## Statistical Inference

© 2024, A. C. Davison

Ecole Polytechnique Fédérale de Lausanne EPFL-FSB-MATH-STAT Station 8, 1015 Lausanne, Switzerland http://stat.epfl.ch

Everything below is approximate. Please signal any corrections to Anthony.Davison@epfl.ch.

## Course web page

Further material, links to data sets, etc., can be found on the course moodle page.

## Lecture contents

- 1. Introduction, Probability revision I (12/9/24; 1–19)
  - Introduction. Probability: basic ideas, Bayes' theorem, random variables, conditional and marginal distributions, exchangeability (1–14)
  - Order statistics; moments and conditional moments; multivariate normal distribution; MGFs and KGFs. (15–19)
- 2. Probability revision II (19/9/24; 20–29)
  - Exponential tilting and exponential families. (19–23)
  - Convergence and delta method. Statistics revision: tasks and models. I. (24–29)
- 3. Statistics revision (26/9/24; 30–38)
  - Model formulation. Point estimation: some types of estimator (ML, moments, score-matching). (30–34)
  - Properties of point estimators: consistency, MSE, bias, variance. Bartlett identities. (35–38, not 37)
- 4. Statistics revision (3/10/24; 37-44)
  - CRLB and Fisher information. Efficient estimation. (36–38)
  - Interval estimation. Pivots. Confidence and prediction intervals. (39–44)
- 5. Statistics revision (10/10/24; 45-58)
  - Hypothesis testing. Bases for inference: sampling theory. (44–49)
  - Bases for inference: Bayes' theorem; randomisation. (50–58)
- 6. Basic notions (17/10/24; 59-76)
  - Likelihood and basic properties. Complications: selection. (59–70)
  - Complications: censoring, dependent data, missing data. (71–76)

- 7. Basic notions (31/10/24; 77-82)
  - Sufficiency, minimal sufficiency. Factorisation theorem. (77–79)
  - Rao-Blackwell theorem. Completeness. (80-81)
- 8. Basic notions (7/11/24; 83-98)
  - Eliminating nuisance parameters. Conditioning and ancillary statistics. (83–85)
  - Inference. Likelihood: generalities, consistency (86–98)
- 9. Likelihood theory II (14/11/24; slides 99–112)
  - Asymptotic normality of MLE. Classical regularity conditions, related statistics, exponential example (99–100)
  - Non-regular models. Vector case, profile log likelihood (101–112).
- 10. Likelihood theory III (21/11/24; slides 113–125)
  - Model selection. Nuisance parameters: modified profile likelihood, higher-order asymptotics (112–117)
  - Orthogonal parameters. Composite likelihood. (118–125)
- 11. Significance tests (28/11/24; slides 126–142)
  - Pure significance tests. Uniformity of P-value. Exact and inexact tests. (126–133)
  - Neyman–Pearson approach. Critical regions, size, power and the ROC curve. NP lemma. (134–142)
- 12. Multiple testing (5/12/24; slides 142-153)
  - Optimal test in exponential family. Local power and score tests. Comments/discussion of testing. (142–146)
  - Multiple testing, graphical methods. Error control. Bonferroni procedures. False discovery rate, Benjamini–Hochberg procedure. (147–155)
- 13. Testing. Selection. Bootstrap (12/12/24; slides 156–168)
  - Recap. Proof of BH procedure. Final comments. Selection generalities. (155–162)
  - Sample splitting; randomisation. Bootstrap intro. (163–168)
- 14. Bootstrap inference (19/12/24; slides 169–205)
  - Bootstrap simulation (169–187)
  - Bootstrap confidence intervals. Nonparametric delta method (187–205)