

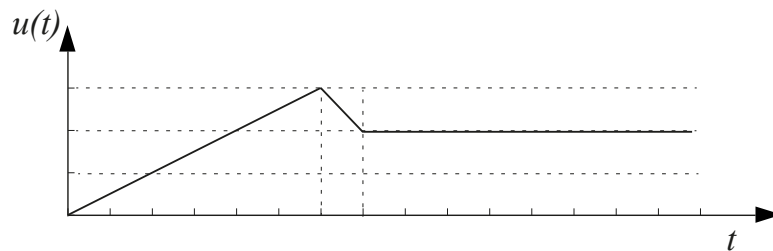
1. **(20 points)** A dynamical system is given by its step response:

$$y(t) = 0.25 - 0.25e^{-t} \cos \sqrt{3} t + 0.25\sqrt{3}e^{-t} \sin \sqrt{3} t, \quad t \geq 0$$

- Calculate the transfer function of the system.
 - Calculate the static gain, the natural frequency, the damping factor and the time constant(s) of the system.
 - Calculate and sketch the impulse response of this system.
2. **(20 points)** Consider the following dynamical system

$$y^{(i)}(t) + 2y(t) = u(t)$$

with $y(t)$ being the output and $u(t)$ the input of the system. If $u(t)$ given in the figure below (one tick represents one unit) is applied to the system:



- Calculate the Laplace transform of the input signal.
- Calculate the time response of the system.
- What is the final value of the response obtained in b)?
- Calculate and sketch the *step response* of this system for the initial condition $y(0) = -0.5$.