## **Lecture III**

# **Enzyme Kinetics Exercise**

#### PROBLEM 1:

An enzymatic assay was carried under two different sets of conditions out using a pure substrate S. The results are tabulated below.

[S], mM	Va, mM/s	V <sub>b</sub> , mM/s
1.5	0.21	0.08
2.0	0.25	0.1
3.0	0.28	0.12
4.0	0.33	0.13
8.0	0.44	0.16
16.0	0.40	0.18

- a. Plot the data using the Lineweaver-Burke plot
- b. Calculate the values of  $V_{\text{max}}$  and  $K_{\text{m}}$  for both sets of conditions, starting from the Michaelis-Menten equation.
- c. Suggest possible reasons why the two sets of results might be different.

### **PROBLEM 2:**

An enzyme catalyzed reaction of the form  $S \leftrightarrow P$ 

Has a  $\Delta G^{\circ}$  value of 3.4 kJ mol<sup>-1</sup>. Calculate the equilibrium constant for the enzymatic process at 298 K (Universal Gas constant R = 8.314 J mol<sup>-1</sup>K<sup>-1</sup>).

## **Exercises on DNA/DNA pairing and bond energy**

This table presents the thermodynamic nearest neighbor (NN) parameters for Watson-Crick base pairs in 1 M NaCl.

**TABLE 1** Nearest-neighbor thermodynamic parameters for DNA Watson-Crick pairs in 1 M NaCl<sup>a</sup>

Propagation sequence	$\Delta H^{\circ}$ (kcal mol $^{-1}$ )	ΔS° (e.u.)	$\begin{array}{c} \Delta G_{37}^{\circ} \\ (kcal\ mol^{-1}) \end{array}$
AA/TT	-7.6	-21.3	-1.00
AT/TA	-7.2	-20.4	-0.88
TA/AT	-7.2	-21.3	-0.58
CA/GT	-8.5	-22.7	-1.45
GT/CA	-8.4	-22.4	-1.44
CT/GA	-7.8	-21.0	-1.28
GA/CT	-8.2	-22.2	-1.30
CG/GC	-10.6	-27.2	-2.17
GC/CG	-9.8	-24.4	-2.24
GG/CC	-8.0	-19.9	-1.84
Initiation	+0.2	-5.7	+1.96
Terminal AT penalty	+2.2	+6.9	+0.05
Symmetry correction	0.0	-1.4	+0.43

<sup>&</sup>lt;sup>a</sup>The slash indicates the sequences are given in antiparallel orientation. (e.g., AC/TG means 5'-AC-3' is Watson-Crick base paired with 3'-TG-5'). The symmetry correction applies to only self-complementary duplexes. The terminal AT penalty is applied for each end of a duplex that has a terminal AT (a duplex with both end closed by AT pairs would have a penalty of +0.1 kcal/mol for  $\Delta G_{37}^3$ ).

The following equation is used to predict the  $\Delta G_T^0$  at a different temperature, T:

$$\Delta G_T^0 = \Delta H^0 - T \Delta S^0$$

where T is in Kelvin,  $\Delta H^0$  is in cal/mol, and  $\Delta S^0$  is in units of  $cal/K \cdot mol$  (entropy units, e.u.).  $\Delta H^0$  and  $\Delta S^0$  are assumed to be temperature independent; this is an excellent approximation for nucleic acids.

### The NN Model.

The NN model for nucleic acids assumes that the stability of a given base pair depends on the identity and orientation of neighboring base pairs.

According to this model, the total  $\Delta G^0_{Total(37)}$  is given by:

$$\Delta G_{Total(37)}^{0} = \sum_{i} n_{i} \Delta G^{0}(i) + \Delta G^{0}(init\ w/term\ G \cdot C) + \Delta G^{0}(init\ w/term\ A \cdot T) + \Delta G^{0}(sym)$$

where  $\Delta G^0(i)$  are the standard free-energy changes for the 10 possible Watson–Crick NNs (Table 1),  $n_i$  is the number of occurrences of each nearest neighbor (*i.e.* the number of pairs), i, and  $\Delta G^0(sym)$  equals +0.43 kcal/mol (1cal =4.184J) if the duplex is self-complementary and zero if it is non-self-complementary.

#### Prediction of the Melting Temperature T<sub>M</sub>.

 $T_M$  is defined as the temperature at which half of the strands are in the double-helical state and half are in the "random-coil" state. The  $T_M$  is calculated from the predicted  $\Delta H^0$  and  $\Delta S^0$ , and the total oligonucleotide strand concentration  $C_T$ , by using the equation:

$$T_{M} = \frac{\Delta H^{0}}{\Delta S^{0} + R \ln C_{T}}$$

where R is the gas constant (1.987  $cal/K \cdot mol$ ).

To compute the T<sub>M</sub> in Celsius degree: 
$$T_{M}=\frac{\Delta H^{0}\cdot 1000}{\Delta S^{0}+R\ln C_{T}}-273.15$$
 where  $\Delta H^{0}$  is given in cal/mol

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### PROBLEM 1

Calculate the  $\Delta G^0_{Total(37)}$  and  ${\rm T_M}$  for the sequence CGTTGA-TCAACG using the NN model. Consider a total strand concentration of 0.4mM.

### PROBLEM 2

Calculate the TM for a non self-complementary duplex with  $\Delta H^0_{Total(37)} = -45.5 \textit{kcal/mol},$  $\Delta S_{\text{Total}(37)}^0 = -132.5 \, e. \, u.$ , and a strand concentration of 0.2mM for each strand.

### **Internal Single Mismatches**

The nearest-neighbor model can be extended beyond the Watson-Crick pairs to include parameters for interactions between mismatches and neighboring base pairs. Table 2 provides the complete thermodynamic database for internal single mismatches.

TABLE 2 Nearest-neighbor  $\Delta G_{37}^\circ$  increments (kcal mol $^{-1}$ ) for internal single mismatches next to Watson-Crick pairs in 1 M NaCla

Propagation		Y			
sequence	X	A	C	G	T
GX/CY	A	0.17	0.81	-0.25	WC
	C	0.47	0.79	WC	0.62
	G	-0.52	WC	-1.11	0.08
	T	WC	0.98	-0.59	0.45
CX/GY	A	0.43	0.75	0.03	WC
	C	0.79	0.70	WC	0.62
	G	0.11	WC	-0.11	-0.47
	T	WC	0.40	-0.32	-0.12
AX/TY	Α	0.61	0.88	0.14	WC
	C	0.77	1.33	WC	0.64
	G	0.02	WC	-0.13	0.71
	T	WC	0.73	0.07	0.69
TX/AY	A	0.69	0.92	0.42	WC
	C	1.33	1.05	WC	0.97
	G	0.74	WC	0.44	0.43
	T	WC	0.75	0.34	0.68

 $<sup>^</sup>aWC$  indicates a Watson-Crick pair, which is given in Table 1. Error bars and  $\Delta H^o$  and  $\Delta S^o$  parameters are provided in the original references.

### **PROBLEM 3**

Calculate the  $\Delta G^0_{Total(37)}$  for the sequence GGACTGACG-CCTGGCTGC (the underlined residues are mismatched) using the NN model.

# Exercises on Antibody/Antigen affinity and bond energy

If a monovalent antibody fragment is used for analysis, the equilibrium of antigen-antibody binding is defined as:

$$Antibody + Antigen \stackrel{K_a}{\Leftrightarrow} Complex$$

where

$$K_a = \frac{[Complex]}{[Antibody][Antigen]}$$

Association and dissociation rate constants are defined as follows:

$$\begin{aligned} v_{ass} &= k_{ass} [Antibody] [Antigen] \\ v_{diss} &= k_{diss} [Complex] \end{aligned}$$

where  $v_{ass}$  and  $v_{diss}$  represent the rates of association and dissociation, respectively, and  $k_{ass}$  and  $k_{diss}$  represent the rate constants of association and dissociation, respectively. At equilibrium  $v_{ass}$  is equal to  $v_{diss}$  and the following equation is obtained:

$$K_a = \frac{k_{ass}}{k_{diss}}$$

The Gibbs' energy of formation ( $\Delta G_0$ ) of an antigen—antibody complex is given by:

$$\Delta G_0 = -RT \ln K_a$$

where R is the gas constant (1.987 cal/molK) and T is temperature.

The free energy of complex formation represents a balance between enthalpic ( $\Delta H_0$ ) and entropic ( $\Delta S_0$ ) forces as defined by the equation:

$$\Delta G_0 = \Delta H_0 - T \Delta S_0$$

In general, antigens and antibodies in solution have to overcome large entropic barriers before they can form a tight binding.

#### **PROBLEM 1**

For the following Antigen/antibody couples, calculate the  $K_a$  and the Gibbs' energy of formation (at 298K).

Ab/Ag pair	K <sub>ass</sub> (M <sup>-1</sup> s <sup>-1</sup> )	K <sub>diss</sub> (s <sup>-1</sup> )	K <sub>a</sub> (M <sup>-1</sup> )	$\Delta G_0$ (kcal/molM)
1	8.68 x10 <sup>-5</sup>	1.84 x10 <sup>-4</sup>		
2	2.38 x10 <sup>-6</sup>	2.21 x10 <sup>-4</sup>		
3	3.72 x10 <sup>-4</sup>	2.93 x10 <sup>-4</sup>		
4	6.15 x10 <sup>-5</sup>	2.33 x10 <sup>-4</sup>		