

# Yangying Zhu

Department of Mechanical Engineering, Massachusetts Institute of Technology, Cambridge, MA 02139 e-mail: yyzhu@mit.edu

## Dion S. Antao

Department of Mechanical Engineering, Massachusetts Institute of Technology, Cambridge, MA 02139 e-mail: dantao@mit.edu

# Kuang-Han Chu

Department of Mechanical Engineering, Massachusetts Institute of Technology, Cambridge, MA 02139 e-mail: flyjohn@gmail.com

## Siyu Chen

Department of Mechanical Engineering, Massachusetts Institute of Technology, Cambridge, MA 02139 e-mail: chensiyu@mit.edu

## Terry J. Hendricks

NASA/Jet Propulsion Laboratory, California Institute of Technology, 4800 Oak Grove Drive, Pasadena, CA 91109 e-mail: terry.j.hendricks@jpl.nasa.gov

# Tiejun Zhang

Department of Mechanical and Materials Engineering, Masdar Institute of Science and Technology, Building 1A, P.O. Box 54224, Abu Dhabi, UAE e-mail: tjzhang@masdar.ac.ae

# Evelyn N. Wang<sup>1</sup>

Department of Mechanical Engineering, Massachusetts Institute of Technology, Cambridge, MA 02139 e-mail: enwang@mit.edu

# Surface Structure Enhanced Microchannel Flow Boiling

We investigated the role of surface microstructures in two-phase microchannels on suppressing flow instabilities and enhancing heat transfer. We designed and fabricated microchannels with well-defined silicon micropillar arrays on the bottom heated microchannel wall to promote capillary flow for thin film evaporation while facilitating nucleation only from the sidewalls. Our experimental results show significantly reduced temperature and pressure drop fluctuation especially at high heat fluxes. A critical heat flux (CHF) of 969 W/cm² was achieved with a structured surface, a 57% enhancement compared to a smooth surface. We explain the experimental trends for the CHF enhancement with a liquid wicking model. The results suggest that capillary flow can be maximized to enhance heat transfer via optimizing the microstructure geometry for the development of high performance two-phase microchannel heat sinks.

[DOI: 10.1115/1.4033497]

Keywords: microchannel flow boiling, surface microstructures, flow instabilities, critical heat flux

## 1 Introduction

The increasing power densities in various electronic devices including concentrated photovoltaics, power electronics, and laser diodes pose significant thermal management challenges for the electronics industry [1–3]. Two-phase microchannel heat sinks are attractive to cool advanced electronic devices because they harness the latent heat of vaporization to dissipate high heat fluxes in a compact form factor. However, minimizing flow instabilities during boiling while enhancing the critical heat flux (CHF) to maximize heat dissipation has been difficult to achieve [4–6]. These flow instabilities which can be triggered by several mechanisms including explosive bubble expansion [7], upstream compressibility [8,9], and density wave oscillation [10] can lead to large pressure drop fluctuations across the channels and temperature spikes associated with liquid dry-out. This dry-out severely

limits the heat removal ability of these microchannel heat sinks and leads to device failure once reaching CHF [11].

To suppress flow instability and to enhance heat transfer, recent studies have focused on incorporating various structures in microchannels, such as inlet restrictors [12–14], artificial nucleation sites [14,15], vapor venting membranes [16–18], micropin fins [19–21], and nanowire-coated surfaces [22–24] integrated into the microchannel. However, there are challenges with several of these approaches. Inlet restrictors can significantly reduce backflow but with a pressure drop penalty for the stabilization [13]. Fabricated nucleation sites have demonstrated enhanced nucleate boiling heat transfer; however, the introduction of the cavities alone can increase the instabilities [14]. Vapor venting membranes can reduce dry-out and pressure drop oscillations by locally removing the expanding vapor; however, the operational range is limited due to the risk of membrane flooding at high pressures [17].

Micro and nanostructure-coated surfaces are attractive owing to the ability to modify surface wettability, generate capillarity, and create nucleation sites. In fact, in pool boiling, superhydrophilic micro and nanostructures have demonstrated significantly increased CHF [25–31] and biophilic patterned surfaces have

<sup>&</sup>lt;sup>1</sup>Corresponding author.

Contributed by the Heat Transfer Division of ASME for publication in the JOURNAL OF HEAT TRANSFER. Manuscript received June 9, 2015; final manuscript received April 14, 2016; published online May 17, 2016. Editor: Portonovo S. Ayyaswamy.

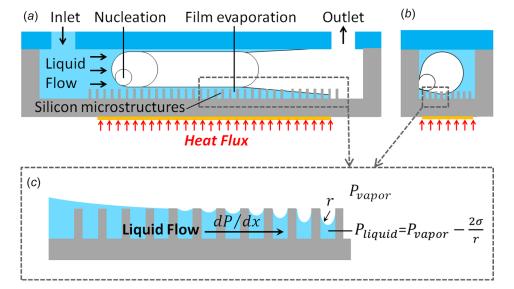


Fig. 1 Schematic of the microchannel heat sink design with micropillars on the heated surface. (a) Side view, (b) cross section view, and (c) magnified view of the liquid film forming menisci which create the capillary pressure gradient, dP/dx, that helps drive the liquid flow. The equation that describes the liquid pressure below the meniscus is the Young–Laplace equation where  $\sigma$  is the surface tension of the liquid, r is the radius of curvature of the local meniscus, and  $P_{\text{liquid}}$  and  $P_{\text{vapor}}$  are the local pressure of the liquid and vapor, respectively.

shown large enhancements in heat transfer coefficients (HTCs) [32,33]. In flow boiling, silicon nanowire-coated channel surfaces have been reported to reduce temperature fluctuations [22], increase the HTC and CHF, and decrease the pressure drop across the microchannels with water as the working fluid [23,24]. The enhancement mechanism was mainly attributed to both increased wettability in delaying CHF and nucleation sites formed by the nanowire bundles to improve the HTC in the nucleate boiling regime. At high heat fluxes, however, the annular flow regime typically dominates, where film evaporation is the important heat transfer mode [4]. Thus, the role of the surface structures on the stability of the annular liquid film and on the film evaporation performance needs to be investigated. In addition, while introducing structures on the channel wall offers capillary driven liquid flow, the associated viscous resistance [34–36] from the structures, especially in the presence of shear from the vapor, can be significant. These effects are sensitive to the geometry of the structures. Therefore, the precise role of the surface structures on flow boiling needs to be studied in more detail.

In this work, we investigated superhydrophilic microstructured surfaces in microchannels for flow boiling heat transfer. These surface structures have length scales much smaller than the height of the microchannel, and thus are different from micropin fins which extend to the ceiling of the microchannel [19-21]. We fabricated and characterized microchannels with well-defined micropillar arrays on the bottom channel wall, where heat was applied. The hydrophilic micropillars were only integrated on the heated bottom surface to promote wicking and film evaporation while suppressing dry-out. The sidewalls, with tailored roughness of  $1-2 \mu m$ , promoted nucleation near the bottom corners [37]. Spatially decoupling nucleation to the sidewalls and film evaporation to the bottom surface promises to achieve high heat fluxes while maintaining stable heat transfer performance. We characterized structured surface microchannel and benchmark smooth surface microchannel devices in a custom closed loop setup. In particular, we investigated flow instabilities through temporally resolved temperature and pressure drop measurements, and simultaneous visualization of the flow in the device. We also characterized the heat transfer performance (the HTC, CHF, and pressure drop), and explained the experimental trends for the CHF enhancement with an adiabatic liquid wicking model. The insights gained from

this work are a first step toward guiding the design of stable, high performance surface structure enhanced two-phase microchannel heat sinks.

## 2 Methodology

In high heat flux applications, microchannel heat sinks usually operate in the annular flow regime due to the high vapor quality associated with heat dissipation in the confined space [38]. Since evaporation can be dominant in the annular flow regime, we designed the structured surfaces to enhance and sustain stable liquid film evaporation (Figs. 1(a) and 1(b)). The structures were integrated only on the bottom heated surface where the wall temperature and the heat flux are the highest, in order to suppress liquid dry-out by generating capillary flow in the presence of menisci formation (Fig. 1(c)). This capillary flow can be created both along the channel direction and from the sidewalls to the center (the dotted line regions in Figs. 1(a) and 1(b)). The sidewalls have tailored roughness of 1–2  $\mu$ m to promote nucleation [37]. By nucleating on the side walls, it is less likely for dry-out to occur on the bottom surface. In contrast, for smooth-surface microchannels, dry-out typically occurs on the bottom surface due to explosive bubble growth from it.

2.1 Device Design and Fabrication. We investigated single microchannels with typical characteristic dimensions of 10 mm in length,  $500 \,\mu\text{m}$  in width, and  $500 \,\mu\text{m}$  in height. We varied the micropillar geometries on the bottom surface of the microchannel with diameters of 5–10  $\mu$ m, pitches of 10–40  $\mu$ m, and constant heights of 25  $\mu$ m. These micropillar geometries were chosen for the following reasons: (1) The micropillars are easy to fabricate in silicon (Si) using standard etching processes and the geometries can be well controlled in this range. (2) At these length scales, the capillary pressures that can be generated are a few kPa which are comparable to the typical microchannel pressure drop. This suggests that capillary effects are not small and can be used to manipulate flow behavior. (3) The surface structures are mechanically robust and will not change morphology (deform or form clusters) as the liquid evaporates. The specific micropillar geometries fabricated and tested are shown in Table 1, which allows investigation of the effect of micropillar diameter d and pitch l on heat transfer

Table 1 Geometric parameters (height, diameter, and pitch) of the fabricated micropillars in the microchannel test devices

Device no.	Height, h (μm)	Diameter, $d(\mu m)$	Pitch, l (μm)
S1	25	5	10
S2 S3 S4	25	5	15
S3	25	10	30
S4	25	10	40

and flow characteristics during flow boiling. Specifically, we aimed to maximize the liquid propagation coefficient in micropillar arrays with a fixed aspect ratio h/d but different pitches l based on a fluid wicking model developed by Xiao et al. [39].

To emulate the heat flux from a high performance electronic device, we integrated a thin-film metal heater (8.6 mm long- $\times$  380  $\mu$ m wide) directly underneath the microchannel to serve as a heat source via Joule heating (Figs. 1(a) and 2(a)). In addition to the heating element, we incorporated four thin-film resistance temperature detectors (RTDs), which are commonly used for flow boiling studies [22–24,40,41], along the length of the heater to measure the microchannel backside surface temperature at different locations. Specifically, the distances x of RTD1 through RTD4 from the inlet of the microchannel were 0 mm, 1.4 mm, 5.7 mm, and 10 mm, respectively, (Fig. 2(a)).

Standard silicon MEMS fabrication processes were used to create the microchannel test devices and are summarized in Fig. 2. The micropillars were etched in a  $500 \, \mu \text{m}$  thick Si wafer using deep reactive ion etching (DRIE) of the channel bottom surface

(Fig. 2(b)). A second 500  $\mu$ m thick Si wafer was etched through using DRIE to define the channel sidewalls (Fig. 2(c)). Inlet and outlet ports were created on a Pyrex wafer by laser drilling (Fig. 2(d)). The two Si wafers were bonded together using direct Si-Si fusion bonding. A 1 μm silicon dioxide (SiO<sub>2</sub>) layer was thermally grown on the Si surface as a hydrophilic coating on the channel walls and as an electrical insulation layer on the backside. The Pyrex wafer was subsequently bonded onto the Si wafers using anodic bonding to cover the microchannel and facilitate flow visualizations (Fig. 2(e)). Finally, a layer of  $\sim$ 170 nm thick platinum (Pt) was deposited on the backside of the microchannel with electron-beam evaporation and patterned by lift-off technique to serve as the heater and RTDs (Figs. 2(f), 3(b), and 3(c)). To maximize the power dissipation capability of the heater, the target heater resistance was determined by the maximum allowable heater voltage (180 V) and current (0.5 A) to prevent burnout. To achieve this target resistance of 360  $\Omega$ , we designed the thin film heater thickness and dimensions. In addition to the microstructured microchannels, we also fabricated microchannels with smooth surfaces following a similar procedure; however, a polished Si wafer (roughness < 50 nm) was used instead of the micropillar wafer in the initial step (Fig. 2(b)).

Figures 3(a) and 3(b) show the front and backside of a fabricated microchannel device. The two open chambers next to the microchannel (Figs. 3(a) and 3(d)) were incorporated to minimize heat loss via conduction and to better isolate the effect of flow boiling in the microchannel. Figure 3(c) shows a magnified view of the Pt heater and an RTD on the backside of the microchannel. Figure 3(d) shows a scanning electron micrograph (SEM) of the cross section of the microchannel (A–A plane in Fig. 3(a)) with

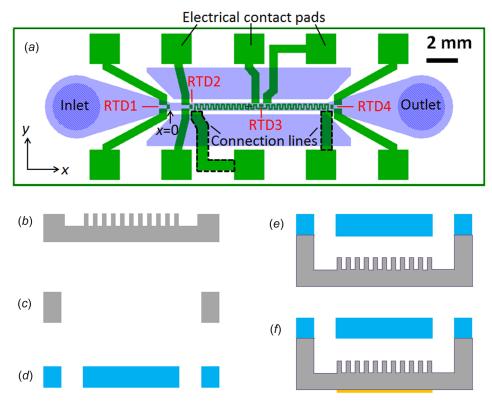


Fig. 2 Design and fabrication process of the microchannel device. (a) Schematic (to scale) of the heater and RTDs on the backside of the microchannel device. The dotted sections are the electrical connection lines to the contact pads. (b) Micropillars of 25  $\mu$ m height were etched in Si using DRIE. (c) A Si wafer was etched through using DRIE to define the channel. (d) Inlet and outlet ports were laser-drilled on a Pyrex glass wafer. (e) The Si layers were bonded using direct Si–Si bonding. A silicon dioxide (SiO<sub>2</sub>) layer was thermally grown on the Si surface. The Pyrex layer was bonded to the top Si layer using anodic bonding. (f) A platinum (Pt) layer was deposited on the backside of the microchannel using electron-beam evaporation and patterned to form the heater and RTDs.

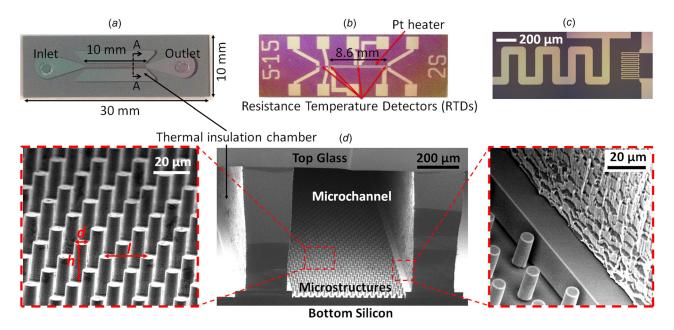


Fig. 3 Images of a representative fabricated microchannel with micropillar arrays. Optical images of the (a) front and (b) backside of a device. (c) Optical microscope image of the heater and RTD4 on the backside of the microchannel. (d) SEM image of the cross section (A–A plane in Fig. 3(a)) of a microchannel with magnified view of the micropillars (left inset) and a sidewall at the bottom corner (right inset).

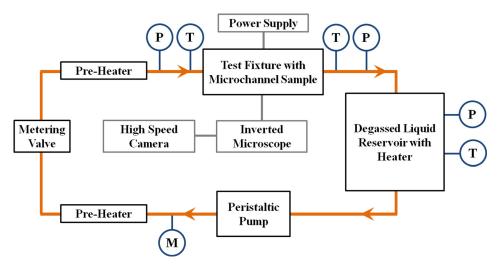


Fig. 4 Schematic of the custom flow boiling loop used in the study. The loop consists of a liquid reservoir, a pump to provide a constant flow rate, a valve for flow stabilization, preheaters to minimize subcooling, a test fixture to interface with the test device, and various sensors. The components "P," "T," and "M" indicate locations of pressure transducers, thermocouples and the liquid flow meter, respectively.

representative micropillars. The magnified views of micropillars on the channel bottom surface and a side wall near the bottom corner are shown in the left and right inset of Fig. 3(d). The side walls have small roughness ( $\sim$ 1–2  $\mu$ m) from the DRIE process (Fig. 2(c)).

## 2.2 Experiment Methodology and Measurement Uncertainty.

We developed a closed loop test rig to characterize the microchannel test devices during flow boiling (Fig. 4). The loop consists of a liquid reservoir, a pump to provide a constant flow rate, a valve for flow stabilization, preheaters to minimize subcooling, a test fixture to interface with the test device, and various sensors. Degassed and high purity water (WX0004-1, OmniSolv, McLean, VA) was used as the working fluid. Throughout the experiment,

water in the liquid reservoir was heated and degassed to saturated conditions under atmospheric pressure ( $T_{\rm water,res} = 100\,^{\circ}{\rm C}$  for  $P_{\rm water,res} = 1$  atm). The fluid from the reservoir was pumped through the loop using a peristaltic pump (7528-30, Masterflex, Gelsenkirchen, Germany) to avoid contamination of the working fluid. In order to measure the flow rate with a liquid flow meter (L-50CCM-D, Alicat Scientific, Tucson, AZ) which has a maximum working temperature of 60 °C, the degassed liquid was cooled via heat exchange with the ambient to below 60 °C as it passed through the metal tubing (the line in Fig. 4 between the liquid reservoir and the flow meter). The mass flux chosen in this study was  $G = 300\,{\rm kg/m^2} \cdot {\rm s}$ , which is a commonly used value in the literature [4,15–17]. In addition, this moderate mass flux allowed for high heat flux dissipation at reasonable pressure drops and pumping powers. To achieve this mass flux, the flow rate was

maintained at 4.5 ml/min. We reduced the flow rate fluctuations intrinsic to the peristaltic pump by using a high pump speed (~70 rpm) with the smallest pump tubing available (tube ID = 0.8 mm, L/S 13, Masterflex) for the pump used in the study. However, flow rate fluctuations (±0.6 ml/min) were inevitable with the peristaltic pump at these low mass fluxes. Accordingly, a metering valve (SS-SS4-VH, Swagelok, Signal Hill, CA) was used to create additional hydraulic resistance (~8 kPa) for flow stabilization within the loop, and was kept at a fixed opening for all the testing (the structured surface test samples and the smooth surface test sample). Since the liquid was subcooled due to heat loss to the ambient before the microchannel test section, we added preheaters (FGR-030, Omega, Stamford, CT) to compensate for this heat loss. The preheaters maintained a minimum liquid subcooling (10 °C) while also avoiding boiling at the entrance of the test fixture. Thermocouples (K type, Omega) and pressure transducers (PX319-030A5V, Omega) were used to monitor the loop conditions. The microchannel test devices were placed in an Ultem test fixture that interfaces with the loop. The test fixture was placed in an inverted microscope (TE2000-U, Nikon, Tokyo, Japan) and the flow was captured using a high speed camera (Phantom v7.1, Vision Research, Wayne, NJ) at 2000 frames/s. The two-phase flow pressure at the outlet of the microchannel was approximately  $P_{\text{out}} = 1$  atm since it was connected to the liquid reservoir at atmospheric pressure.

Before the experiment, the Pt heater and RTDs were annealed at 400 °C for 1 hr to avoid resistance drift. The resistance R of the heater and RTDs after annealing was approximately 275  $\Omega$  at room temperature and 340  $\Omega$  at 120 °C. All the RTDs were calibrated in an oven and a linear correlation between the resistance and temperature was observed. The average sensitivity of the temperature with the resistance of the fabricated RTDs is  $\Delta T = 1.4\Delta R$ . The uncertainty of the resistance measurement (  $\sim\!1.4~\Omega)$  resulted in an uncertainty of  $\pm 2\,^{\circ}\text{C}$  in the measured temperature. The microchannels were rinsed in acetone, isopropyl alcohol, and de-ionized water, and subsequently plasma cleaned in an oxygen environment (29 W at 500 mTorr for 15 min) to remove surface contamination. During the experiments, we heated the microchannel by applying a DC voltage across the thin-film heater. The microchannel heater was connected to a DC power supply (KLP 600-4-1200, Kepco, Naju, South Korea), which was controlled using a proportional integral derivative (PID) algorithm in LABVIEW to maintain a constant output power. At each constant heat flux at steady-state, the temperatures  $T_1$  to  $T_4$  measured by RTD1 to RTD4, respectively, the pressures and temperatures at the inlet and outlet of the microchannel, the flow rate, and the voltage and current across the heater were recorded for 2 min. The heat flux was then increased by an increment of approximately 20 W/cm<sup>2</sup> to the next value. Based on our measured temperature and pressure drop, the rise time to reach the next steady-state was less than 1 min due to the small thermal mass of the test device and the small temperature rise ( $\sim 1-2$  °C, see Appendix for details). In addition, we examined the measured steady state temperature for  $\sim$ 5 min and no further rise was observed. Therefore the loop was left running for at least 1 min to reach steady-state before we acquired the data at this new heat flux. All the data was recorded using a data acquisition card (NI-PCI-6289, National Instruments, Austin, TX) at a sample rate of 2 Hz. The experiments were performed twice for each sample under the same experimental conditions to verify repeatability (the samples were cleaned using the methods described here prior to each experiment). The experimental results were similar (within the error bars) and the data reported in this manuscript are from the repeated experiment. Since the microchannel is a three-layer stack that is bonded together, we cannot remove the cover layer (without damaging the sample) of the microchannel to measure the contact angle on the channel walls. However, wicking was observed with the structured surface microchannels before and after the experiment, which suggests an apparent contact angle of 0 deg.

The error bars in the experiments were estimated based on the uncertainty of the measurement from the instrument error (error<sub>instrument</sub>) and the standard deviation (STD) of multiple data points for the time-averaged data, described by the following equation:

$$error = \sqrt{error_{instrument}^2 + STD^2}$$
 (1)

The instrument error included the resolution of the pressure transducers ( $\pm 300\,\text{Pa}$ ), the data acquisition card ( $\pm 1\,\text{mV}$ ) which resulted in the uncertainty of the temperature measured by the RTDs ( $\pm 2\,^{\circ}\text{C}$ ), the power supply (0.06 V and 0.4 mA), and the flow meter ( $\pm 1\,\text{ml/min}$ ).

**2.3 Data Processing.** Since the backside temperature  $(T_1 \text{ to } T_4)$  varies along the microchannel (see Appendix for a representative measurement), we compared different samples using the temperature values measured at the midpoint of the microchannel backside surface by RTD3  $(T_3)$ , where the highest heater surface temperatures were observed. The outlet temperature was lower than the center as expected due to heat spreading in the substrate. The temperature rise  $\Delta T$ , obtained from the difference between the midpoint temperature and the saturation temperature of the fluid  $(T_{\text{sat}})$  at this location, is

$$\Delta T = T_3 - T_{\text{sat}} \tag{2}$$

The fluid pressure and the corresponding saturation temperature (approximately  $100\,^{\circ}$ C) also vary along the channel (see Appendix). The saturation pressure ( $P_{\rm sat}$ ) of the fluid at the midpoint location was determined as the average of the measured absolute pressure values at the inlet and outlet of the microchannel

$$P_{\text{sat}} = \frac{1}{2} (P_{\text{in}} + P_{\text{out}}) \tag{3}$$

The midpoint saturation temperature was then obtained from the NIST database [42] using the calculated midpoint pressure  $P_{\rm sat}$  (Eq. (3)). The heat flux was obtained from the input electrical power (DC voltage and current), the surface area of the channel bottom wall and accounting for the loss to the environment as

$$q'' = \frac{0.95UI - P_{\text{loss}}}{A_{\text{mc}}} \tag{4}$$

where U is the input voltage, I is the input current,  $P_{\rm loss}$  is the calibrated loss to the environment,  $A_{\rm mc}$  is the microchannel bottom wall surface area ( $500\,\mu{\rm m}\times10\,{\rm mm}$ ). The heat generated in the electrical connection lines to the contact pads (enclosed in the dotted line in Fig. 2(a)) was 5% of the total heat from the power supply. The factor of 0.95 (5% loss) in Eq. (4) was obtained based on the geometry of this resistance relative to the total resistance using

$$\frac{R_c}{R_{\text{total}}} = \frac{\frac{L_c}{W_c}}{\frac{L_c}{W_c} + \frac{L_{\text{heater}}}{W_{\text{heater}}}} = 0.05$$
 (5)

where  $R_c$  and  $R_{\rm total}$  are the resistance of the connection lines and the total heater resistance, respectively,  $L_c$ ,  $L_{\rm heater}$ ,  $W_c$ , and  $W_{\rm heater}$  are the length and width of the connection lines and the heater, respectively. The temperature (at the heater surface) dependent heat loss to the environment  $P_{\rm loss}$  measured by the RTDs was obtained from experiments where the test device in the fixture was heated with the flow loop evacuated (i.e., no working fluid). A second-order polynomial (close to linear) fit ( $R^2 = 1$ ) between  $P_{\rm loss}$  (W) and the average microchannel backside surface temperature  $T_{\rm ave}$  (°C) was determined from the experimental data as

$$P_{\text{loss}} = 4.5 \times 10^{-5} T_{\text{ave}}^2 + 0.0163 T_{\text{ave}} - 0.299 \tag{6}$$

Since  $T_2$ ,  $T_3$ , and  $T_4$  are the backside surface temperatures at the inlet, midpoint, and outlet of the microchannel, respectively, by approximating the first half of the microchannel backside surface temperature as  $0.5(T_2+T_3)$ , and the second half as  $0.5(T_3+T_4)$ , the average microchannel backside surface temperature was approximated as

$$T_{\text{ave}} = 0.25T_2 + 0.5T_3 + 0.25T_4 \tag{7}$$

The overall HTC which includes boiling, evaporation, and conduction through the bottom Si layer was calculated from the heat flux q'' and the time-averaged temperature rise  $\Delta T$  as

$$HTC = \frac{q''}{\Lambda T} \tag{8}$$

Due to the unstable nature of flow boiling,  $\Delta T$  typically does not capture the dynamic behavior, such as periodic dry-out, which can also cause severe transient overheating issues. Therefore we defined CHF as the heat flux beyond which the following criteria hold: (1) There is at least a 5 °C jump in  $\Delta T$ ; (2) There is constant or periodic dry-out in terms of time-resolved temperature and pressure drop measurements, and visualizations. In the case of periodic dry-out, the temperature fluctuations were larger than 20 °C, the pressure drop fluctuations were larger than 2 kPa, and the duration of dry-out was longer than half the cycle time.

#### 3 Results and Discussion

In this section, we first compare the stability of the measured temperature and pressure drop, and discuss the difference between the structured surface devices and the smooth surface device. Images and videos of the bottom heated surface were used to investigate the role of surface structures in annular flow stability. We then characterized the boiling curve and pressure drop curve, and discuss the heat transfer enhancement mechanism in the CHF and HTC. Finally, we explain the different behavior among the structured surface microchannels by extension of a liquid wicking model and provide insights into the optimization of the micropillar geometries.

3.1 Temperature and Pressure Drop Fluctuations. Typically with smooth surface microchannels, flow instability can cause temperature and pressure drop fluctuations due to the change of flow pattern and local surface dry-out [43,44]. To study the effect of surface structures on flow instabilities, we measured the temporal change in the backside surface temperature and pressure drop across the microchannels with structured surfaces and compared to the fluctuations of a smooth surface microchannel. The midpoint backside surface temperature  $T_3$  measured from RTD3 which was the highest temperature obtained compared to  $T_1$ ,  $T_2$ , and  $T_4$  was studied for this purpose. The smooth surface and the structured surface microchannels showed similar and small

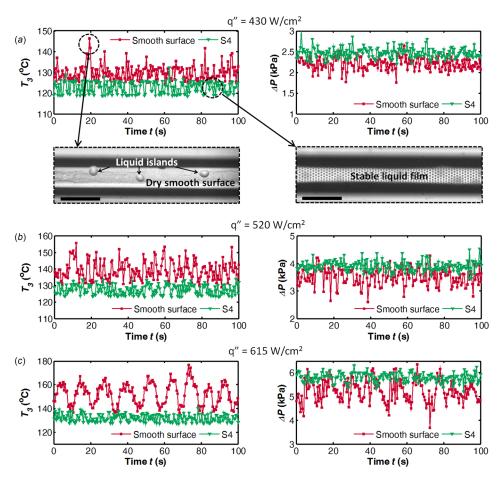


Fig. 5 Temporally resolved temperature and pressure drop, and flow visualization at  $G=300\,\mathrm{kg/m^2}\cdot\mathrm{s}$ . (a) Midpoint backside surface temperature  $T_3$  and pressure drop across a smooth surface microchannel and a structured surface microchannel S4 at  $q''=430\,\mathrm{W/cm^2}$ . Insets are optical images of a smooth bottom channel surface and a structured bottom channel surface (S4). Midpoint backside surface temperature  $T_3$  and pressure drop of a smooth surface microchannel and a structured surface microchannel S4 at (b)  $q''=520\,\mathrm{W/cm^2}$  and (c)  $q''=615\,\mathrm{W/cm^2}$ . The uncertainties of the temperature and pressure drop measurement were approximately  $\pm 2\,^\circ\mathrm{C}$  and  $\pm 300\,\mathrm{Pa}$ .

fluctuations at low heat fluxes ( $q'' < 400 \text{ W/cm}^2$ ) for the mass flux investigated ( $G = 300 \, \text{kg/m}^2 \cdot \text{s}$ ), since the vapor quality was relatively low and dry-out of the thin liquid film was less likely to occur compared to that at higher heat fluxes. As the heat flux increased to  $q'' = 430 \text{ W/cm}^2$ , temperature spikes and increased pressure drop fluctuations were observed for the smooth surface microchannels (Fig. 5(a)). At the same heat flux, all the structured surface microchannels showed small temperature (±5°C) and pressure drop fluctuations (±300 Pa), and the data of one representative structured surface device (S4) is shown in Fig. 5(a). From the visualization of the flow ((the movie is available under "Supplementary Materials" tab for this paper on the ASME Digital Collection) and Fig. 5(a)), the temperature spikes of the smooth surface correspond to dry-out at the bottom microchannel surface. In contrast, flow visualization of the structured surface microchannel (Fig. 5(a) and the "Supplementary Materials" indicated a stable liquid film covering the microchannel bottom surface. This stable liquid film contributed to the stability of the temperature and the pressure drop significantly. Dry-out on the structured surface occurred less frequently with shorter durations and less dry surface area compared to the smooth surface ("Supplementary Materials").

With further increases in heat flux, the temperature spikes observed on the smooth surface microchannel occurred more often and gradually developed to large amplitude (>20 °C) periodic dry-out (Figs. 5(b) and 5(c) at  $q''=520\,\mathrm{W/cm^2}$  and  $615\,\mathrm{W/cm^2}$ , respectively). In comparison, the structured surface microchannel showed stable temperature ( $\pm5$  °C) and pressure drop ( $\pm300\,\mathrm{Pa}$ ) at the same heat flux (Figs. 5(b) and 5(c)), even at CHF ( $\pm5-7$  °C and  $\pm300-600\,\mathrm{Pa}$ , Fig. 6).

To further investigate the role of the structures during the dryout process, we compared visualizations of the flow on a smooth surface and on a representative structured surface (Fig. 7,  $q'' = 430 \,\mathrm{W/cm^2}$ ,  $G = 300 \,\mathrm{kg/m^2}$  s). At  $t = 0 \,\mathrm{s}$  both microchannels were in the annular flow regime. At  $t > 0 \,\mathrm{s}$ , the annular liquid volume started to reduce. Dry-out occurred first from the corners on the smooth surface ( $t = 0.002 \,\mathrm{s}$ ), and the dry surface area expanded to the center of the microchannel ( $0.002 \,\mathrm{s} < t < 0.010 \,\mathrm{s}$ ), leaving individual liquid islands. Due to the inability to supply liquid to the surface, the smooth surface could not maintain this liquid film and thus the dry-out area expanded. The smooth surface was completely dry from  $t = 0.012 \,\mathrm{s}$  to  $0.022 \,\mathrm{s}$  before the liquid built up at the inlet reflushed the channel at  $t = 0.024 \,\mathrm{s}$ .

In comparison, the structured surface (S4) maintained the liquid film due to the wicking capability of the microstructures  $(0.002 \, \text{s} < t < 0.010 \, \text{s})$ , until vapor/dry islands formed first at the center instead of the sides of the channel from  $t = 0.012 \, \text{s}$  (Fig. 7). This suggests that there is wicking from the sides to the center where the propagation distance is the longest. This wicking sustained the liquid film  $(0.002 \, \text{s} < t < 0.010 \, \text{s})$  and delayed dry-out  $(t > 0.012 \, \text{s})$ . In general, the wicking from the structures prevented dry-out from occurring (see "Supplementary Materials"). In addition, the dry patches formed at downstream locations before the upstream locations, which indicate that there is also wicking along the microchannel length. From the above observations, it is evident capillarity generated with the structures plays a significant role in stabilizing the liquid thin film and the resulting surface temperature.

3.2 Heat Transfer Performance Characterization. We also characterized the time-averaged heat transfer performance of the structured surface microchannels. We compared the heat flux q'' calculated by Eq. (4) as a function of the time-averaged midpoint backside surface temperature rise  $\Delta T$  (Eq. (2)) for the four

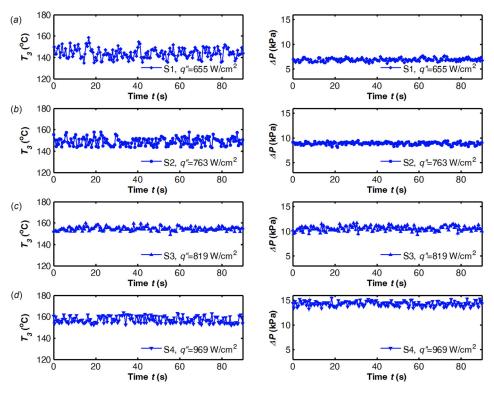


Fig. 6 Midpoint backside surface temperature  $T_3$  and pressure drop  $\Delta P$  fluctuations of the structured surface microchannels at CHF (the highest heat flux beyond which dry-out occurred). (a) Device S1 at  $q'=655\,\mathrm{W/cm^2}$ , (b) device S2 at  $q'=763\,\mathrm{W/cm^2}$ , (c) device S3 at  $q'=819\,\mathrm{W/cm^2}$ , and (d) device S4 at  $q''=969\,\mathrm{W/cm^2}$ . The mass flux  $G=300\,\mathrm{kg/m^2 \cdot s}$ . The uncertainties of the temperature and pressure drop measurement were approximately  $\pm 2\,^\circ\mathrm{C}$  and  $\pm 300\,\mathrm{Pa}$ .

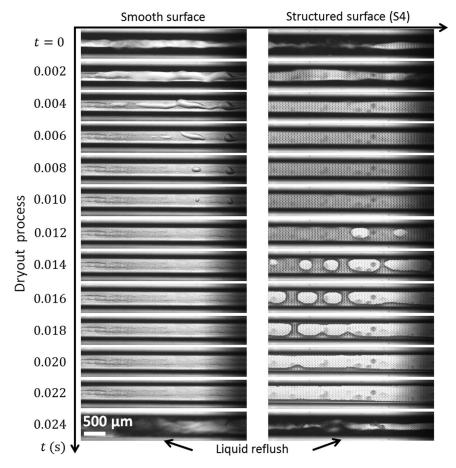


Fig. 7 Time-lapse images of the dynamic dry-out process on a smooth surface and on a structured surface (S4) captured by a high speed camera.  $q''=430\,\mathrm{W/cm^2}$  and  $G=300\,\mathrm{kg/m^2}$  s. The structured surface showed less dry-out spatially and temporally compared to the smooth surface due to wicking. Dry patches formed at the center of the channel which indicated wicking in the transverse direction (from the sidewalls inward). Wicking along the channel direction also existed since the dry patches formed earlier at downstream locations of the channel.

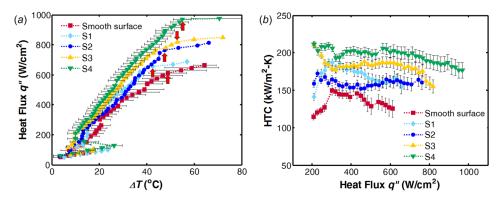


Fig. 8 The heat transfer performance characteristics of the microchannel. (a) The boiling curve (heat flux q'' versus heater temperature rise  $\Delta T$ ).  $\Delta T$  and q'' were calculated by Eqs. (2) and (4), respectively. The arrows indicate the CHF. (b) The HTC (calculated by Eq. (8)) as a function of q''. The error bars for q'' were approximately  $\pm 1\%$ . The error bars for  $\Delta T$  were approximately  $\pm 3.5\,^{\circ}$ C for the structured devices (shown for S4) and grew with the heat flux due to the increasing temperature oscillations ( $\pm 3.5\,^{\circ}$ C to  $\pm 11\,^{\circ}$ C) for the smooth surface.

microstructured surface devices (Table 1) and the smooth surface device investigated, as shown in Fig. 8(a) (i.e., the boiling curves). The y-axis intercept ( $\sim\!50\,\text{W/cm}^2$ ) at  $\Delta T = 0\,^\circ\text{C}$  was mainly due to the 10 $^\circ\text{C}$  subcooling, which agrees well with the estimated heat flux due to subcooling  $q''_{\text{subcooling}} = \dot{m}c_p\Delta T_{\text{subcooling}}/A_{\text{mc}} = 63\,\text{W/cm}^2$ . The low-slope in the curves at q'' below 150 W/cm² was due to

single phase heat transfer where the onset of nucleate boiling was indicated by the sudden drop in  $\Delta T$ . After the onset of nucleate boiling, the temperature rise increased with the heat flux.

The arrows in the boiling curves (Fig. 8(a)) indicate the CHF. The structured surface microchannels had a clear transition at CHF, which can be seen by the sudden drop in the boiling curve

slope after CHF. The time-resolved temperature and pressure drop were also very stable before and at CHF (Fig. 6). In contrast, the smooth surface microchannel had a less obvious transition to CHF, since periodic dry-out occurred much earlier on the boiling curve from  $q'' = 430 \, \text{W/cm}^2$ , as indicated by the temperature spikes (Fig. 5). The large error bars of  $\Delta T$  for the smooth surface devices at high heat fluxes were also due to the increasing temperature oscillations (Fig. 8(a)). This resulted in a higher time-averaged temperature rise under the same heat flux compared with the structured surface microchannels and thus a gradual decrease in the boiling curve slope. As the heat flux increased, flow instabilities (temperature spikes and pressure drop oscillations) developed to large amplitude periodic dry-out or constant dry-out (longer than 1 min).

The structured surface showed an enhanced CHF with a maximum value of  $969 \, \text{W/cm}^2$  at a corresponding vapor quality  $\chi$  of 0.29 achieved by device S4, which is a 57% enhancement compared with that of the smooth surface microchannel ( $615 \, \text{W/cm}^2$  at  $\chi = 0.19$ ). This CHF value is significant in comparison with similar studies in literature for a mass flux G of  $300 \, \text{kg/m}^2 \cdot \text{s}$ . The corresponding HTCs which were obtained from Fig. 8(a) and Eq. (8) are shown in Fig. 8(b). The structured surface microchannels showed significantly enhanced HTC even at heat fluxes close to CHF. This is due to the fact that evaporation is dominant in the annular flow, and the structures facilitate a stable liquid film and the menisci increased the thin film area. The HTC of the structured surface devices were relatively constant, which indicates that dry-out was minimized by the structures and the thermal resistance remained relatively unchanged.

3.3 Pressure Drop. The hydrodynamic characteristics of the microchannels were also studied since pumping penalties can limit implementation of the solution in flow boiling systems [4]. Figure 9 shows the measured time-averaged pressure drop as a function of heat flux q''. The pressure drops across all devices were similar, which indicates that the additional pressure drop introduced by the surface structures in this study were negligible. The maximum  $\Delta P$  was 14.3 kPa for device S4 at  $q'' = 969 \text{ W/cm}^2$  and  $G = 300 \text{ kg/m}^2 \cdot \text{s}$ , which resulted in a negligible pumping power of  $P_{\text{pump}} = Q\Delta P = 1 \text{ mW}$ , where Q is the volumetric flow rate (m³/s). This implies that the structures did not cost more pumping power while they maintained the temperature stability and enhanced heat transfer. This result is attributed to the liquid–vapor interface only forming menisci within the structures when there is insufficient liquid supply (Fig. 1(c)) which is usually

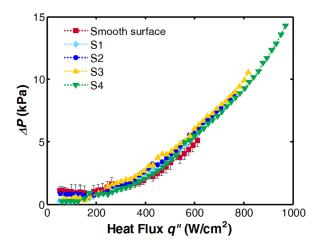


Fig. 9 Pressure drop across the microchannel as a function of heat flux for the devices investigated. The data were plotted until CHF. Error bars in pressure were approximately  $\pm 430\,\mathrm{Pa}$  (shown for the smooth surface microchannel), which were calculated from the STD of the temporal pressure measurement and the accuracy of the pressure transducers.

at the downstream section of the microchannel. In the devices tested, there was sufficient liquid supply upstream such that the majority of liquid was on top of the structures, and the structures only acted as surface roughness and did not introduce noticeable extra viscous pressure drop. In addition, wicking from the sidewalls to the center of the bottom surface as discussed in Sec. 3.1 did not contribute to the pressure drop along the microchannel direction.

**3.4 Wicking Model.** To further support our explanation for the role of the micropillar geometries in the wicking performance, we predicted the transverse liquid propagation flow rate (from the side walls to the center) in the micropillar arrays (Fig. 1(c)) using an adiabatic (no phase-change) wicking model developed by Xiao et al. [39]. The model solves the 1D Brinkman equation to obtain the liquid velocity in porous media. Details of the model framework are listed in the Appendix, which gives the velocity profile

$$u = Ae^{\alpha\sqrt{\varepsilon}y} + Be^{\alpha\sqrt{\varepsilon}y} - \frac{1}{\alpha^2\mu} \frac{dP}{dx}$$
 (9)

where u is the velocity, dP/dx is the pressure gradient which drives the liquid flow,  $\mu$  is the viscosity of the liquid,  $\varepsilon$  is the porosity of the micropillar arrays, and  $\alpha^{-2}$  is the permeability that accounts for the drag introduced by porous media, A and B are constants listed in Appendix.

To estimate the driving pressure gradient dP/dx in Eq. (9) in the transverse direction of the microchannel, we assume that (1) the dry-out location has the largest meniscus curvature k (i.e., minimum radius of curvature r = 1/k, Fig. 1(c)) since the liquid level is the lowest. Therefore the liquid pressure is the lowest at the dryout point based on the Young-Laplace equation  $(P_{\rm cap} = P_{\rm vapor})$  $-P_{\text{liquid}} = 2\sigma/r$ ; (2) at the dry-out location, the contact angle of water on silicon dioxide (pillar surface) is the receding contact angle  $\theta_r$  ( $\theta_r \approx 15 \text{ deg}$ ) [45]; (3) the pressure gradient is approximated as  $dP/dx = (P_{max} - P_{min})/L_w$ , where  $P_{max}$  is the maximum pressure along the wicking path which is at the sidewalls  $(P_{\text{max}} \approx P_{\text{vapor}})$  since the curvature is approximately zero,  $P_{\text{min}}$  is the pressure at the dry-out location  $(P_{\min} = P_{\text{vapor}} - 2\sigma/r)$ , and  $L_w$  is the wicking distance. From above,  $dP/dx = P_{\text{cap}}/L_w$ ; (4)  $P_{\text{cap}}$  is derived using a force balance on the liquid-vapor interface,  $P_{\text{cap}}(l^2 - 0.25\pi d^2) = \gamma \pi d \cos \theta_r$  [46,47]; (5) the longest wicking distance is from one sidewall to the other sidewall since dry-out can happen at random locations, and thus maximum  $L_w = W$ , where W is the width of the microchannel ( $W = 500 \,\mu\text{m}$ ). With these assumptions, we calculated the average liquid wicking velocity  $u_{\text{ave}}$  which is proportional to the flow rate of the wicking liquid film

$$u_{\text{ave}} = \frac{1}{h} \int_{y=0}^{y=h} u dy$$
 (10)

where the height h is fixed ( $h = 25 \mu m$ ). The result is shown in Fig. 10, where  $u_{ave}$  is plotted as a function of l and d. The geometries of the micropillars investigated in this study are also shown in symbols in Fig. 10 (devices S1–S4).

By comparing the results in Figs. 10 and 8(a), the microstructures that led to a higher liquid wicking velocity also had a higher CHF. This positive correlation between wicking velocity and CHF is expected based on our proposed mechanism, since efficient liquid transport helped sustain the thin film evaporation and prevent dry-out. Figure 10 also indicates that the wicking velocity depends both on the capillary pressure which creates the driving pressure gradient, and the viscous resistance, which hinders effective liquid propagation. Both terms depend on the structure geometry. Specifically, the capillary pressure approximately scales with 1/l, and the viscous drag scales with  $1/l^2$ , thus as l decreases the drag force increases faster than the driving capillary pressure. This is the reason device S1 has lower wicking velocity even

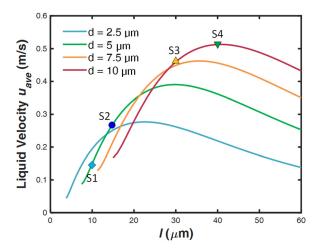


Fig. 10 The liquid wicking velocity  $u_{\rm ave}$  as a function of the diameters d and pitches I of the micropillars, when the height h is fixed ( $h = 25 \,\mu\mathrm{m}$ ).  $u_{\mathrm{ave}}$  is calculated by Eq. (10), and the magnitude of  $u_{ave}$  is proportional to the flow rate of the wicking liquid film in the pillar arrays. The symbols on the curves mark the locations of the geometries of the micropillars investigated in this study.

though it has higher capillary pressure (due to smaller spacing) compared to device S4 because the increased viscous resistance is more significant than the increase of the pressure gradient. In fact, the geometry of the structures can be further optimized to maximize the wicking capability, and hence enhance the flow stability and heat transfer.

While this wicking model explains the trends of our results, there are limitations. First, the effects of evaporation and the curved interfaces were not accounted for. A more detailed numerical model which takes these two factors into consideration can be found in Ref. [46]. In addition, this model cannot predict the liquid velocity along the channel direction due to the existence of vapor shear stress (i.e., an axially varying vapor pressure). This velocity in the axial direction is also important in determining the CHF in microchannels. A more comprehensive model which accounts for evaporation and wicking in both lateral and axial directions needs to be developed in the future to provide more detailed understanding of the role of surface structures on flow boiling.

#### Conclusions

We have demonstrated the design of a two-phase microchannel heat sink incorporated with micropillar arrays as a platform to study the effect of surface structures on flow boiling in microchannels. The design decouples thin film evaporation and nucleation by promoting capillary flow on the bottom heated surface while facilitating nucleation from the sidewalls. The structures reduced flow boiling instability significantly in the annular flow regime, and achieved very stable surface temperature and channel pressure drop even at high heat fluxes close to CHF. The smooth surface showed frequent temperature spikes and pressure drop fluctuations due to dry-out, which developed gradually to CHF. Visualization of the flow pattern and the dry-out process indicates that the micropillar surface can promote capillary flow and increase flow stability by maintaining a stable annular flow and highperformance thin film evaporation. This stabilized annular flow and thin film evaporation contributed to an enhanced HTC and CHF (maximum 57%) compared to a smooth surface microchannel. The pressure drop across all devices was similar, which indicates that the additional pressure drop introduced by the surface structures in this study was negligible. A liquid wicking model in the transverse direction of the channel was developed to explain the trend in the enhancement of CHF among the structured devices. Both the experimental results and the model suggest that capillary pressure can be maximized without introducing large viscous resistance when the microstructure geometry is optimized. A more comprehensive model that accounts for wicking in the microchannel axial direction will be developed in the future to aid in further understanding the role of surface structures on flow boiling. This work provides important insights into the role and promise of incorporating micropillar designs in high performance microchannel heat sinks.

## Acknowledgment

This work was partially funded by the Office of Naval Research (ONR) with Dr. Mark Spector as program manager (N00014-15-1-2483), the Cooperative Agreement between the Masdar Institute of Science and Technology (Masdar Institute), Abu Dhabi, UAE and the Massachusetts Institute of Technology (MIT), Cambridge, MA,—Reference 02/MI/MI/CP/11/07633/GEN/G/00, the Battelle Memorial Institute, the Air Force Office of Scientific Research (AFOSR) and the Singapore-MIT Alliance for Research and Technology (SMART). The research was technically supported and encouraged by the Jet Propulsion Laboratory, California Institute of Technology, under a contract with the National Aeronautics and Space Administration. The authors would also like to acknowledge the MIT Microsystems Technology Lab for fabrication staff support, help, and use of equipment.

#### Nomenclature

 $A_{\rm mc} =$  microchannel bottom wall surface area

 $c_p$  = specific heat of water

d = diameter of the micropillar

G =mass flux in the microchannel

h = height of the micropillar

I =input current from the power supply

k = curvature of the meniscus

l = pitch of the micropillar

 $L_c$  = length of the electrical connection resistance

 $L_w$  = wicking distance

 $L_{\text{heater}} = \text{length of the heater resistance}$ 

 $\dot{m} = \text{mass flow rate}$ 

 $P_{\rm cap} = {\rm capillary \ pressure}$ 

 $P_{\rm in}$  = microchannel inlet pressure

 $P_{\text{liquid}} = \text{liquid pressure}$ 

 $P_{\rm loss}^{-}$  = calibrated heat loss to the environment

 $P_{\text{out}} = \text{microchannel outlet pressure}$ 

 $P_{\text{pump}} = \text{pumping power}$ 

 $P_{\rm sat} = {\rm saturation \, pressure}$ 

 $P_{\rm vapor} = {\rm vapor} \, {\rm pressure}$ 

 $P_{\text{water,res}}$  = pressure of the water in the reservoir

Q = volumetric flow rate

q'' = heat flux

 $q''_{\text{subcooling}}$  = heat flux due to subcooling

r =radius of curvature

R = electrical resistance

 $R_c$  = electrical connection resistance

 $R_{\text{total}} = \text{total heater resistance}$  $R^2 = \text{coefficient of determination}$ 

 $T_{\text{ave}}$  = average microchannel backside surface temperature

 $T_{\rm sat}$  = saturation temperature

 $T_{\text{water,res}} = \text{temperature of the water in the reservoir}$ 

 $T_1$  = temperature measured by RTD1

 $T_2$  = temperature measured by RTD2

 $T_3$  = temperature measured by RTD3

 $T_4$  = temperature measured by RTD4

u = velocity

U = input voltage from the power supply

 $u_{\text{ave}} = \text{average velocity}$ 

W =width of the microchannel

 $W_c$  = width of the electrical connection resistance

 $W_{\text{heater}} = \text{width of the heater resistance}$ 

x =distance to the inlet of the microchannel

= permeability

 $\Delta P$  = pressure drop across the microchannel

 $\Delta R$  = electrical resistance change

 $\Delta T$  = temperature rise/temperature change

 $\Delta T_{\rm subcooling} = {\rm subcooling}$ 

 $\varepsilon$  = porosity of micropillar arrays

 $\theta_r$  = receding contact angle

 $\mu = viscosity$ 

 $\sigma = \text{surface tension}$ 

 $\chi = \text{vapor quality}$ 

## **Appendix**

## Time Required to Reach Steady-State

We determined that the time of at least 1 min was needed to reach the steady-state as the heat flux was incremented by  $\sim 20 \,\mathrm{W/cm^2}$ . This was based on our experimental observation where we constantly monitored the device temperature and pressure. A typical temperature response as the heat flux was incremented is shown in Fig. 11 (Sample S2). We measured the steady-state temperature for  $\sim$ 5 min and the average temperature was constant (no further rise was observed). This fast response is due to the small thermal mass of our device (1 mm thick silicon of 1 cm  $\times$  3 cm area) and a small temperature rise of  $\sim 1-2$  °C (shown in the boiling curve, Fig. 8) associated with a small increment of heat flux ( $\sim 20 \text{ W/cm}^2$ ). In addition, our flow loop was optimized to have minimal influence on the rise time of the microchannel: the inlet water temperature and flow rate were kept constant, and the flow exiting the microchannel directly entered the constant pressure water reservoir ( $\sim$ 1 liter, 1 atm).

## **Temperature and Pressure Variation Along the** Microchannel

Figure 12(a) shows the measured backside temperature at the inlet  $(T_1, T_2)$ , the midpoint  $(T_3)$  and the outlet  $(T_4)$  of the microchannel (Sample S4,  $q = 618 \text{ W/cm}^2$ ). The inlet temperature was close to the saturation temperature, and the midpoint temperature was the highest among the four measured temperatures. The outlet temperature was lower than the midpoint temperature. Figure 12(b) shows the inlet and outlet pressure, and the corresponding fluid saturation temperature. Since the device did not have temperature sensors on the microchannel inner wall surface, we were not able to measure the temperature at the channel wall

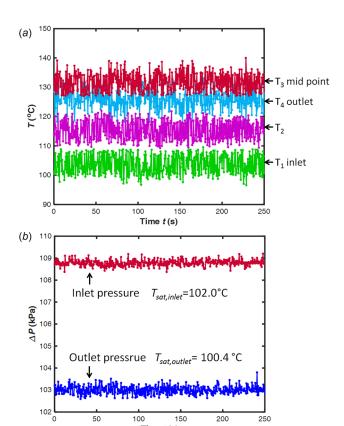


Fig. 12 (a) Measured backside temperature at the inlet  $(T_1, T_2)$ , the midpoint  $(T_3)$ , and the outlet  $(T_4)$  of the microchannel (Sample S4,  $q = 618 \text{ W/cm}^2$ ). (b) The inlet and outlet pressure, and the corresponding fluid saturation temperature.

(the solid-liquid interface). We did not estimate the wall temperature based on the backside temperature due to complex heat spreading in the substrate to the channel bottom surface and to the side walls of the microchannel.

## Wicking Model

The model by Xiao et al. [39] minimizes surface energy to predict the equilibrium liquid-vapor interface meniscus shape and thus the capillary pressure generated by the pillar arrays. The

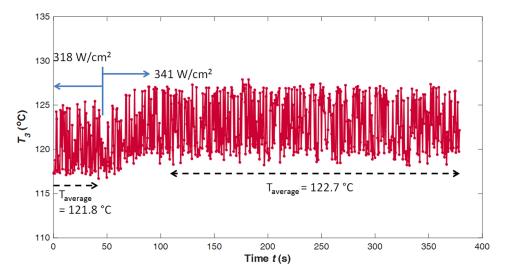


Fig. 11 Midpoint microchannel backside temperature  $T_3$  for sample S2. At t = 45 s the heat flux was increased to 341 W/cm<sup>2</sup>.

liquid velocity profile was analytically solved using the onedimensional form of the Brinkman equation [48] as shown in Eq. (A1), which is a modified form of the Navier–Stokes equation including a Darcy term to study flow through porous media

$$\mu \frac{d^2 u}{dv^2} - \varepsilon \frac{dP}{dx} - \mu \alpha^2 \varepsilon u = 0 \tag{A1}$$

In Eq. (A1), u is the velocity, dP/dx is the pressure gradient which drives the liquid flow,  $\mu$  is the viscosity of the liquid,  $\varepsilon$  is the porosity of the micropillar arrays, and  $\alpha^{-2}$  is the permeability that accounts for the drag introduced by porous media. The micropillars were regarded as porous media with permeability numerically studied by Sangani and Acrivos [49], and the expression is given by

$$a^{-2} = l^2 \frac{\ln c^{-1/2} - 0.738 + c - 0.887c^2 + 2.038c^3 + O(c^4)}{4\pi}$$
(A2)

where  $c = \pi d^2/4l^2$  is the solid fraction. We assume no slip boundary condition (u=0) at y=0 (bottom surface) and a shear free boundary condition at the pillar tops  $(\mathrm{d}u/\mathrm{d}y=0)$  at  $y=h=25\,\mu\mathrm{m}$ , where h is the height of the pillars). Since we only model the wicking process in the cross-sectional plane (from the sidewalls inward), it is reasonable to neglect shear at y=h in the lateral direction, since the shear force is mainly along the channel direction due to the vapor flow.

With the boundary conditions, the velocity field is expressed as Eq. (9) [39], where the constants A and B in Eq. (9) are

$$A = \frac{dP/dx \exp(-\alpha h\sqrt{\varepsilon})}{\alpha^2 \mu \left[\exp(\alpha h\sqrt{\varepsilon}) + \exp(-\alpha h\sqrt{\varepsilon})\right]}$$
 (A3)

$$B = \frac{dP/dx \exp(\alpha h \sqrt{\varepsilon})}{\alpha^2 \mu \left[\exp(\alpha h \sqrt{\varepsilon}) + \exp(-\alpha h \sqrt{\varepsilon})\right]}$$
(A4)

#### References

- Pop, E., 2010, "Energy Dissipation and Transport in Nanoscale Devices," Nano Res., 3(3), pp. 147–169.
- [2] Thome, J. R., 2006, 'The New Frontier in Heat Transfer: Microscale and Nanoscale Technologies,' Heat Transfer Eng., 27(9), pp. 1–3.
- [3] Krishnan, S., Garimella, S. V., Chrysler, G. M., and Mahajan, R. V., 2007, "Towards a Thermal Moore's Law," IEEE Trans. Adv. Packag., 30(3), pp. 462–474.
  [4] Kandlikar, S. G., 2002, "Fundamental Issues Related to Flow Boiling in Mini-
- [4] Kandlikar, S. G., 2002, "Fundamental Issues Related to Flow Boiling in Minichannels and Microchannels," Exp. Therm. Fluid Sci., 26(2–4), pp. 389–407.
- [5] Das, P. K., Chakraborty, S., and Bhaduri, S., 2012, "Critical Heat Flux During Flow Boiling in Mini and Microchannel-A State of the Art Review," Front. Heat Mass Transfer, 3(1), p. 013008.
- [6] Bergles, A. E., Lienhard, V. J. H., Kendall, G. E., and Griffith, P., 2003, "Boiling and Evaporation in Small Diameter Channels," Heat Transfer Eng., 24(1), pp. 18–40.
- [7] Hetsroni, G., Mosyak, A., Pogrebnyak, E., and Segal, Z., 2005, "Explosive Boiling of Water in Parallel Micro-Channels," Int. J. Multiphase Flow, 31(4), pp. 371–392.
- [8] Zhang, T., Peles, Y., Wen, J. T., Tong, T., Chang, J.-Y., Prasher, R., and Jensen, M. K., 2010, "Analysis and Active Control of Pressure-Drop Flow Instabilities in Boiling Microchannel Systems," Int. J. Heat Mass Transfer, 53(11–12), pp. 2347–2360.
- [9] Zhang, T., Tong, T., Chang, J.-Y., Peles, Y., Prasher, R., Jensen, M. K., Wen, J. T., and Phelan, P., 2009, "Ledinegg Instability in Microchannels," Int. J. Heat Mass Transfer, 52(25–26), pp. 5661–5674.
- [10] Yadigaroglu, G., and Bergles, A. E., 1972, "Fundamental and Higher-Mode Density-Wave Oscillations in Two-Phase Flow," ASME J. Heat Transfer, 94(2), pp. 189–195.
- [11] Bergles, A. E., and Kandlikar, S. G., 2005, "On the Nature of Critical Heat Flux in Microchannels," ASME J. Heat Transfer, 127(1), pp. 101–107.
  [12] Koşar, A., Kuo, C.-J., and Peles, Y., 2005, "Suppression of Boiling Flow Oscil-
- [12] Koşar, A., Kuo, C.-J., and Peles, Y., 2005, "Suppression of Boiling Flow Oscillations in Parallel Microchannels by Inlet Restrictors," ASME J. Heat Transfer, 128(3), pp. 251–260.
- [13] Wang, G., Cheng, P., and Bergles, A. E., 2008, "Effects of Inlet/Outlet Configurations on Flow Boiling Instability in Parallel Microchannels," Int. J. Heat Mass Transfer, 51(9–10), pp. 2267–2281.

- [14] Kandlikar, S. G., Kuan, W. K., Willistein, D. A., and Borrelli, J., 2005, "Stabilization of Flow Boiling in Microchannels Using Pressure Drop Elements and Fabricated Nucleation Sites," ASME J. Heat Transfer, 128(4), pp. 389–396.
- [15] Koşar, A., Kuo, C.-J., and Peles, Y., 2005, "Boiling Heat Transfer in Rectangular Microchannels With Reentrant Cavities," Int. J. Heat Mass Transfer, 48(23–24), pp. 4867–4886.
- [16] David, M. P., Steinbrenner, J. E., Miler, J., and Goodson, K. E., 2011, "Adiabatic and Diabatic Two-Phase Venting Flow in a Microchannel," Int. J. Multiphase Flow, 37(9), pp. 1135–1146.
- [17] Alexander, B. R., and Wang, E. N., 2009, "Design of a Microbreather for Two-Phase Microchannel Heat Sinks," Nanoscale Microscale Thermophys. Eng., 13(3), pp. 151–164.
- [18] Fazeli, A., Mortazavi, M., and Moghaddam, S., 2015, "Hierarchical Biphilic Micro/Nanostructures for a New Generation Phase-Change Heat Sink," Appl. Therm. Eng., 78, pp. 380–386.
- [19] Koşar, A., and Peles, Y., 2007, "Boiling Heat Transfer in a Hydrofoil-Based Micro Pin Fin Heat Sink," Int. J. Heat Mass Transfer, 50(5-6), pp. 1018-1034.
- [20] Wang, Y., and Peles, Y., 2015, "Subcooled Flow Boiling in a Microchannel With a Pin Fin and a Liquid Jet in Crossflow," Int. J. Heat Mass Transfer, 86, pp. 165–173.
- [21] Woodcock, C., Yu, X., Plawsky, J., and Peles, Y., 2015, "Piranha Pin Fin (PPF)—Advanced Flow Boiling Microstructures With Low Surface Tension Dielectric Fluids," Int. J. Heat Mass Transfer, 90, pp. 591–604.
- [22] Li, D., Wu, G. S., Wang, W., Wang, Y. D., Liu, D., Zhang, D. C., Chen, Y. F., Peterson, G. P., and Yang, R., 2012, "Enhancing Flow Boiling Heat Transfer in Microchannels for Thermal Management With Monolithically-Integrated Silicon Nanowires," Nano Lett., 12(7), pp. 3385–3390.
- [23] Yang, F., Dai, X., Peles, Y., Cheng, P., Khan, J., and Li, C., 2014, "Flow Boiling Phenomena in a Single Annular Flow Regime in Microchannels (I): Characterization of Flow Boiling Heat Transfer," Int. J. Heat Mass Transfer, 68, pp. 703–715.
- [24] Yang, F., Dai, X., Peles, Y., Cheng, P., Khan, J., and Li, C., 2014, "Flow Boiling Phenomena in a Single Annular Flow Regime in Microchannels (II): Reduced Pressure Drop and Enhanced Critical Heat Flux," Int. J. Heat Mass Transfer, 68, pp. 716–724.
- [25] Dhir, V. K., 1998, "Boiling Heat Transfer," Annu. Rev. Fluid Mech., 30(1), pp. 365–401.
- [26] Chen, R., Lu, M.-C., Srinivasan, V., Wang, Z., Cho, H. H., and Majumdar, A., 2009, "Nanowires for Enhanced Boiling Heat Transfer," Nano Lett., 9(2), pp. 548–553.
- [27] Li, C., Wang, Z., Wang, P.-I., Peles, Y., Koratkar, N., and Peterson, G. P., 2008, "Nanostructured Copper Interfaces for Enhanced Boiling," Small, 4(8), pp. 1084–1088.
- [28] Ahn, H. S., Jo, H. J., Kang, S. H., and Kim, M. H., 2011, "Effect of Liquid Spreading Due to Nano/Microstructures on the Critical Heat Flux During Pool Boiling," Appl. Phys. Lett., 98(7), p. 071908.
- [29] Rahman, M. M., Ölçeroğlu, E., and McCarthy, M., 2014, "Role of Wickability on the Critical Heat Flux of Structured Superhydrophilic Surfaces," Langmuir, 30(37), pp. 11225–11234.
- [30] Chu, K.-H., Enright, R., and Wang, E. N., 2012, "Structured Surfaces for Enhanced Pool Boiling Heat Transfer," Appl. Phys. Lett., 100(24), p. 241603.
  [31] Chu, K.-H., Joung, Y. S., Enright, R., Buie, C. R., and Wang, E. N., 2013,
- [31] Chu, K.-H., Joung, Y. S., Enright, R., Buie, C. R., and Wang, E. N., 2013, "Hierarchically Structured Surfaces for Boiling Critical Heat Flux Enhancement," Appl. Phys. Lett., 102(15), p. 151602.
- [32] Betz, A. R., Jenkins, J., Kim, C.-J. "CJ," and Attinger, D., 2013, "Boiling Heat Transfer on Superhydrophilic, Superhydrophobic, and Superbiphilic Surfaces," Int. J. Heat Mass Transfer, 57(2), pp. 733–741.
- [33] Betz, A. R., Xu, J., Qiu, H., and Altinger, D., 2010, "Do Surfaces With Mixed Hydrophilic and Hydrophobic Areas Enhance Pool Boiling?," Appl. Phys. Lett., 97(14), p. 141909.
- [34] Shin, S., Choi, G., Kim, B. S., and Cho, H. H., 2014, "Flow Boiling Heat Transfer on Nanowire-Coated Surfaces With Highly Wetting Liquid," Energy, 76, pp. 428–435.
- [35] Kleinstreuer, C., and Koo, J., 2004, "Computational Analysis of Wall Roughness Effects for Liquid Flow in Micro-Conduits," ASME J. Fluids Eng., 126(1), pp. 1–9.
- [36] Bahrami, M., Yovanovich, M. M., and Culham, J. R., 2005, "Pressure Drop of Fully Developed, Laminar Flow in Rough Microtubes," ASME J. Fluids Eng., 128(3), pp. 632–637.
- [37] Hsu, Y. Y., 1962, "On the Size Range of Active Nucleation Cavities on a Heating Surface," ASME J. Heat Transfer, 84(3), pp. 207–213.
- [38] Carey, V. P., 2007, Liquid Vapor Phase Change Phenomena: An Introduction to the Thermophysics of Vaporization and Condensation Processes in Heat Transfer Equipment, 2nd ed., Taylor & Francis, Abingdon, UK.
- [39] Xiao, R., Enright, R., and Wang, E. N., 2010, "Prediction and Optimization of Liquid Propagation in Micropillar Arrays," Langmuir, 26(19), pp. 15070–15075.
- [40] Rao, S. R., and Peles, Y., 2015, "Spatiotemporally Resolved Heat Transfer Measurements for Flow Boiling in Microchannels," Int. J. Heat Mass Transfer, 89, pp. 482–493.
- [41] Rao, S. R., Houshmand, F., and Peles, Y., 2014, "Transient Flow Boiling Heat-Transfer Measurements in Microdomains," Int. J. Heat Mass Transfer, 76, pp. 317–329.
- [42] Lemmon, E. W., Huber, M. L., and McLinden, M. O., 2013, "NIST Standard Reference Database 23," National Institute of Standards and Technology, Gaithersburg, MD.

- [43] Kuo, C.-J., and Peles, Y., 2008, "Flow Boiling Instabilities in Microchannels and Means for Mitigation by Reentrant Cavities," ASME J. Heat Transfer, 130(7), p. 072402.
  [44] Wu, H. Y., and Cheng, P., 2003, "Visualization and Measurements of Periodic Boiling in Silicon Microchannels," Int. J. Heat Mass Transfer, 46(14), pp. 2603–2614.
  [45] Raj, R., Maroo, S. C., and Wang, E. N., 2013, "Wettability of Graphene," Nano
- Lett., **13**(4), pp. 1509–1515.
- [46] Zhu, Y., Antao, D. S., Lu, Z., Somasundaram, S., Zhang, T., and Wang, E. N., 2016, "Prediction and Characterization of Dry-Out Heat Flux in Micropillar Wick Structures," Langmuir, 32(7), pp. 1920–1927.

- [49] Sangani, A. S., and Acrivos, A., 1982, "Slow Flow Past Periodic Arrays of Cylinders With Application to Heat Transfer," Int. J. Multiphase Flow, 8(3), pp. 193-206.