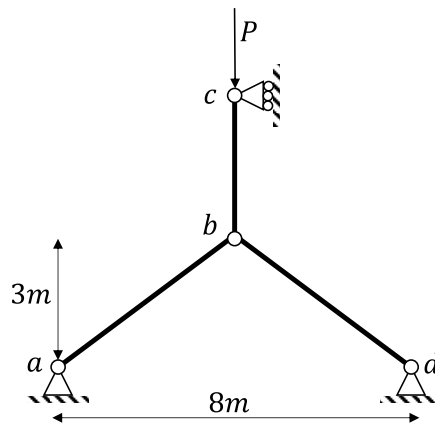


In-class Exercise Week #6: Load-displacement constraint methods

Exercise #1:

Consider the following truss structure:



The members have the following properties:

- ab : $E = 200 \text{ GPa}$, $l_{o,ab} = 5\text{m}$, square cross section of width $b_{ab} = 500\text{mm}$
- bc : $E = 200 \text{ GPa}$, $l_{o,bc} = l_{o,ab}$, square cross section of width b_{bc}
- bd : $E = 200 \text{ GPa}$, $l_{o,bd} = l_{o,ab}$, square cross section of width $b_{bd} = b_{ab}$

1) Determine analytically the minimum dimension $b_{c_{min}}$ such that the structure does not exhibit a snap-back response in the $P - v_c$ equilibrium path (v_c denotes the vertical displacement of node c).

Hint: Consider the tangent in the $P - v_c$ equilibrium path once members ab and bd are horizontal (i.e., when $P = 0$).

2) Derive the corotational formulation for a 2d truss element

3) Model the structure using 2d truss elements and simulate the response of the structure in the case where node c is displaced vertically up to $v_c = 4.0\text{m}$ downwards:

- a) Using displacement control for $b_{bc} = 2 \cdot b_{ab}$
- b) Using arc-length control for $b_{bd} = b_{ab}/2$