - π_k : parameters for calculation the need k
 - assumptions & knowledge
 - from the description of the Physical/Chemical phenomena
 - observations => parameter fitting
 - $x_{i,k,t}$: variables defining the environment applying to the need k
 - observations

- + Q_A : GAIN BY APPLIANCES
- + Q_H : HEAT TO COMPENSATE LOSSES
- + Q_L : GAIN BY LIGHTING SYSTEM
- + Q_M : GAIN BY HUMAN
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- Q_V : LOSSES BY VENTILATION
- Q_R : LOSSES THROUGH THE WALLS



Temperatures of the heat distribution (hd) system:
supply $T_{s,t}$ and return $T_{r,t}$ can be calculated

$$\dot{Q}_{H,t} = \dot{m}_{hd,t} \cdot c p_{hd} \cdot (T_{s,t} - T_{r,t})$$

$$T_{r,t} = T_{s,t} - \frac{\dot{Q}_{H,t}}{\dot{m}_{hd,t} \cdot c p_{hd}}$$

$T_{s,t}$ is calculated by solving

$$\dot{Q}_{H,t} = U A_{hd} \frac{(T_{s,t} - T_{r,t})}{\ln(T_{s,t} - T_{comfort,t}) - \ln(T_{r,t} - T_{comfort,t})}$$

with $U A_{hd}$ calculated from the design conditions

$$U A_{hd} = \dot{Q}_{H,design} \cdot \frac{\ln(T_{s,design} - T_{comfort,design}) - \ln(T_{r,design} - T_{comfort,design})}{(T_{s,design} - T_{r,design})}$$

For each building and each time will obtain the minimum supply and return temperatures of the building.

$$Q_H(t_0, t_{end}) = \int_{t_0}^{t_{end}} \dot{Q}_{H,t} \cdot dt = \int_{t_0}^{t_{end}} \max(0, k_{th} \cdot (T_{comfort,t} - T_{ext,t}) - k_{sun} \cdot Irr_t - \dot{Q}_{gain,t}) \cdot dt$$

Calculate k_{sun} and k_{th} if

$$Q^1 = Q_H(\text{January, December})$$

and

$$Q^2 = Q_H(\text{February, March})$$

$$Q_H(\text{January, December})(k_{sun}, k_{th}) - Q^1 = 0$$

$$Q_H(\text{February, March})(k_{sun}, k_{th}) - Q^2 = 0$$

2 equations and 2 unknowns : k_{sun}, k_{th}

Activate your knowledge :

Solve a set of equations

$$F(X)=0$$