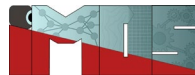


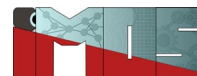
Machine Learning for Predictive Maintenance Applications: Hybrid Models / Graph Neural Networks

Prof. Dr. Olga Fink

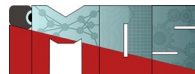
November 2024



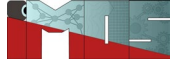
- Domain generalization focuses on training models that generalize to unseen target domains.
- Unlike domain adaptation, it does not require access to target domain data during training.
- It aims to learn robust and invariant features from source domains that perform well under different conditions.
- Useful when target environments are unknown or change dynamically.
- Helps create models that are more adaptable and resilient to distribution shifts or novel scenarios.



- Continuous domain adaptation focuses on adapting a model continuously as the target domain evolves over time.
- Unlike traditional domain adaptation, it handles scenarios where data distributions change dynamically and require ongoing adjustments.
- It seeks to maintain model performance by adapting incrementally to new conditions without needing to retrain from scratch.
- Useful for real-world applications where environments and data distributions are constantly shifting.
- Often involves strategies for updating learned representations, retaining past knowledge, and mitigating catastrophic forgetting.

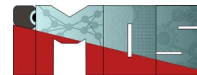


- Test-time adaptation refers to adapting a model to distribution shifts in the target domain during inference, without further training on the source domain.
- It focuses on updating model parameters or representations using only test data, typically through self-supervised or unsupervised strategies.
- Allows models to respond to domain shifts or changes at the point of inference, improving performance in unseen or evolving conditions.
- Reduces the reliance on having a large amount of labeled data in the target domain.
- Useful for scenarios where models encounter dynamic environments or previously unseen data distributions at test time.



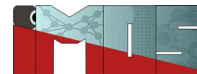
Digital Twins

1. Definition: Digital twins

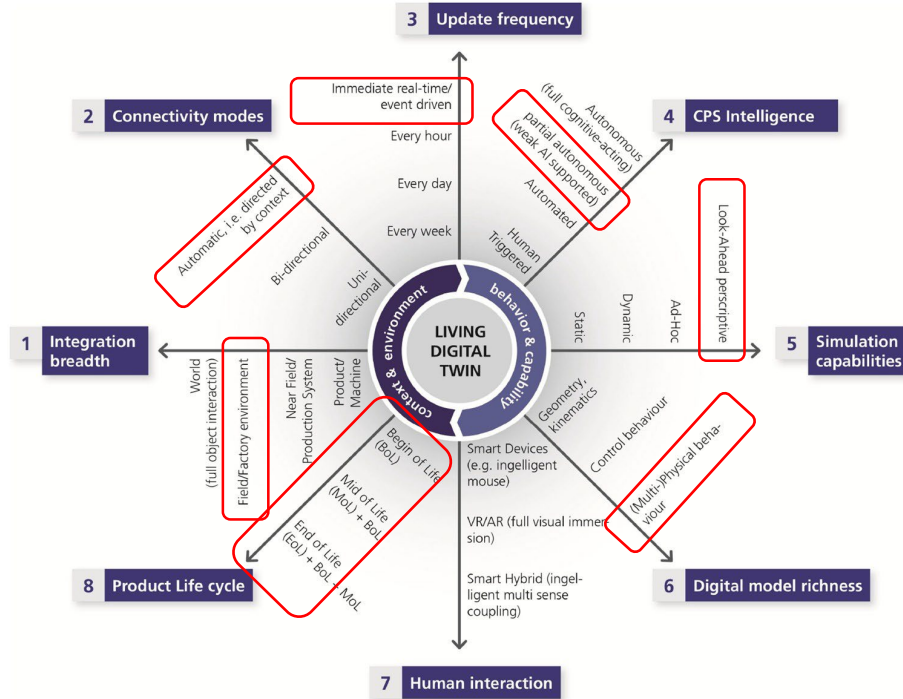
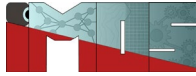


- A digital twin is defined as “a living model of the physical asset or system, which continually adapts to operational changes based on the collected online data and information, and can forecast the future of the corresponding physical counterpart”.

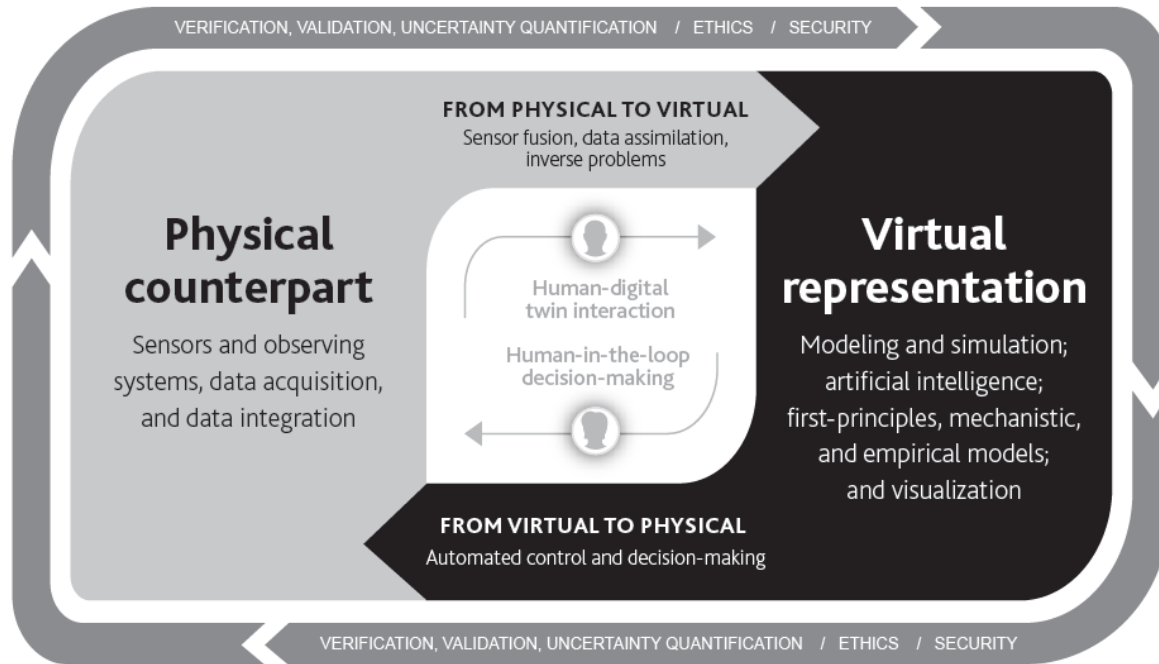
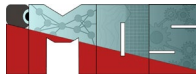
2. Definition: Digital twins



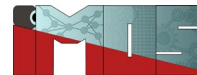
- *A digital twin is a set of virtual information constructs that mimics the structure, context, and behavior of a natural, engineered, or social system (or system-of-systems), is dynamically updated with data from its physical twin, has a predictive capability, and informs decisions that realize value. The bidirectional interaction between the virtual and the physical is central to the digital twin.*



R. Stark, C. Freseemann, and K. Lindow, "Development and operation of Digital Twins for technical systems and services," *CIRP Ann.*, vol. 68, no. 1, pp. 129–132, Jan. 2019.



Digital twin of a patient



REAL WORLD PATIENT

The patient and the tumor from which data is gathered using various clinical assessments to inform the digital twin.

VVUQ

Verification, validation, and uncertainty quantification

As the patient and tumor are constantly evolving and the data collection can also change over time, VVUQ must occur continually for digital twins.

Uncertainty quantification needs to be addressed for all aspects of the digital twin, including the patient's data, modeling and simulation, and decision making.

DIGITAL TWIN

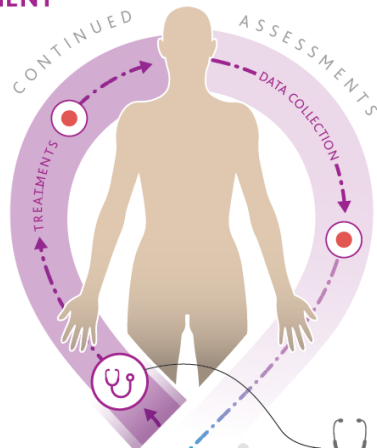
The virtual representation comprised of models describing temporal and spatial characteristics of the patient and tumor with dynamic updates using data from the real world patient.



Modeling

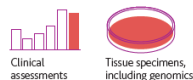
Models spanning a range of fidelities and resolutions may be utilized and potentially integrated together.

As new observed data are acquired, the data are assimilated and the models are calibrated, updated, and estimated.



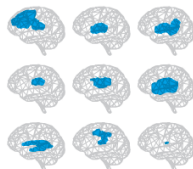
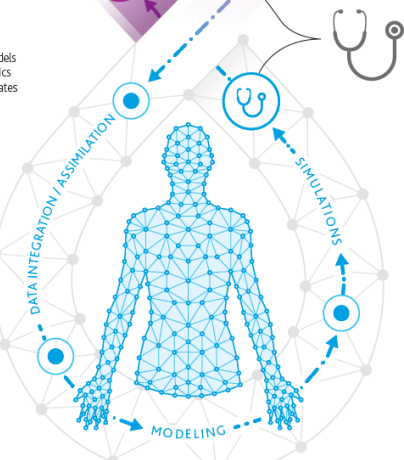
Clinical assessments

Data are collected in many ways:



Human and digital twin interaction

Utilizing the simulated predictions and related uncertainties, the clinician and patient can make informed clinical-decisions around treatment and also the clinical assessments, which affect the data informing the digital twin.

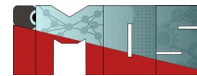


Simulations & predictions

Simulations of potential treatments can generate predictions of outcome and in turn can be optimized to determine the most favorable treatment options.

Verification, Validation, Uncertainty Quantification

- **Verification.** Does a computer program correctly solve the equations of the mathematical model?
- **Validation.** To what degree is a model an accurate representation of the real world, from the perspective of the intended model uses?
- **Uncertainty Quantification.** What are uncertainties in model calculations of quantities of interest?



Manufacturing

Smart Cities

Health care

Energy Sector

Aerospace and Defense

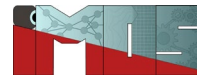
Automotive Industry

Building Energy Systems

Agriculture

Climate

...



Product development

Design + Testing

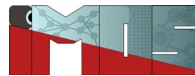
PHM / Maintenance

Optimizing product life-cycle management

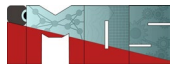
Process Optimization

Prescriptive Operation

A Digital Twin should be Fit for Purpose

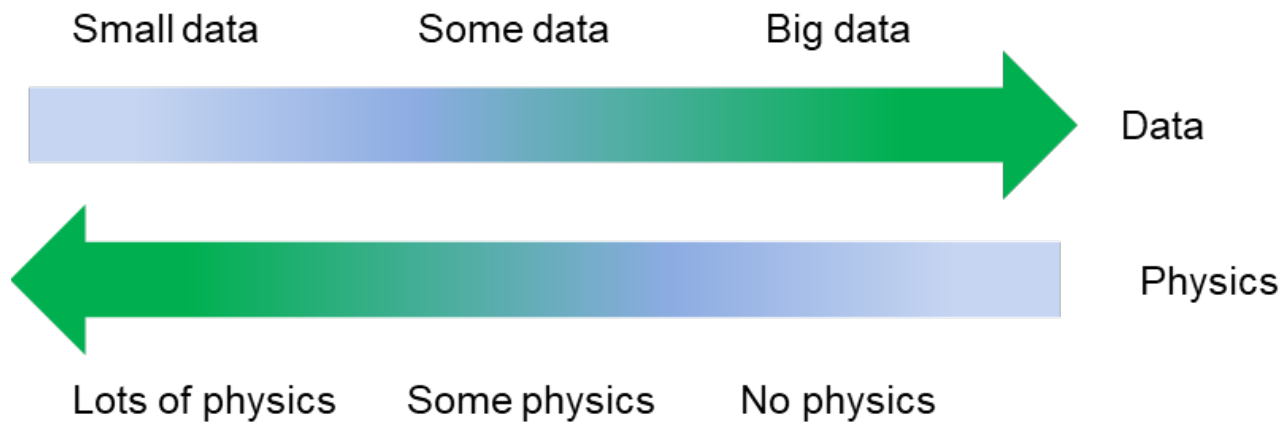
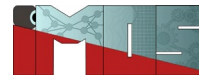


- **Balancing required fidelity for prediction, available resources, and acceptable costs**
- Different digital twin purposes drive different fitness requirements related to modeling fidelity, data availability, visualization, time-to-solution, etc.
- For many potential use cases, achieving fitness-for-purpose is currently intractable

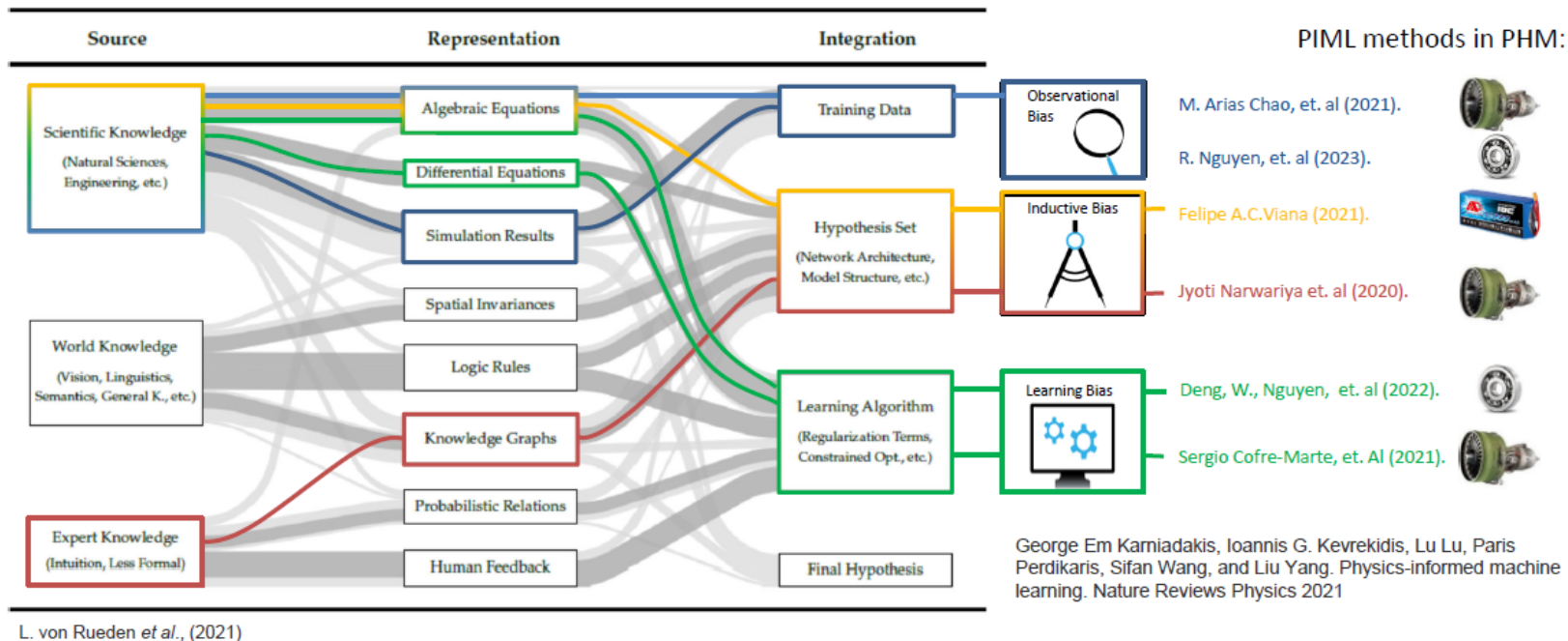
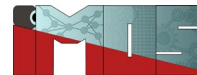


Hybrid Models

Space of potential solutions

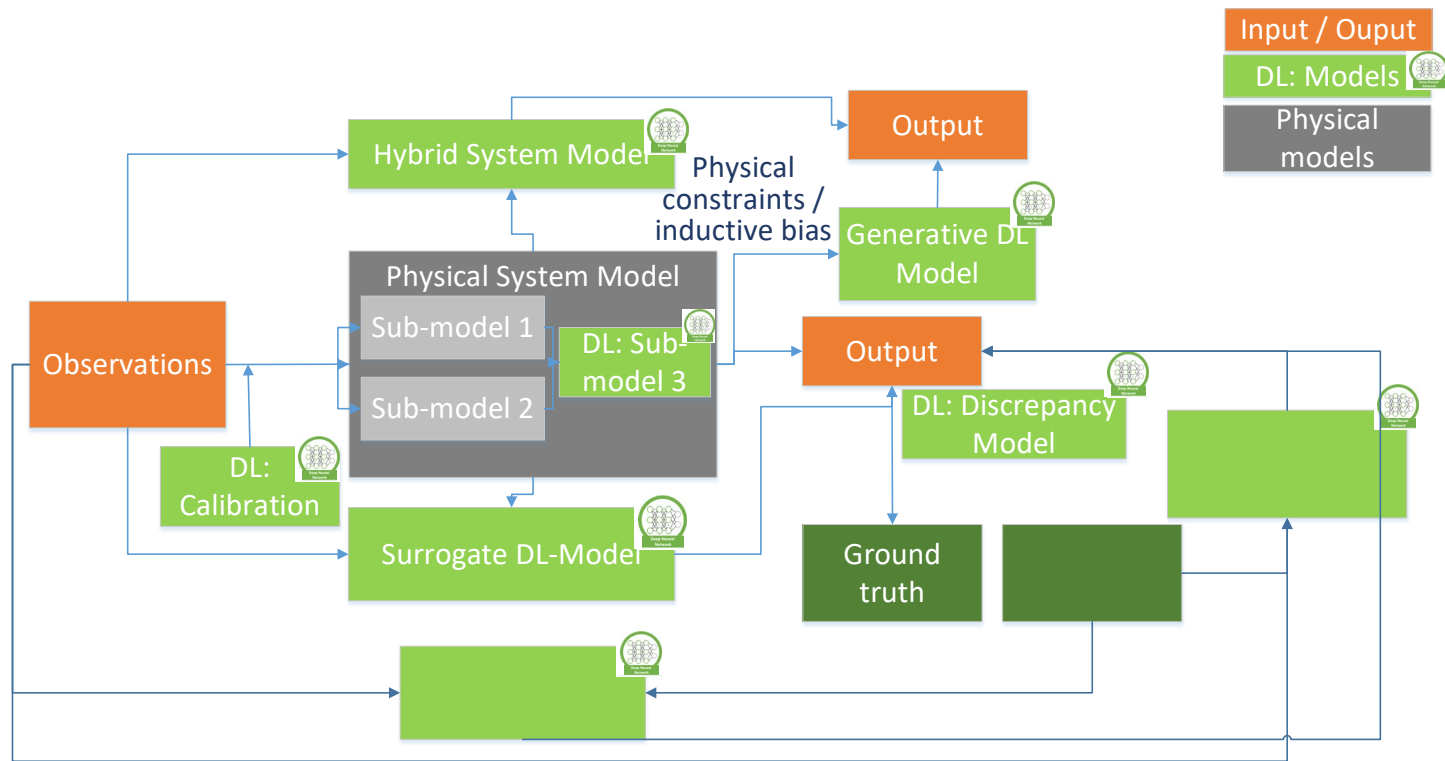
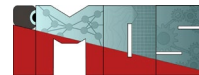


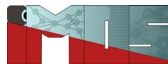
Physics-informed ML for prognostics and health management (PHM)



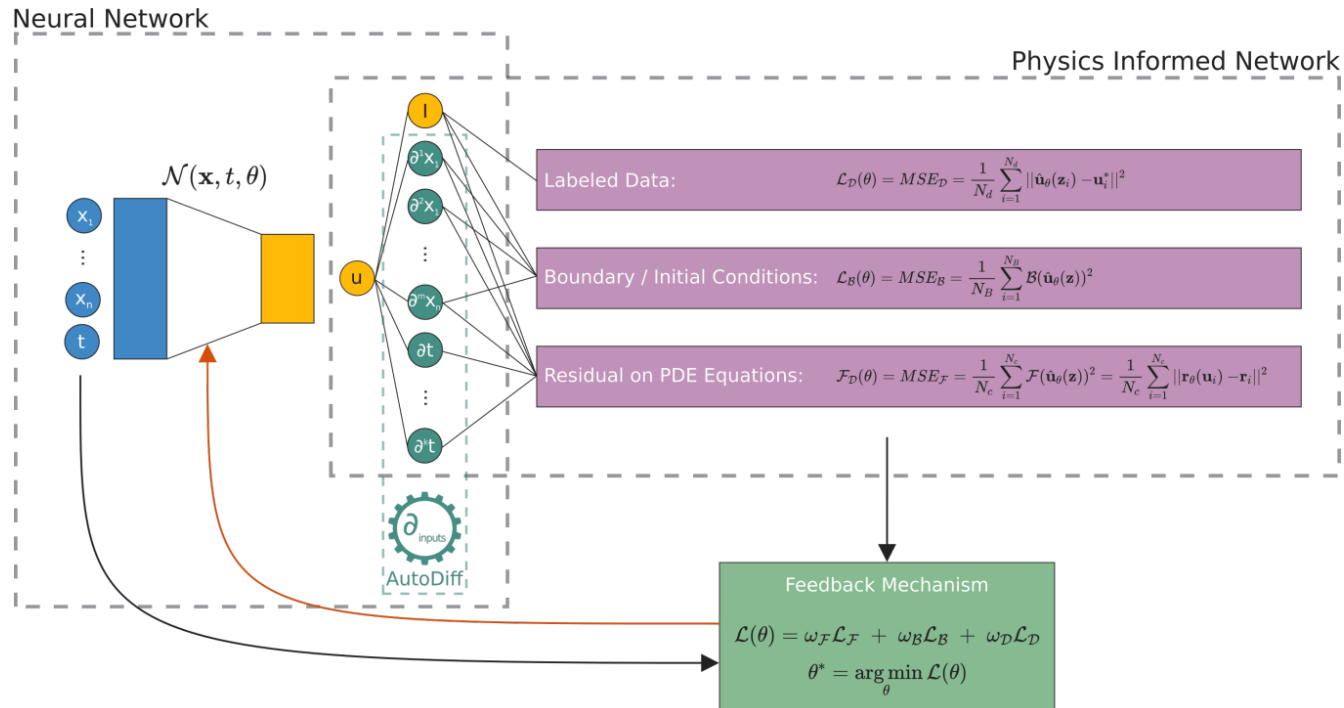
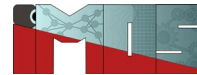
Source: M. Arias

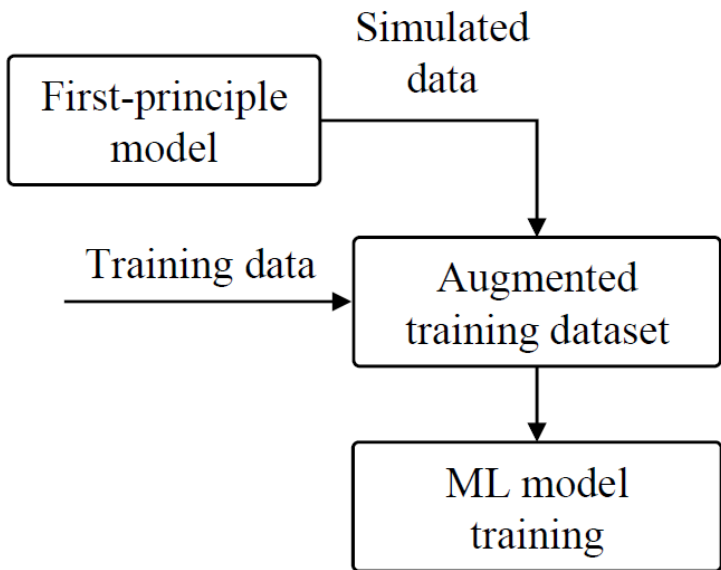
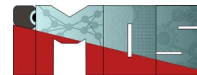
Different ways of fusing DL and physics

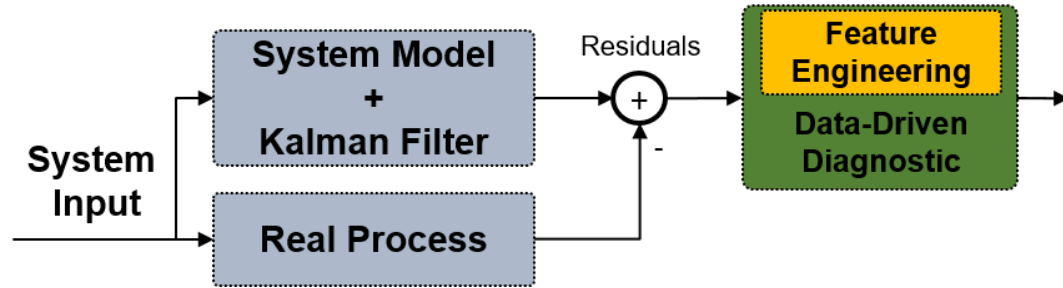
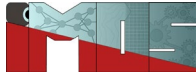


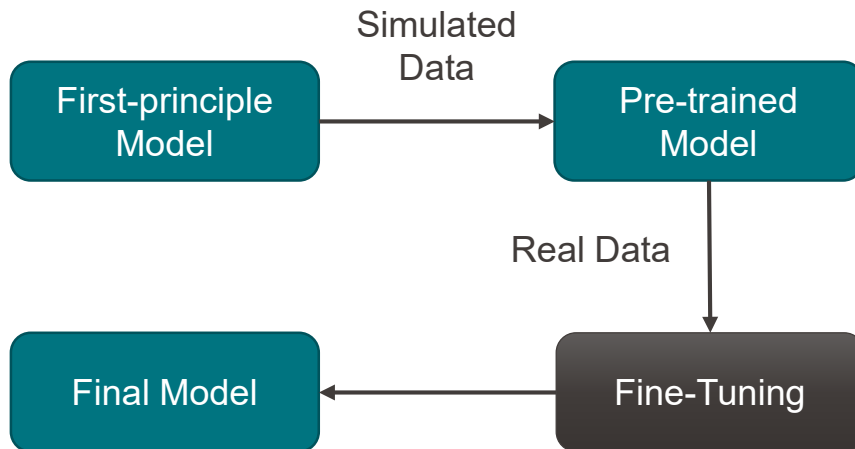
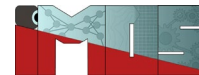


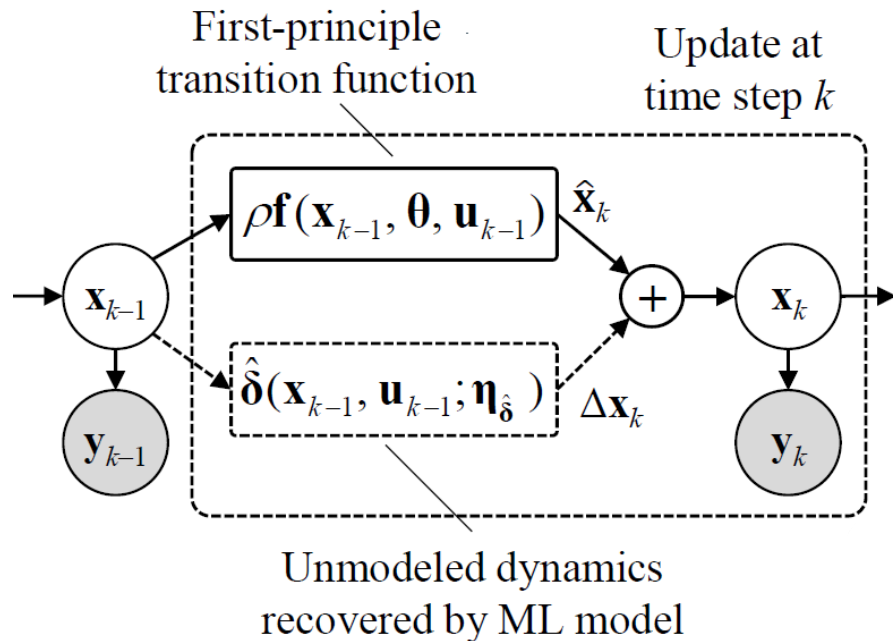
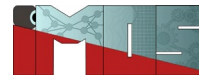
Combining Physics-Based and Deep Learning Models

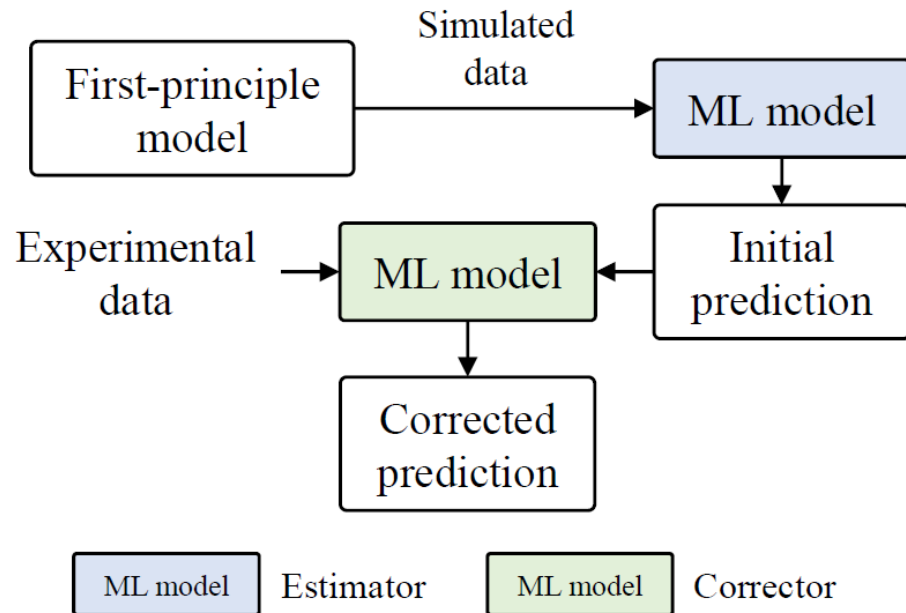
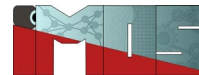


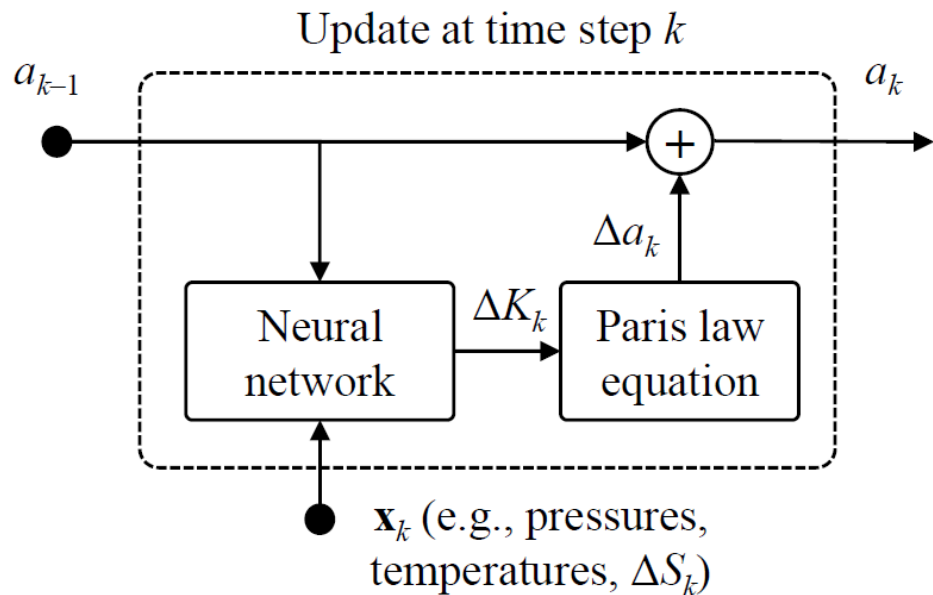
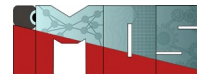






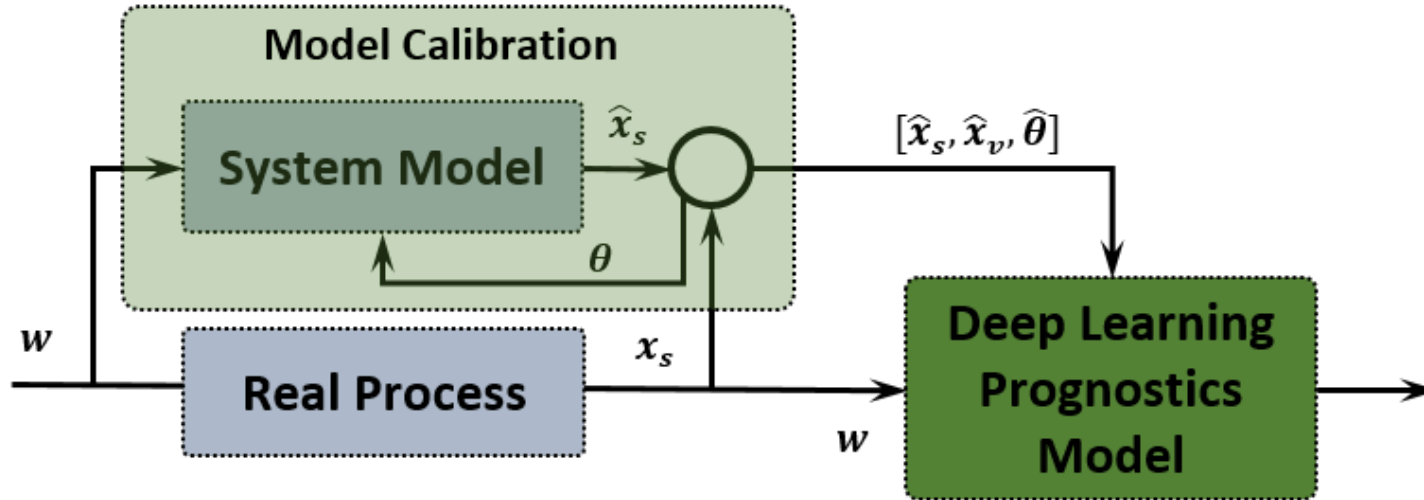
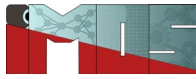


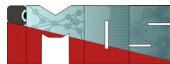




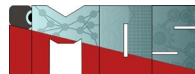
Thelen, A., X. Zhang, O. Fink, Y. Lu, S. Ghosh, B.D. Youn, M.D. Todd, S. Mahadevan, C. Hu, Z. Hu. "A Comprehensive Review of Digital Twin - Part 1: Modeling and Twinning Enabling Technologies"[A Comprehensive Review of Digital Twin - Part 1: Modeling and Twinning Enabling Technologies.", accepted for publication in Structural and Multidisciplinary Optimization journal

Fusing physical performance models and deep learning





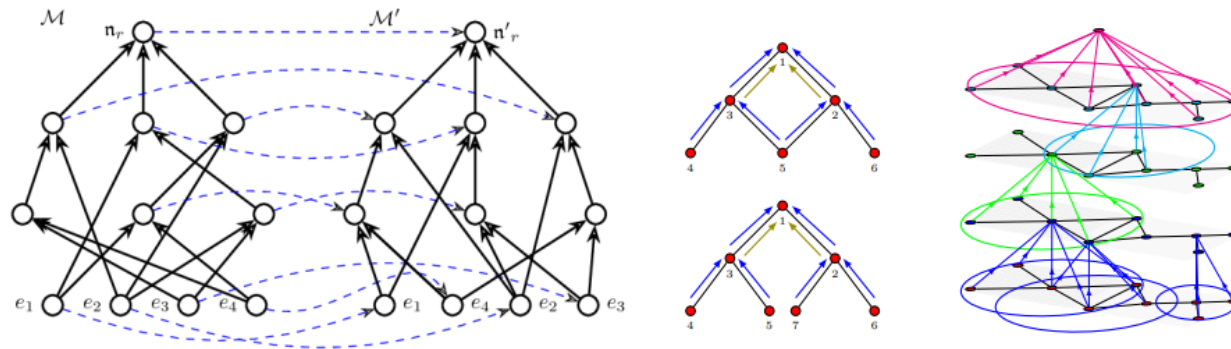
Inductive bias



- Inductive bias refers to the set of assumptions a learning algorithm uses to generalize from training data to unseen data.
- It helps guide the learning process and shapes the predictions that a model makes.
- Strongly impacts how well a model generalizes to new data.
- Examples include:
 - Linear regression assumes a linear relationship between input and output.
 - Convolutional Neural Networks (CNNs) assume spatial hierarchies and local dependencies for image data.
- Enables efficient learning by reducing the hypothesis space.
- Can lead to poor generalization if the assumptions do not match the underlying data distribution.

Inductive bias / Physics Informed Neural Networks (1/2)

I. Physics is implicitly baked in specialized neural architectures with strong inductive biases (e.g. invariance to simple group symmetries).



**figures from Kondor, R., Son, H.T., Pan, H., Anderson, B., & Trivedi, S. (2018). Covariant compositional networks for learning graphs. arXiv preprint arXiv:1801.02144.*

2. Physics is explicitly imposed by constraining the output of conventional neural architectures with weak inductive biases.

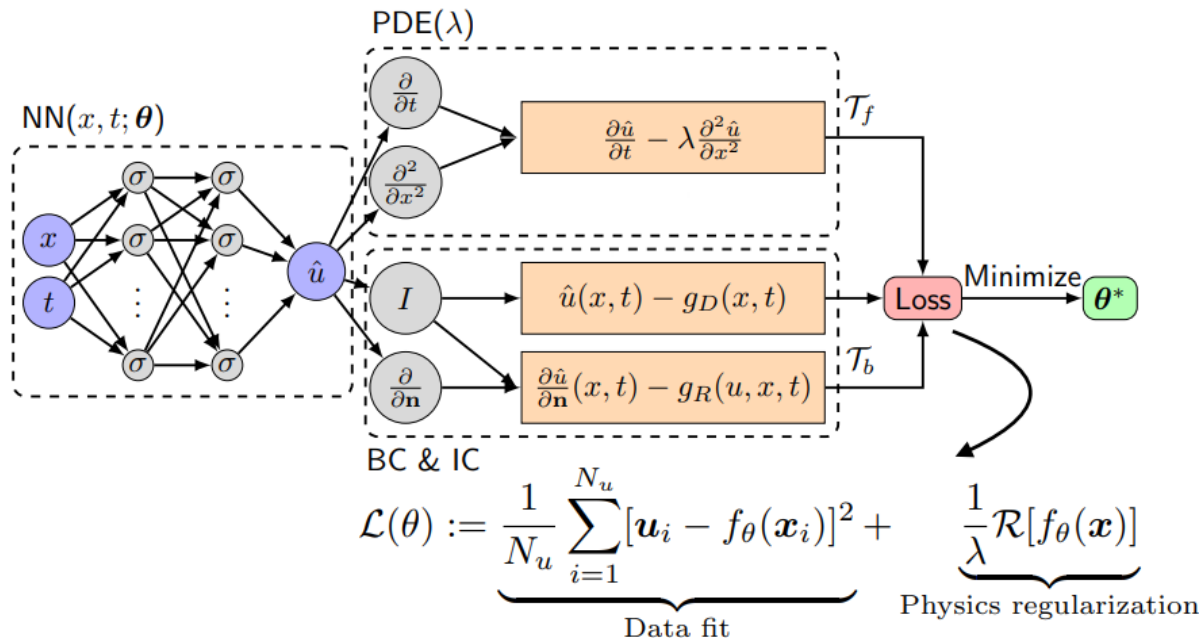
Psichogios & Ungar, 1992

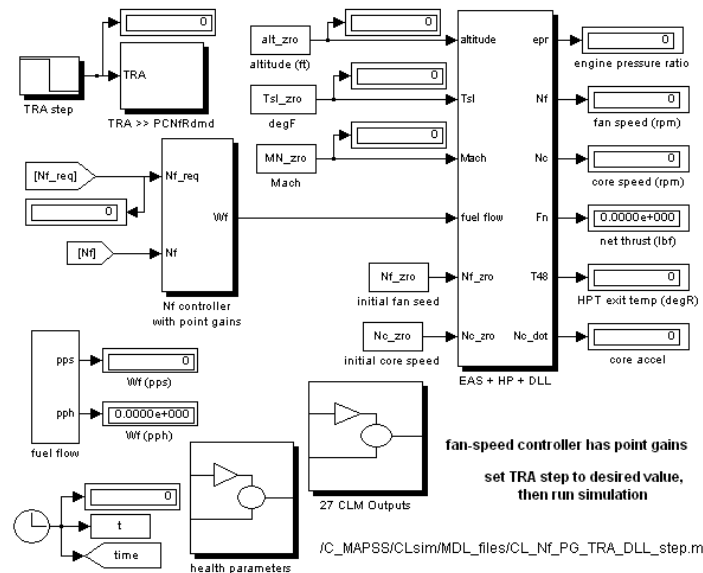
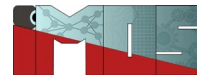
Lagaris et. al., 1998

Raissi et. al., 2019

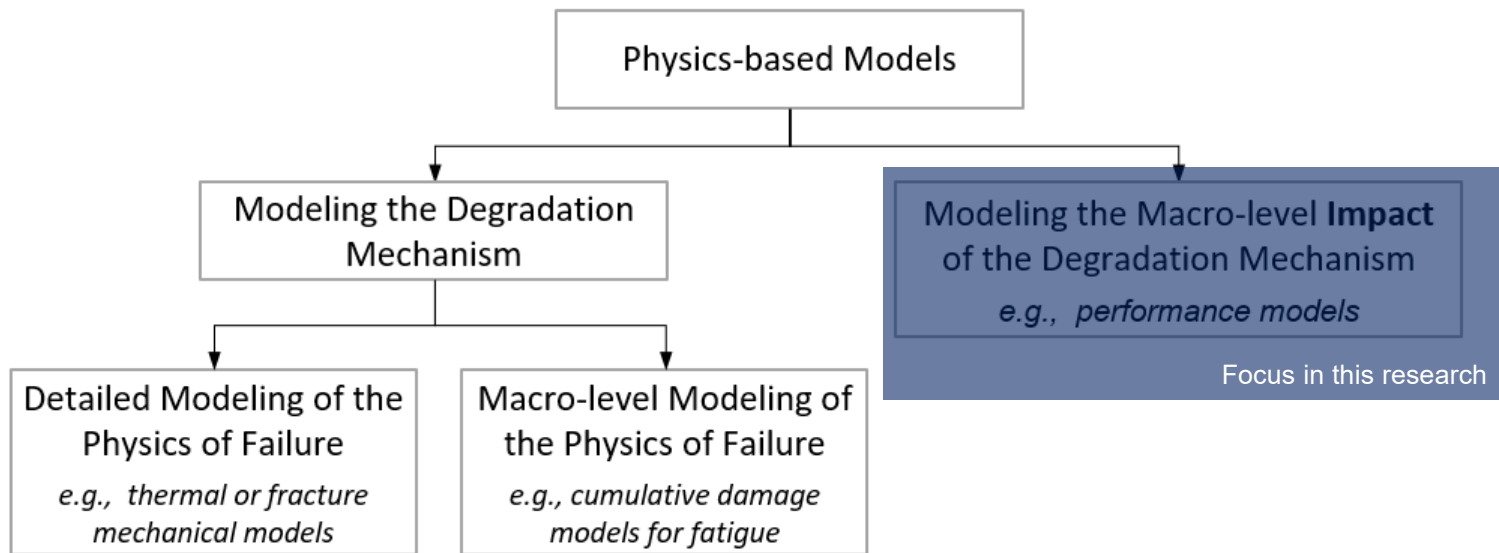
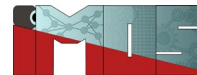
Lu et. al., 2019

Zhu et. al., 2019

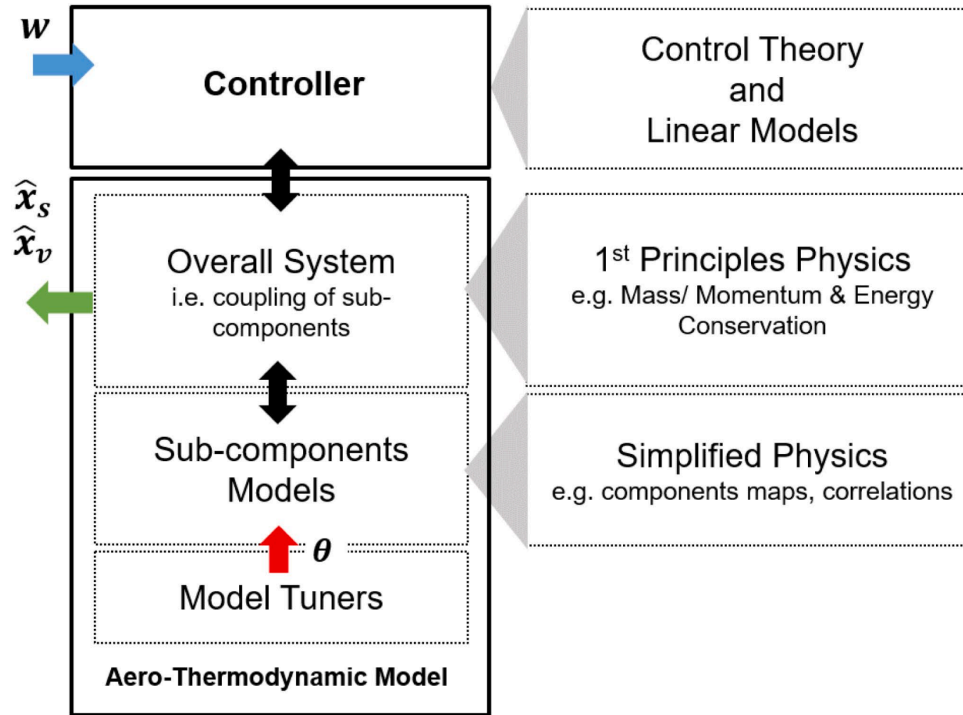
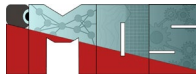




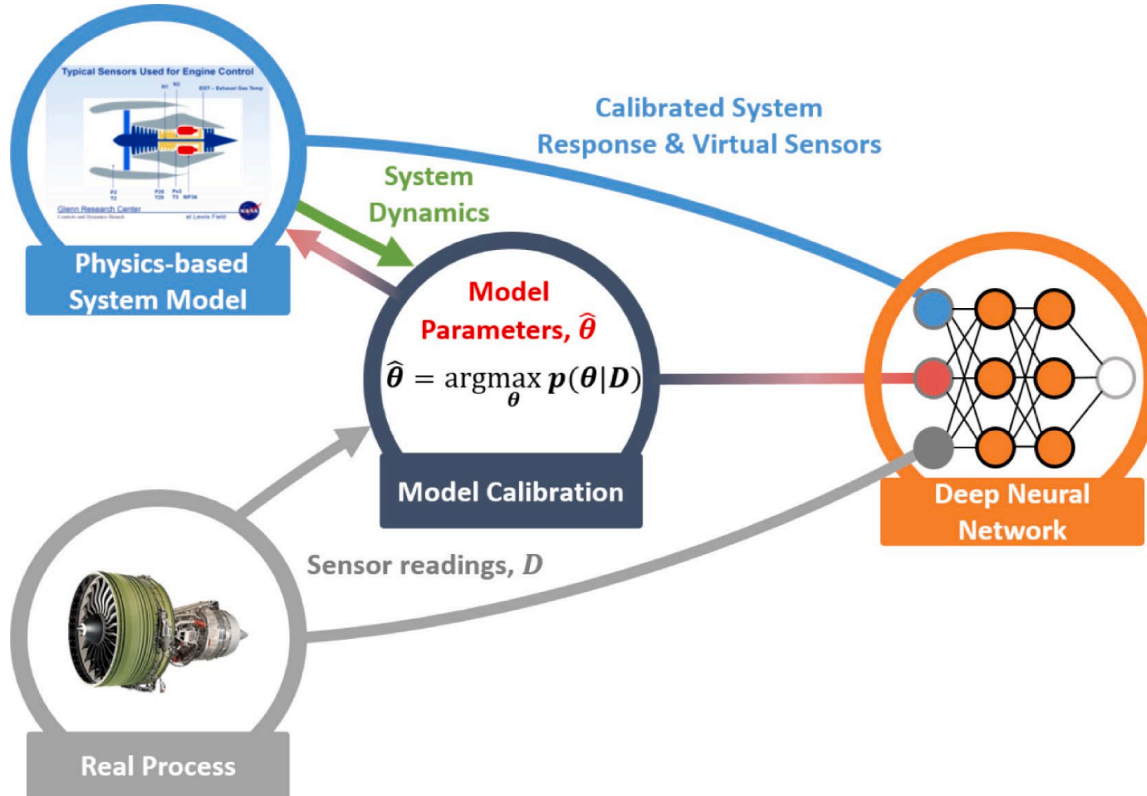
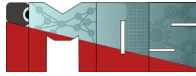
Calibration-based hybrid framework for prognostics

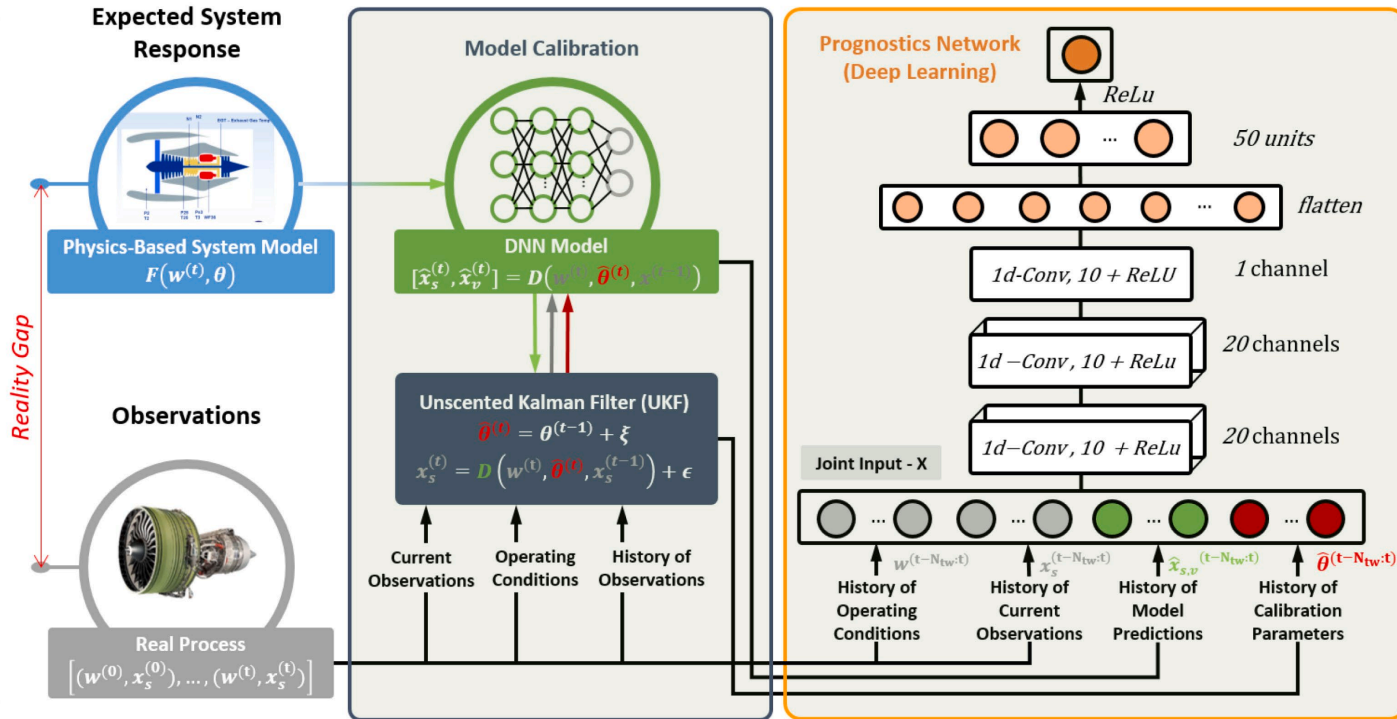
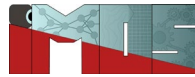


General topology of an aero-thermodynamic performance model

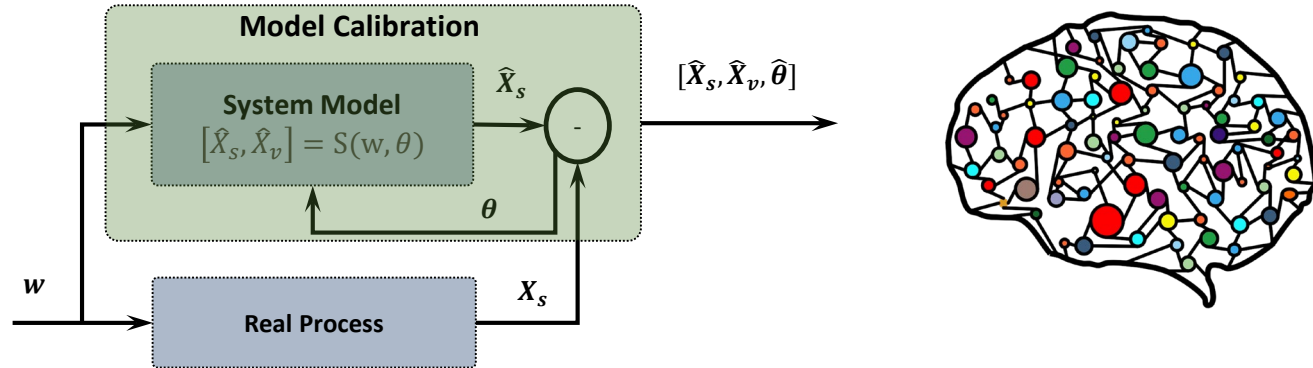
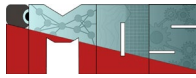


Basic idea of the hybrid approach

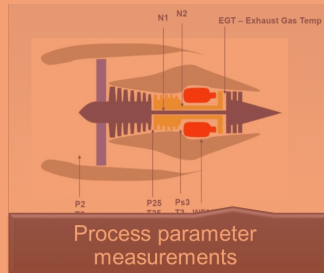




Enhancing the input space with inputs from physics-based models

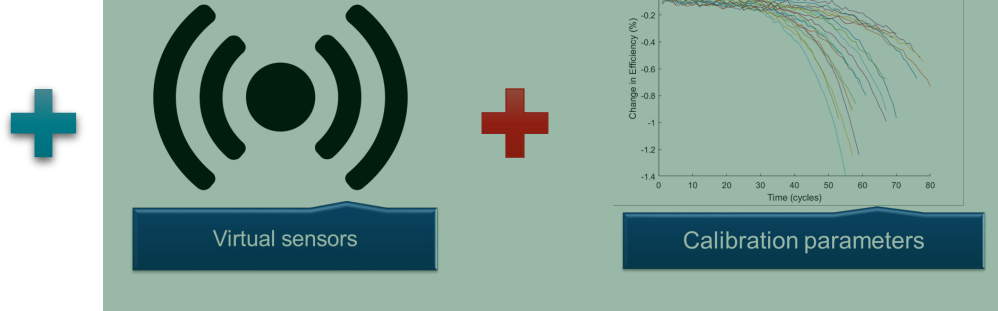


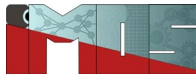
Purely data-driven



11.11.24

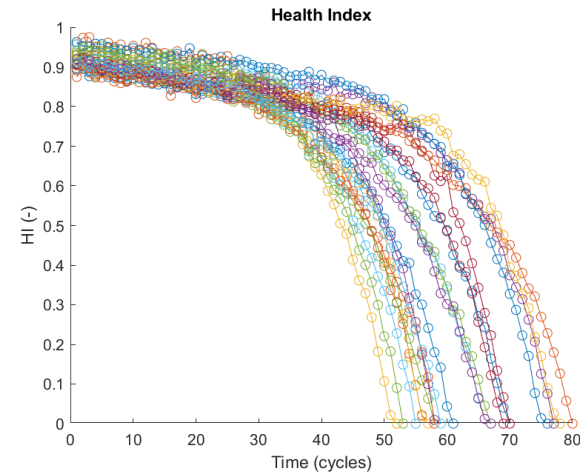
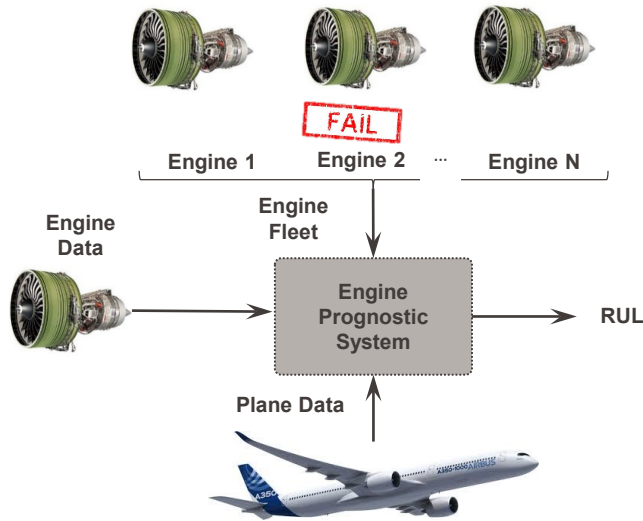
Inferred from physics-based models



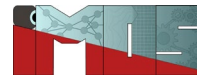


Remaining Useful Life (RUL) of a component

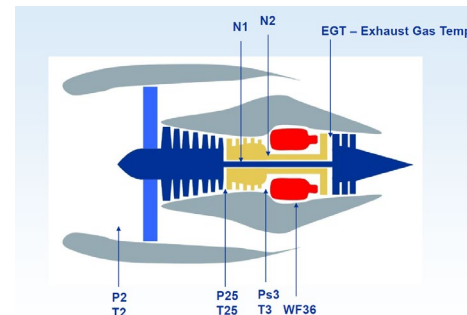
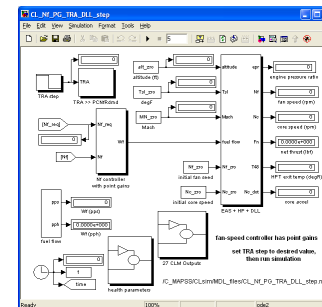
- the amount of time a component can be expected to continue operating within its stated specifications

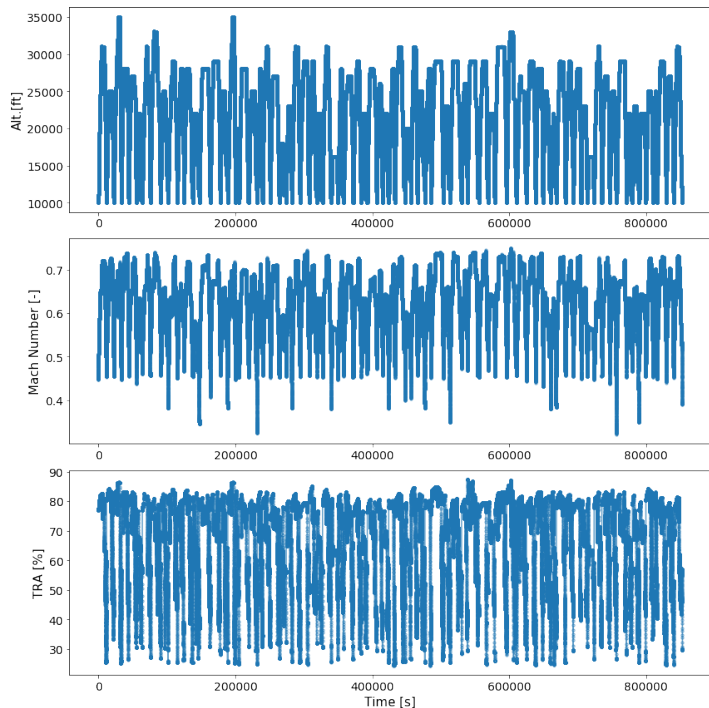
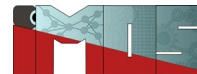


Test Case: Turbofan Engine



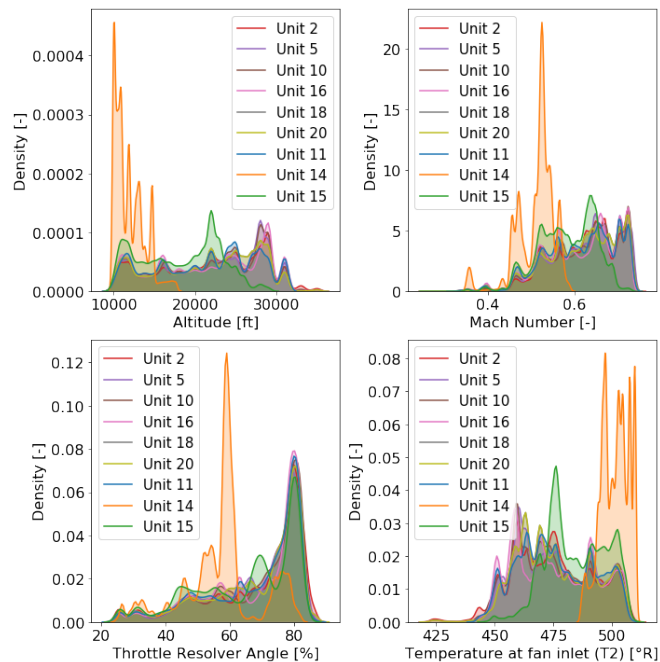
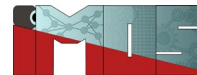
- **Simulation of a realistic large commercial turbofan engine**
 - Simulated run to failure trajectories with the Commercial Modular Aero-Propulsion System Simulation (C-MAPSS) dynamical model
- **Real flight conditions from a commercial jet**
 - NASA DASHlink
 - ~500 different (1-12h) flights
 - Recordings covering climb, cruise and descend
 - Operative conditions - $w \in R^3$
- **Data from a fleet of 9 turbofan engines**
 - Internal sensors - $x_s \in R^{10}$
 - Virtual sensors - $x_v \in R^{15}$
 - Model parameters - $\theta \in R^{10}$

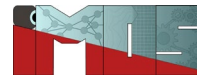




- **Failure modes:** 1) HPT degradation 2) HPT and LPT flow and efficiency degradation
- **Flight conditions:** Alt > 10000 [ft]
- **Training Data:**
 - 6 engines
 - 50-90 cycles (flights)
 - $w, X_s, \hat{\theta}$ & RUL
 - 5.5×10^6 samples
- **Test Data:**
 - 3 engines
 - w, X_s & $\hat{\theta}$
 - 1.2×10^6 samples

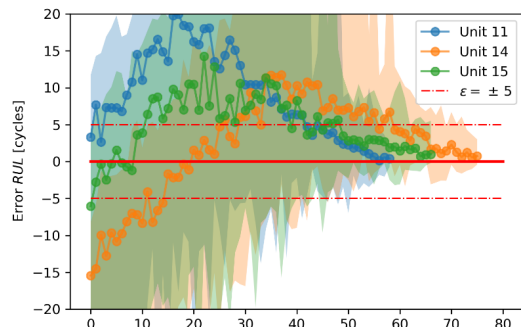
Kernel density estimations of the simulated flight envelopes given by recordings of altitude



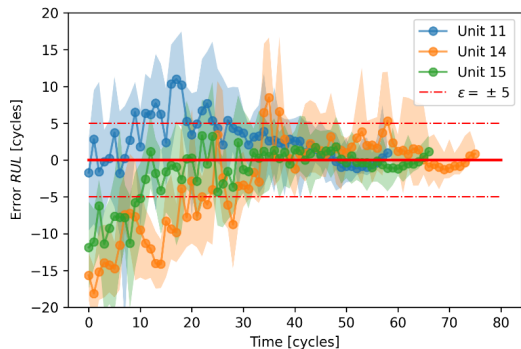


Data-driven - $X = [w, X_s]$

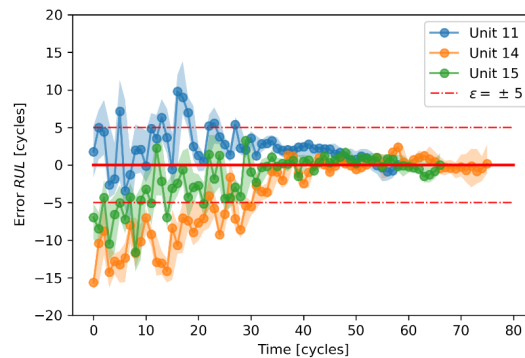
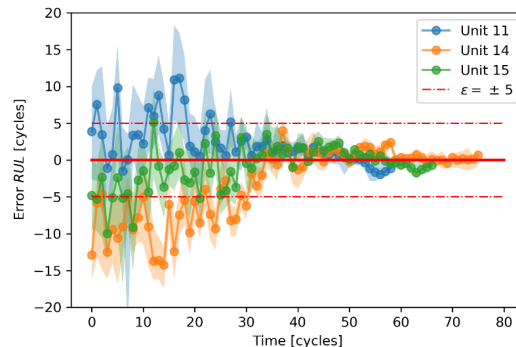
FFN



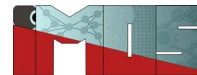
CNN



Hybrid - $X = [w, \hat{X}_s, \hat{X}_v, \hat{\theta}]$



11.11.24



FFN

Metric	Data-Driven	Hybrid	Rel. Delta
RMSE [-]	7.89 ± 0.12	4.22 ± 0.10	-47%
$s \times 10^5 [-]$	1.39 ± 0.04	0.44 ± 0.01	-68%

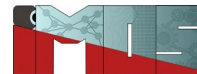
CNN

Metric	Data-Driven	Hybrid	Rel. Delta
RMSE [-]	4.95 ± 0.15	4.14 ± 0.09	-16%
$s \times 10^5 [-]$	0.56 ± 0.03	0.44 ± 0.02	-21%

$$s = \sum_{j=1}^{m_*} \exp(\alpha |\Delta^{(j)}|)$$

$$RMSE = \sqrt{\frac{1}{m_*} \sum_{j=1}^{m_*} (\Delta^{(j)})^2}$$

EOL prediction within the error bound of 5 cycles



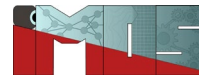
CNN

$t_{EOL} - t_{\epsilon_y < 5}$ in [cycles]

unit	Data-Driven	Hybrid	Rel. Delta
11	11	31	195%
14	15	43	197%
15	24	37	54%
Fleet Avg.	16	37	127%

→ Prediction **horizon prolonged by 127%** on average (for some units ca. 200%)

Detailed results RUL prediction: smaller training dataset



CNN: trained on units 2,5,10,16,18,20

Metric	Data-Driven	Hybrid	Rel. Delta
RMSE [-]	4.95 ± 0.15	4.14 ± 0.09	-16%
$s \times 10^5 [-]$	0.56 ± 0.03	0.44 ± 0.02	-21%

$$s = \sum_{j=1}^{m_*} \exp(\alpha |\Delta^{(j)}|)$$

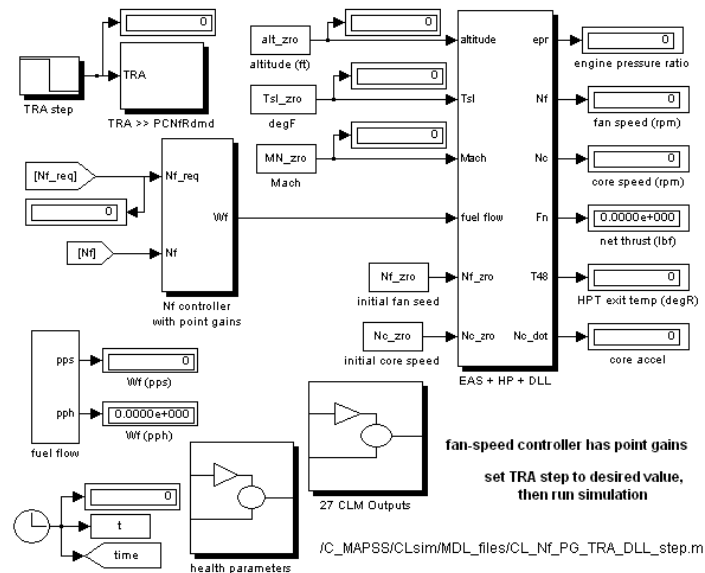
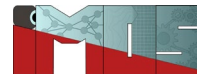
$$RMSE = \sqrt{\frac{1}{m_*} \sum_{j=1}^{m_*} (\Delta^{(j)})^2}$$

CNN: trained on units 16,18,20

Metric	Data-Driven	Hybrid	Rel. Delta
RMSE [-]	5.97 ± 0.37	4.22 ± 0.12	-29%
$s \times 10^5 [-]$	0.61 ± 0.03	0.43 ± 0.02	-29%
rel. Delta RMSE [%]	17%	2%	
Rel. Delta s [%]	8%	-2%	

→ **ca. 50% reduction of training data size**

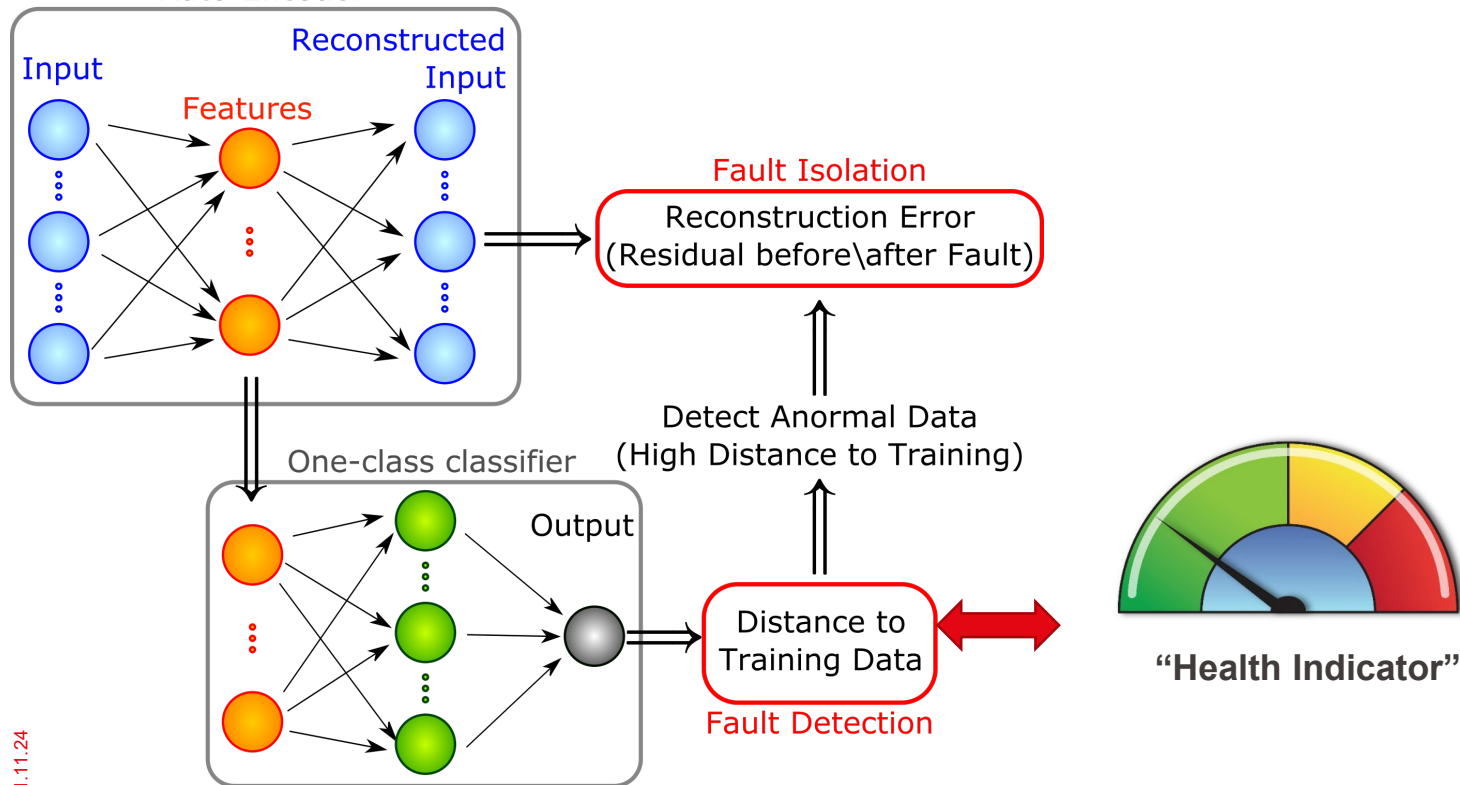
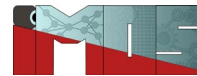
→ **performance level maintained**



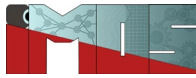
Hybrid Fault Detection and Diagnostics

How to improve not only the performance but also the interpretability and generalizability?

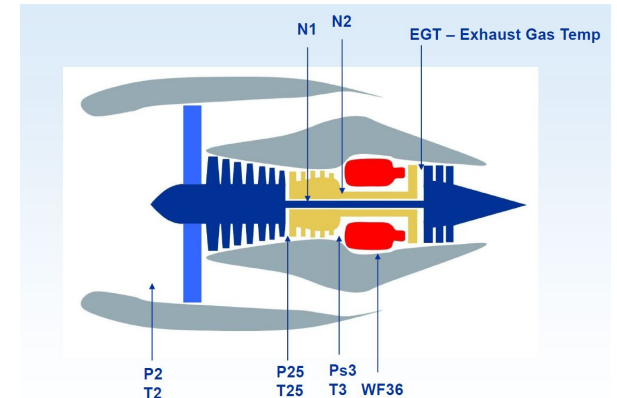
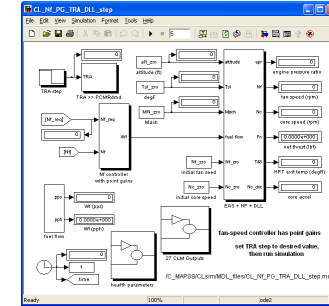
Analysing the reconstruction residuals for fault isolation

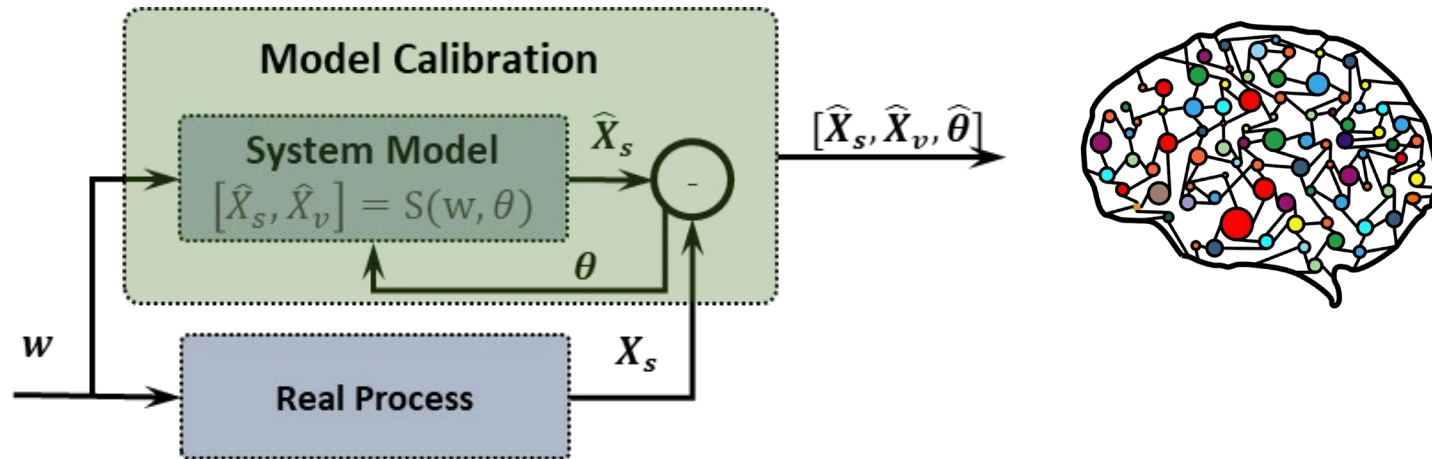
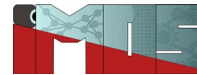


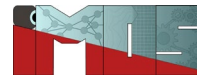
Test Case: Turbofan Engine



- **Simulation of a realistic large commercial turbofan engine**
- **24 flight cycles**
- **Each flight contains ca. 175 snapshots of recordings covering climb, cruise and descend conditions**
- **Real flight conditions from a commercial jet**
- **Fault: HPC Efficiency with different magnitudes**

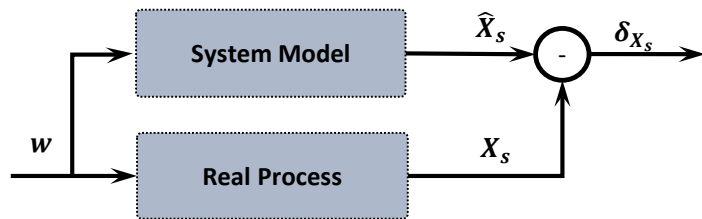




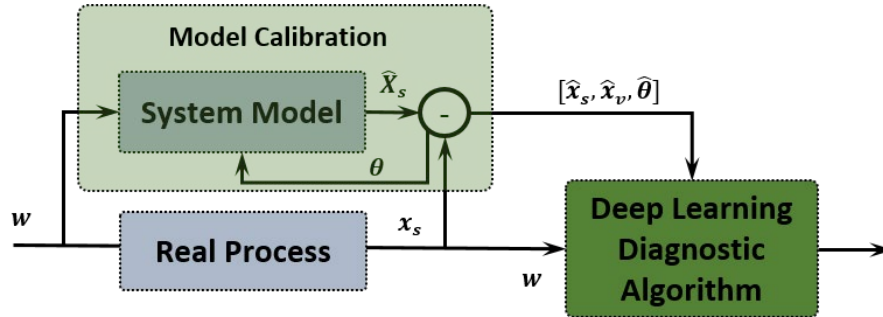
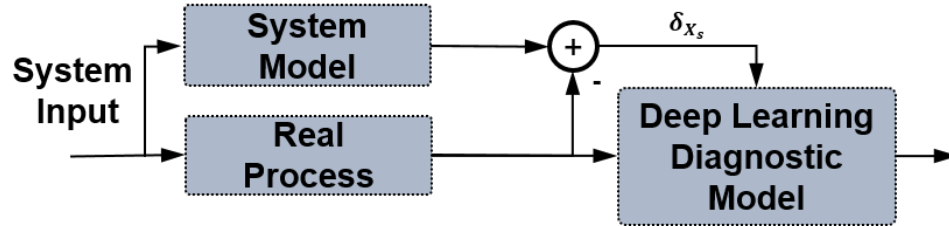
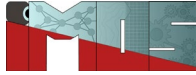


Degradation features provided by the system model:

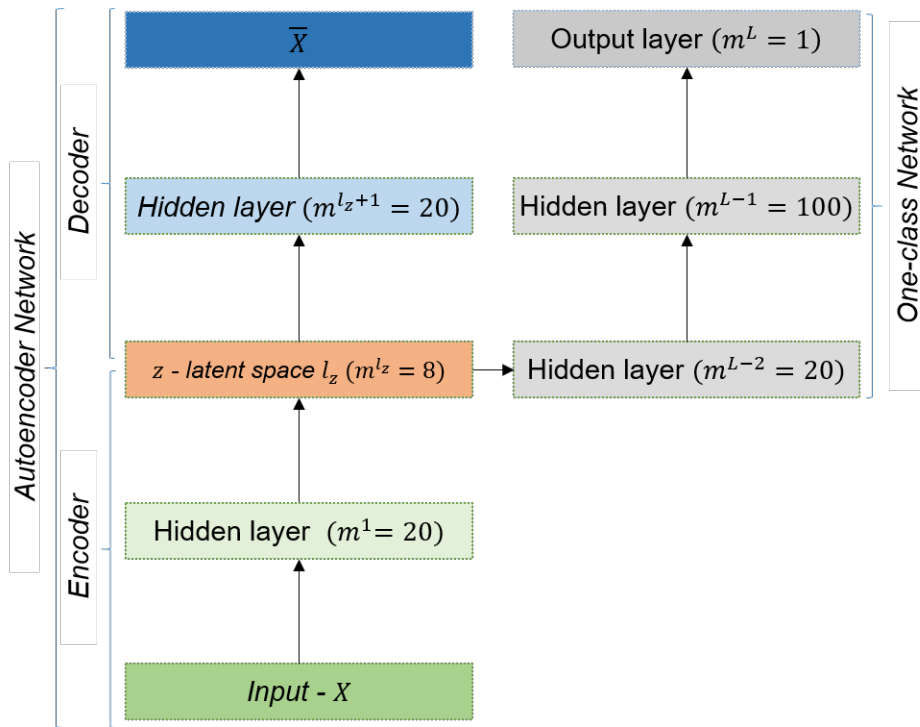
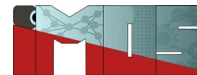
- Residual $\delta_{X_s} = \hat{X}_s - X_s$
 - Direct computation

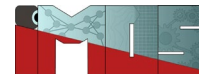


Two tested setups



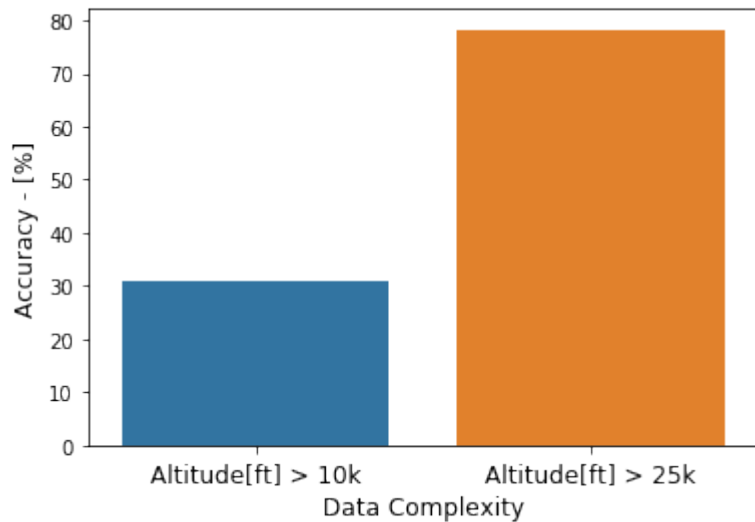
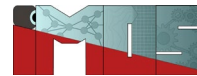
Arias Chao, M., Kulkarni, C., Goebel, K., & Fink, O. (2019). Hybrid deep fault detection and isolation: Combining deep neural networks and system performance models. *International Journal of Prognostics and Health Management*



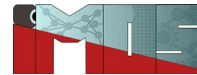


		AE	VAE	OC-SVM
Data-driven	$[W, X_S]$	24.5	12.9	10.0
Residual-based	$[W, X_S, \delta_{X_S}]$	98.7	99.3	79.5
Hybrid (calibration-based)	$[W, \widehat{X}_S, \widehat{X}_V, \hat{\theta}]$	100.0	97.5	96.2

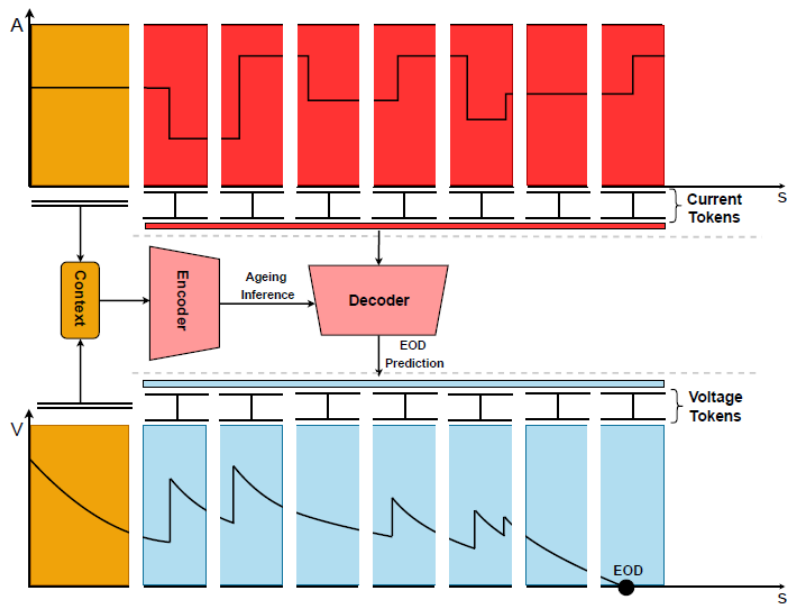
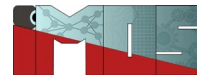
Influence of the data complexity (data-driven model)



Fault isolation (with a high fault intensity)

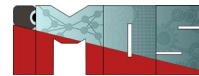


		AE
Data-driven	$[W, X_S]$	Physical core speed Static pressure at HPC outlet
Residual-based	$[W, X_S, \delta_{X_S}]$	Delta physical core speed Delta total temp. at HPC outlet Delta total temp. at LPC outlet Delta total temp. at HPT outlet Delta total temp. at LPT outlet
Hybrid (calibration-based)	$[W, \widehat{X}_S, \widehat{X}_V, \hat{\theta}]$	HPC efficiency modifier

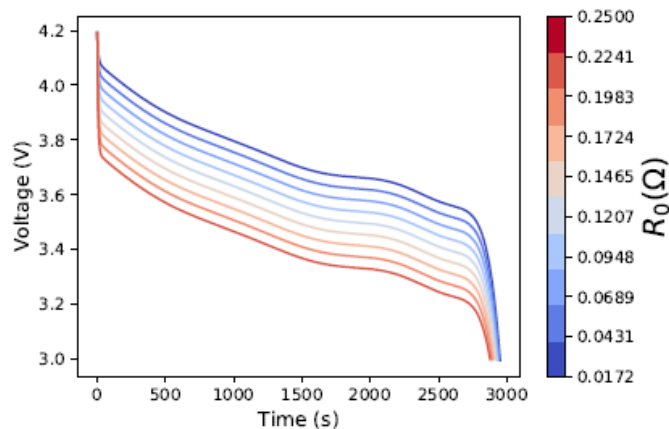
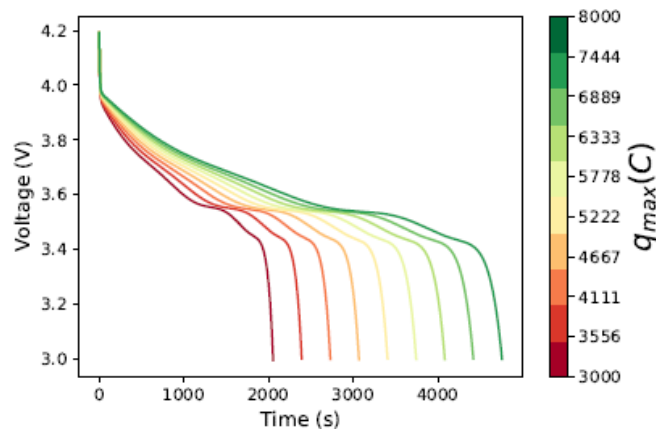
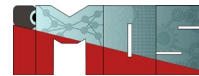


Ageing-aware Battery Discharge Prediction

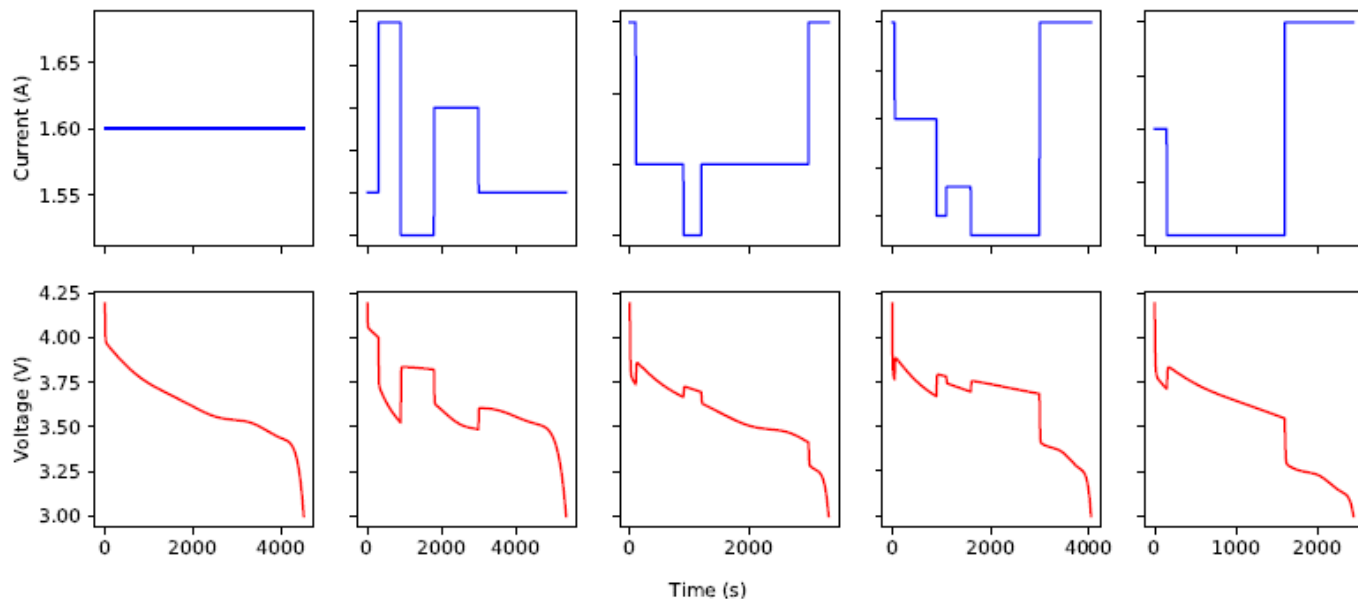
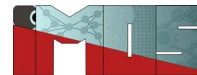
Degradation of Li-Ion batteries → importance of precise planning



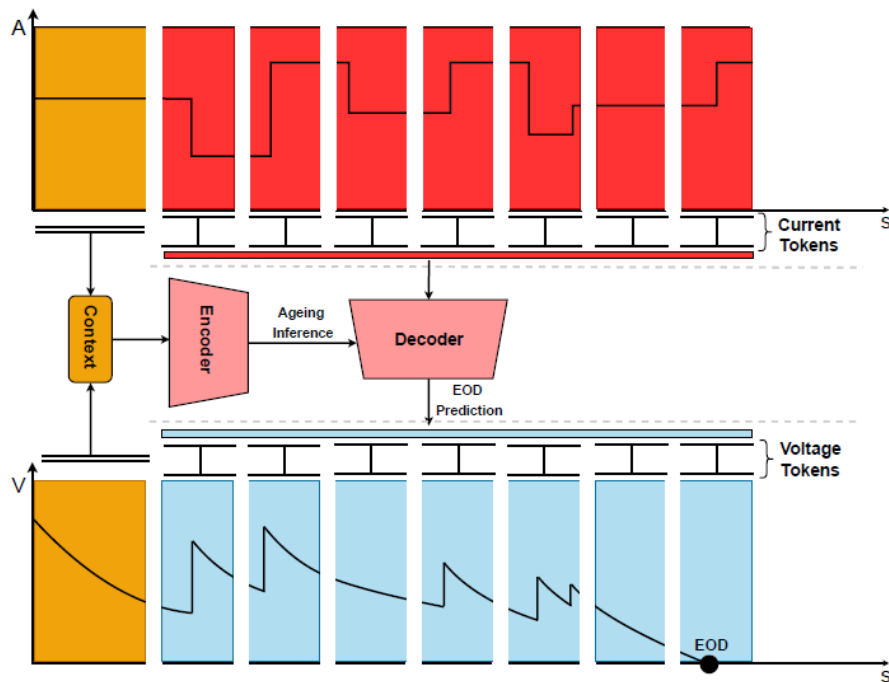
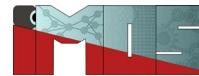
Effect of varying the degradation parameters on the voltage discharge curve of a Li-ion battery

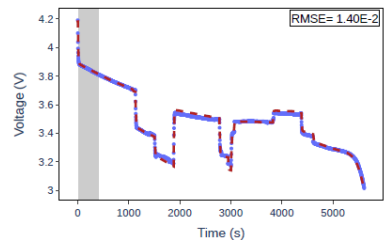
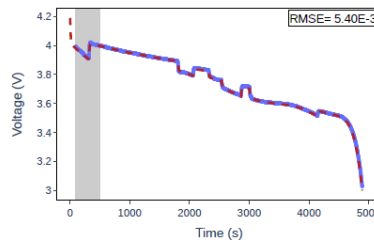
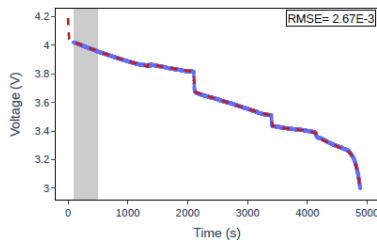
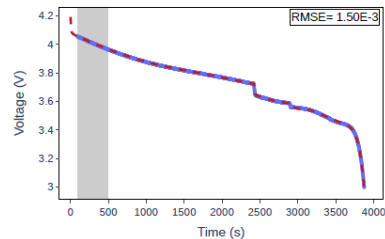
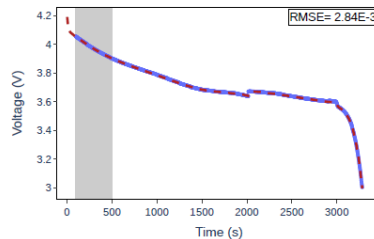
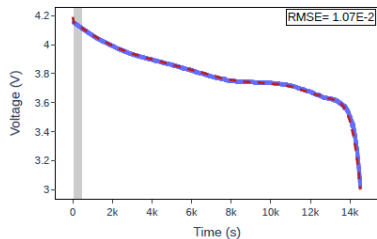
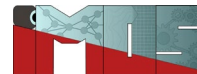


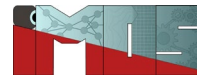
Discharge behaviors with respect to the different load profiles



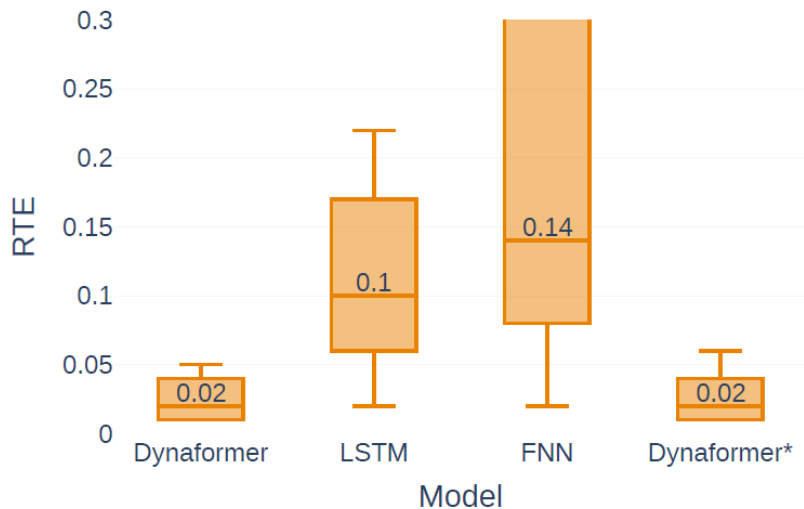
Transformer-based long-term battery discharge prediction → Dynaformer



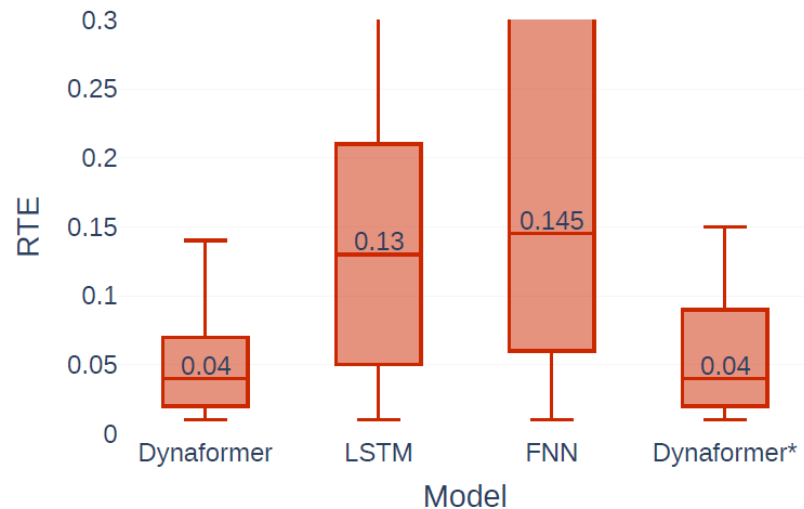




Interpolation



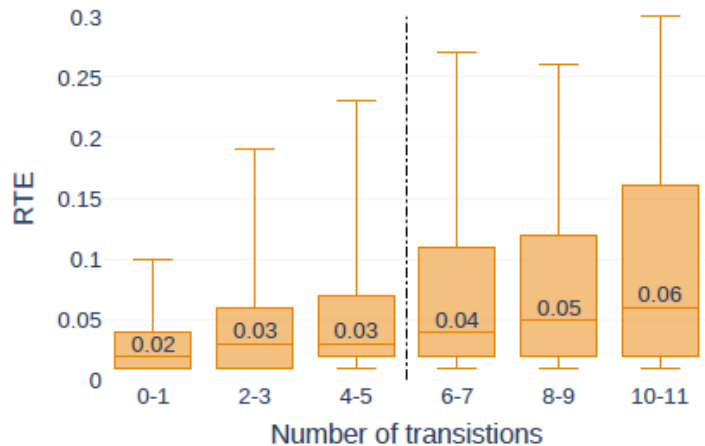
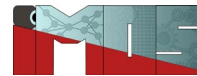
Extrapolation



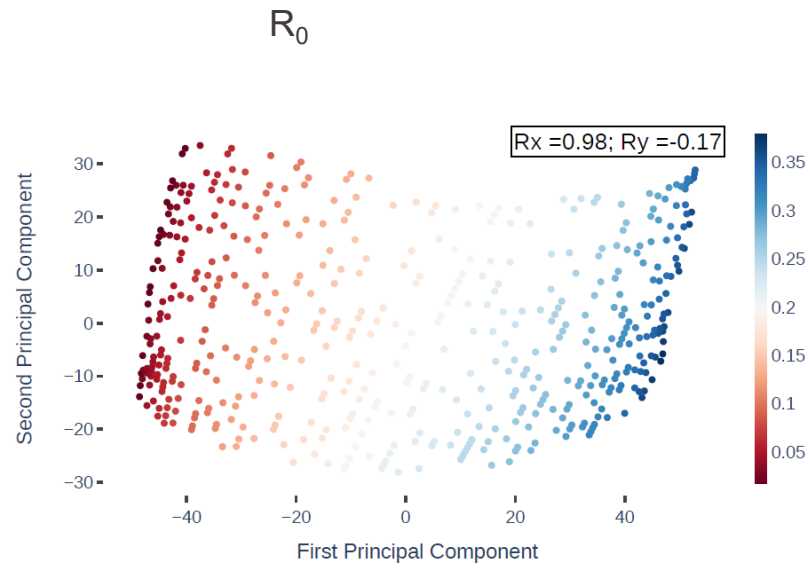
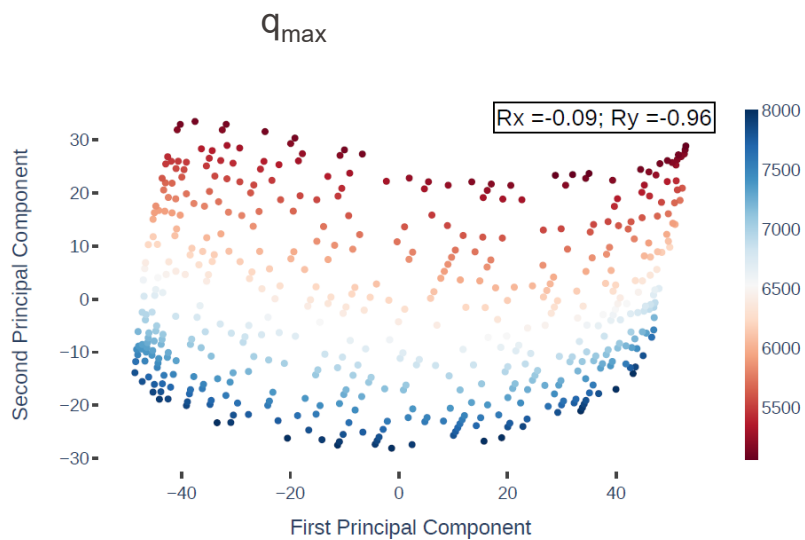
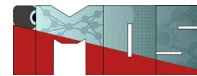
Dynaformer* → trained with variable current profiles

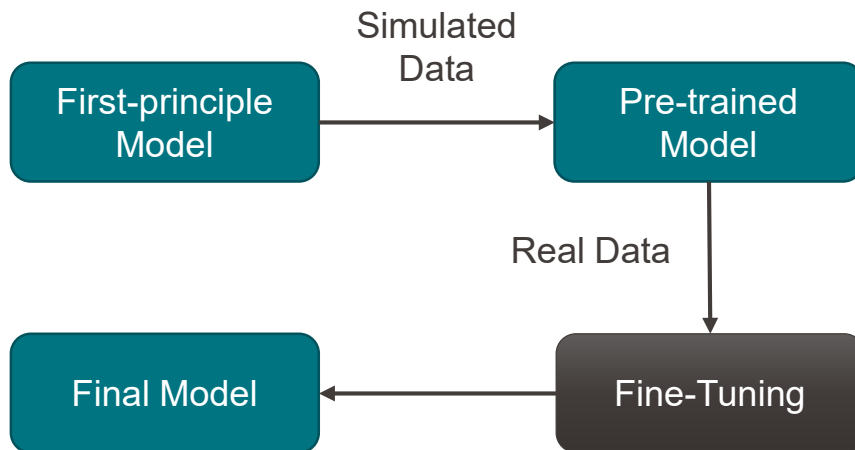
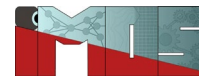
*RTE = relative temporal error

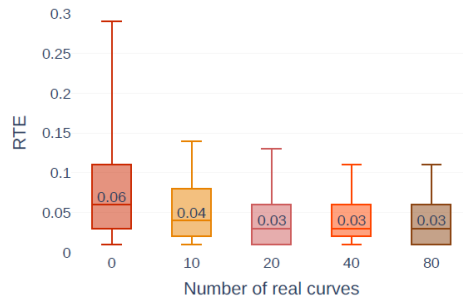
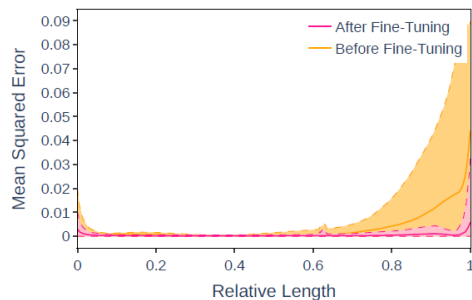
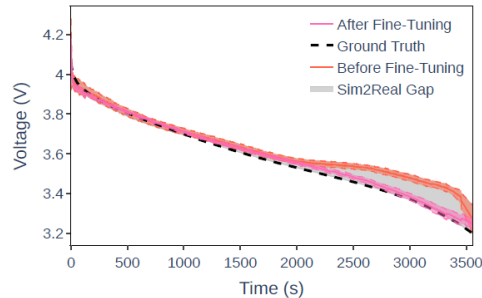
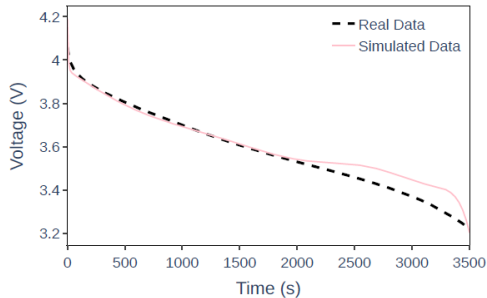
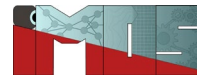
Performance dependent on the complexity of the the load profiles



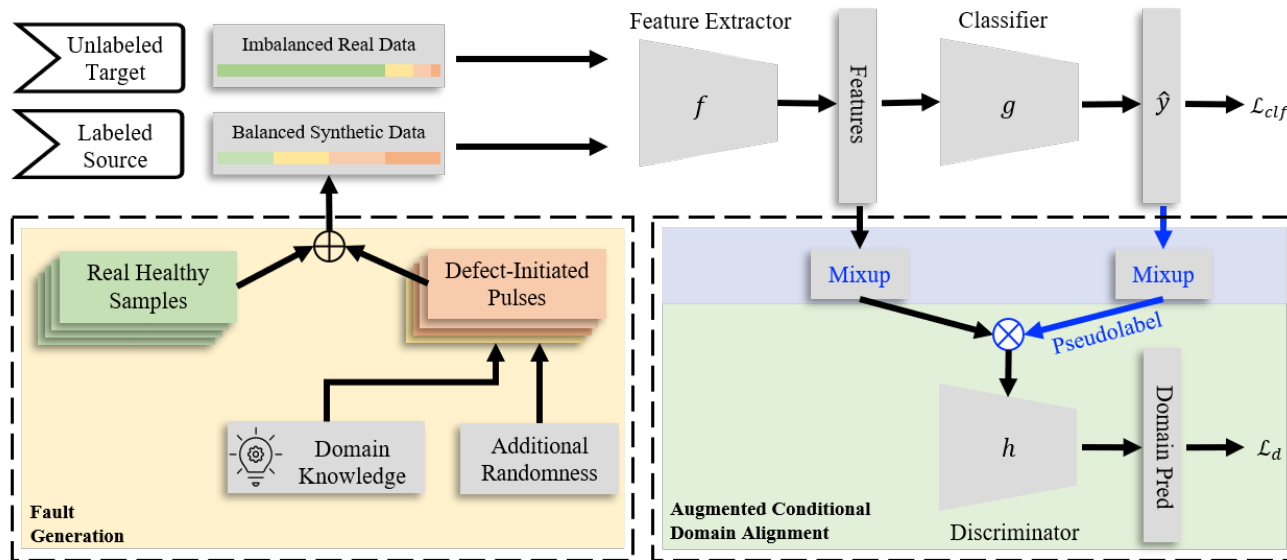
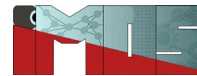
Implicit learning of the degradation parameters in the latent space



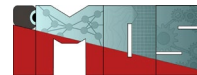




*RTE = relative temporal error

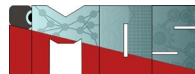


Integrating Expert Knowledge with Domain Adaptation for Unsupervised Fault Diagnosis

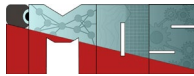


- Turbine Bearing Data
- Distinguish between 3 classes: healthy, inner race, outer race
- Without any faulty examples at training time

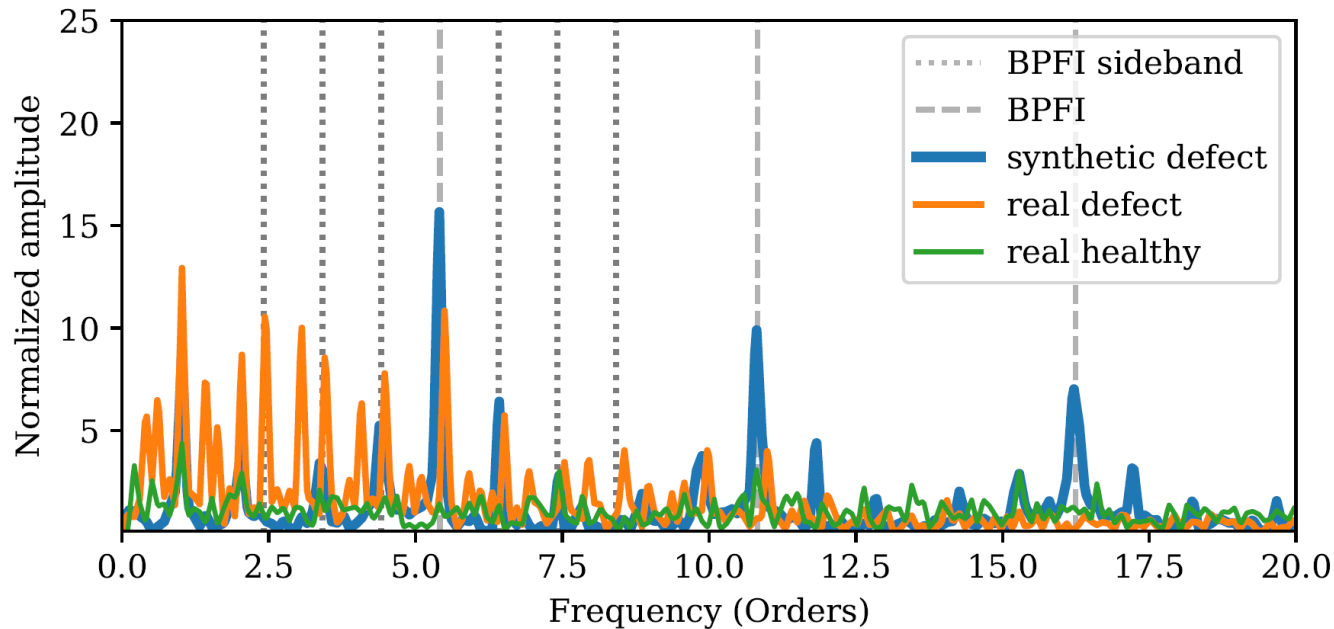


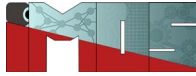


- Healthy data available
- No faulty data available at model development time
- Not just fault detection but also fault diagnostics required (distinguish between the different fault types)
- Developed models need to be tested on real faulty data
- Faulty data imbalanced
- Imbalance level unknown

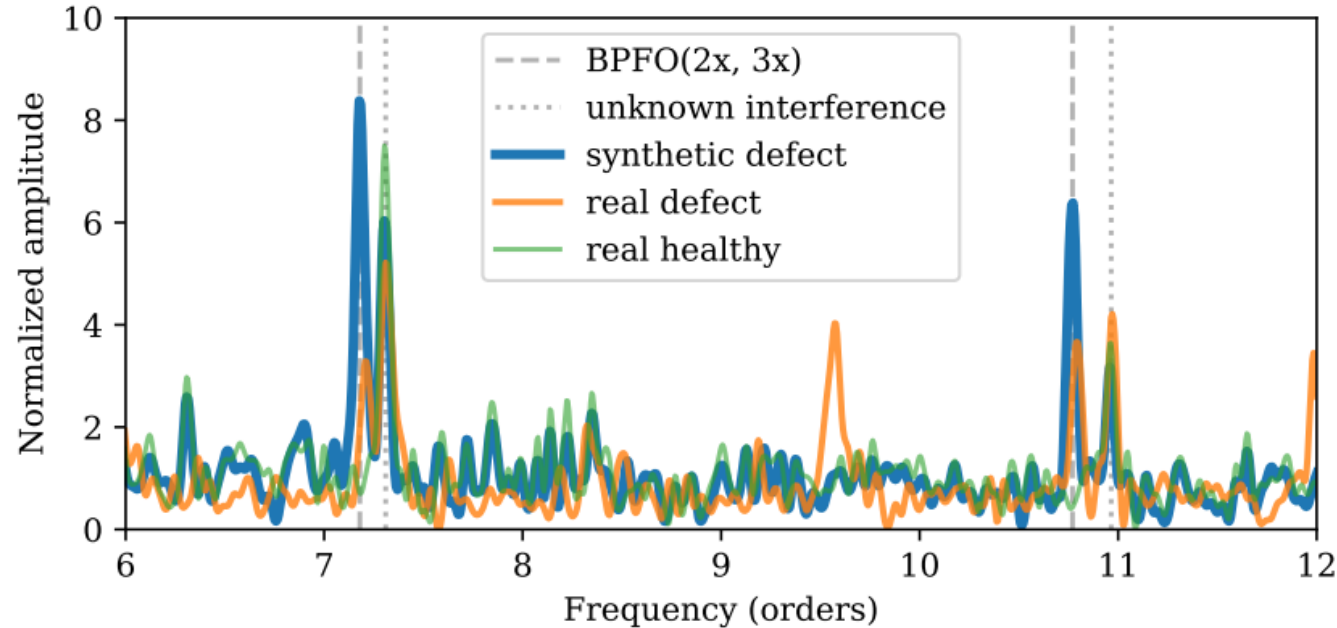


Normalized full-wave rectified envelope spectrum of an inner ring defect example with corresponding defect ball pass frequency

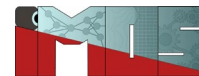




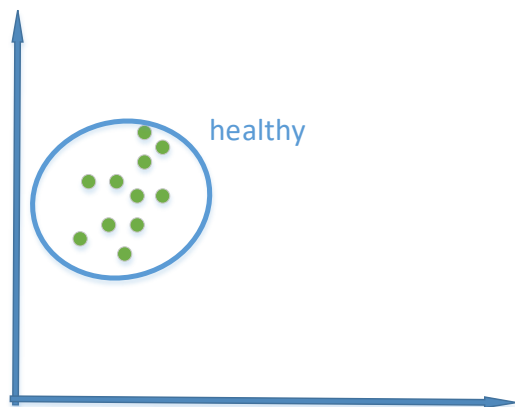
Normalized full-wave rectified envelope spectrum of an outer ring defect example with corresponding defect ball pass frequency



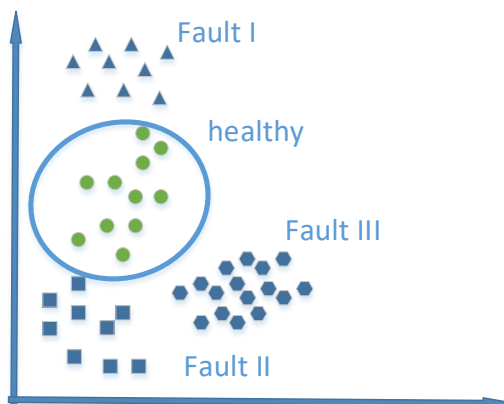
Wang, Q., C. Taal, O. Fink, Integrating Expert Knowledge with Domain Adaptation for Unsupervised Fault Diagnosis, IEEE Transactions on Instrumentation & Measurement



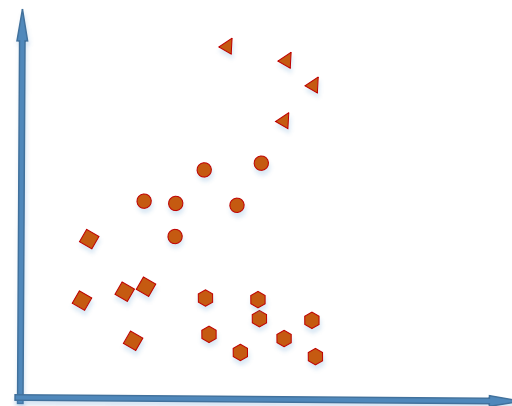
Source



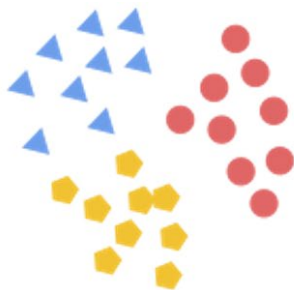
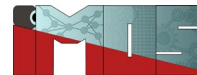
Source + synthetic faults



Target



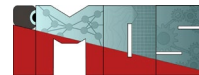
Challenges of DA for imbalanced datasets



Synthetic Source Domain



Real Target Domain



One life-time recording of a bearing



Early part can be safely regarded as healthy



Take out this healthy part



Superposition of healthy signals + defect-initiated pulse-train signal + randomness

Inject synthetic faults to the healthy samples. Based on domain expertise.



Outer race

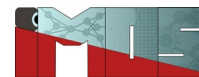
Inner race

Ball

Combine them we get our synthetic data



Naïve Synthetic2Real on imbalanced data: Toy example on CWRU



Source | syn

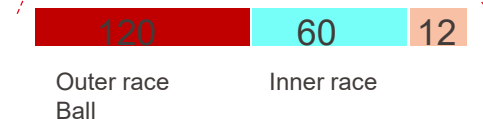


Target |
real



1. Four classes
2. Train only on synthetic data
3. Metric: Report average accuracy for all classes

$$(\text{Acc_healthy} + \text{Acc_fault1} + \text{Acc_fault2} + \text{Accu_fault3}) / 4$$



Source only Accuracy: 59.55%

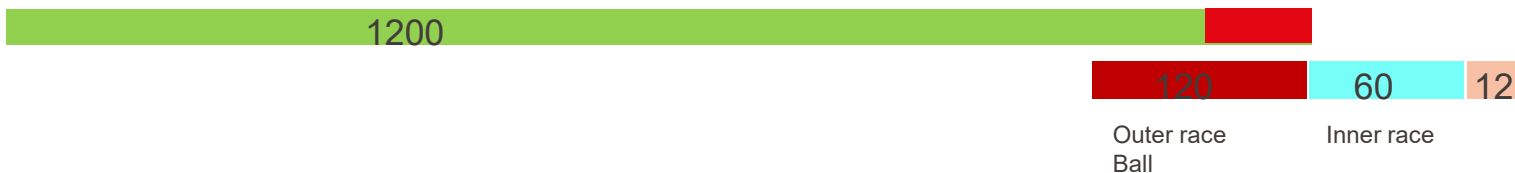
The synthetic data indeed contains information that helps the classification.

Adversarial Synthetic2Real on imbalanced data: Toy example on CWRU

Source | syn



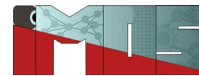
Target |
real



How about adversarial domain adaptation ?

Method	Source-only	Adversarial
Accuracy	59.55%	72.57%

What is the issue ? Imbalanced data in target.



Quick verification: What if we make the number of samples equal for target ?

Target Before:
exp1



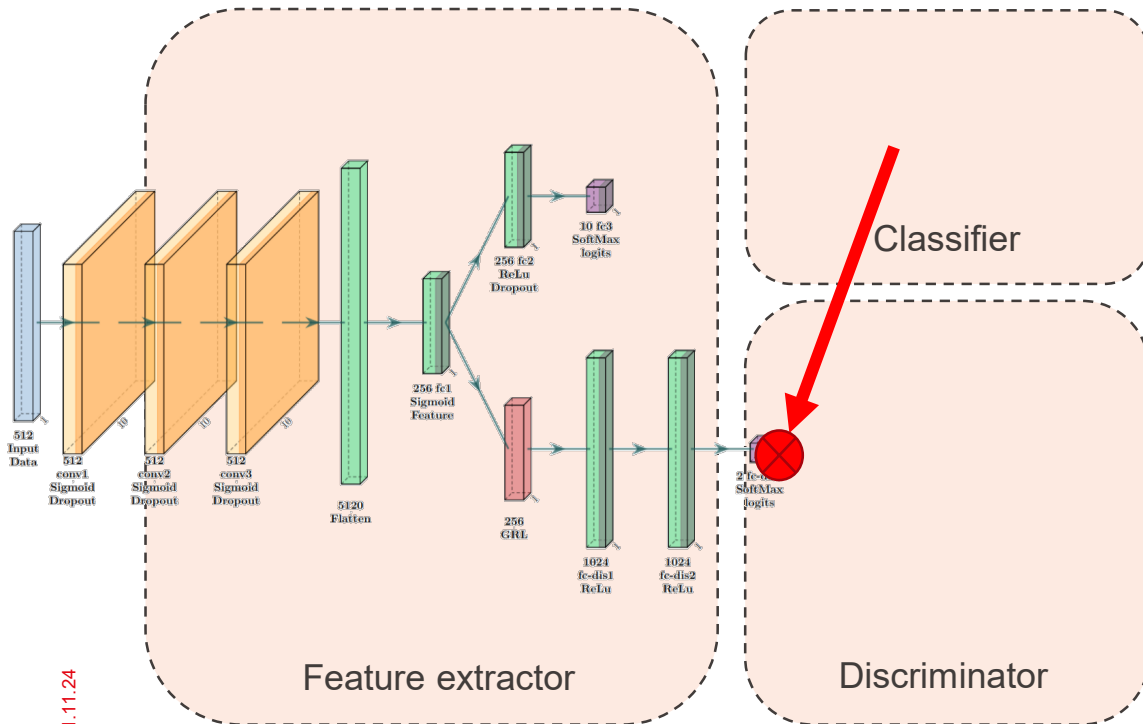
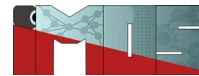
Modified
Target:
exp2



Method	Source-only	Exp1 Adversarial-imbalanced	Exp2 Adversarial-Balanced
Accuracy	59.55%	72.63%	82.59%

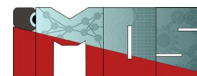
A big improvement on performance!
Simply by making it balanced!
But in reality we don't know the ground truth.

Step 1: How to let the discriminator learn better for the rare faults.

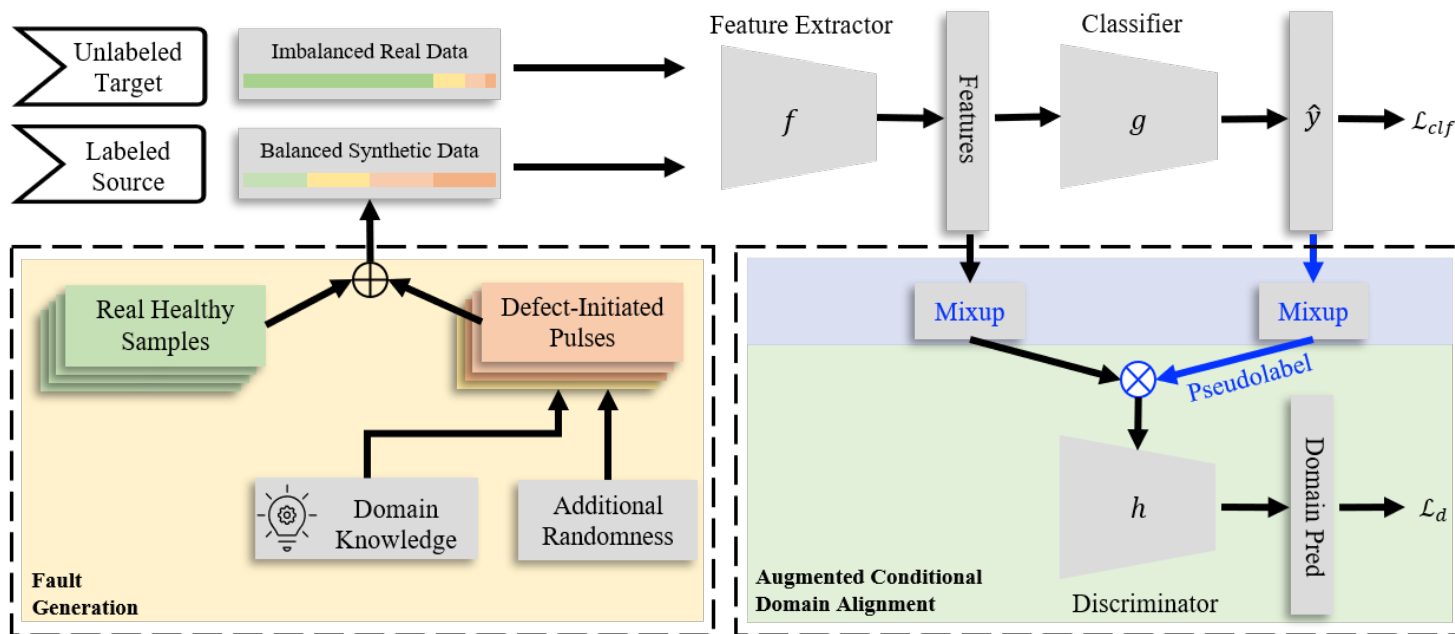
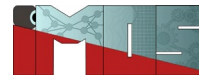


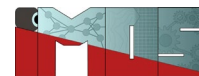
- Inspired by Conditional GAN and CDAN (conditional domain adaptation)
- Use pseudo label from the classifier and provide the class information to discriminator.

Step 2: Provide more support for the target conditioned distribution

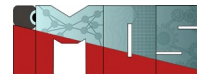


- Inspired by Mixup
- For features and pseudo-labels (in latent space not in input space)
- Performed separately for source and target
- This injects rare faults information to more samples in one batch



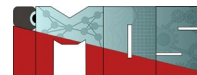


Method	Accuracy
Source only	59.55%
DANN	72.57%
Conditioned	75.38%
Conditioned + Mixup	82.29%



	20%	15%	10%	5%	1%
Baseline	59.55	59.55	59.55	59.55	59.55
DANN	82.04	79.77	78.30	74.96	71.05
Proposed	83.49	83.04	83.32	83.30	82.34

x%: For every 100 healthy samples, x samples for the rare fault class

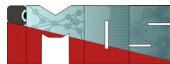


- Turbine Bearing Data from SKF
- 3 classes: Healthy, inner race, outer race
- Generated synthetic fault data from healthy
- There are much more outer race faults than inner race faults



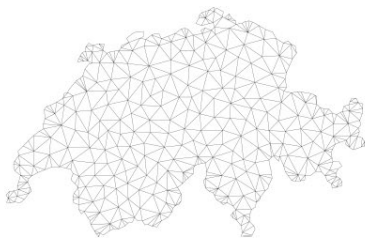
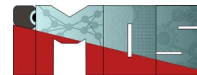
Method	Accuracy
Source only	60.85
DANN	64.47
Conditional (proposed)	68.28
Conditional+mixup(proposed)	70.76

Wang, Q., C. Taal, O. Fink, Integrating Expert Knowledge with Domain Adaptation for Unsupervised Fault Diagnosis, under review



Graph Neural Networks

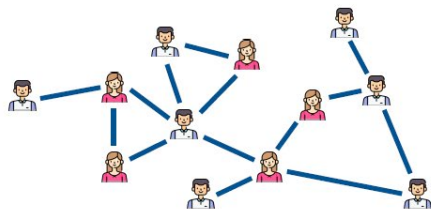
Graphs are everywhere



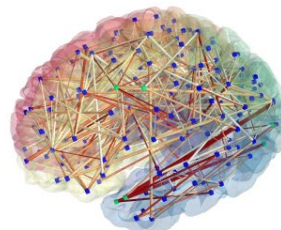
geographical network



traffic network



social network

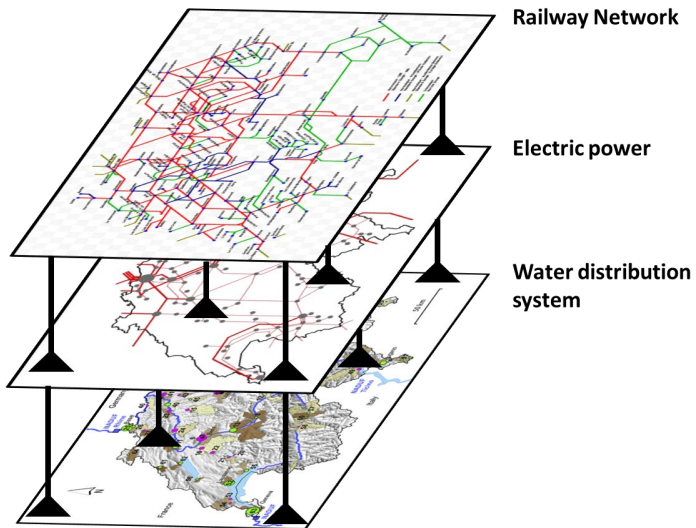
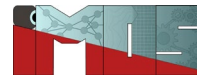


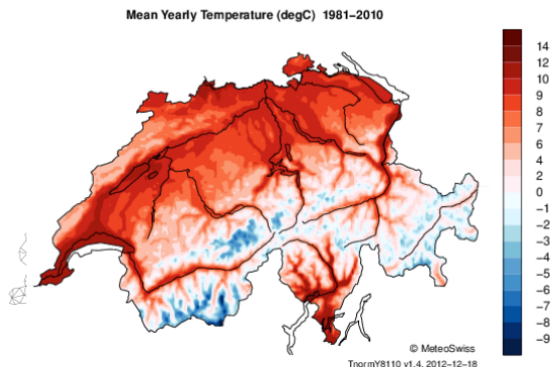
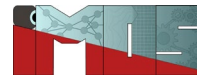
brain network

Graphs provide mathematical representation of networks

Source: P. Frossard

Infrastructure networks can be represented as graphs

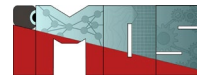




- nodes
 - geographical regions
- edges
 - geographical proximity between regions
- signal
 - temperature records in these regions

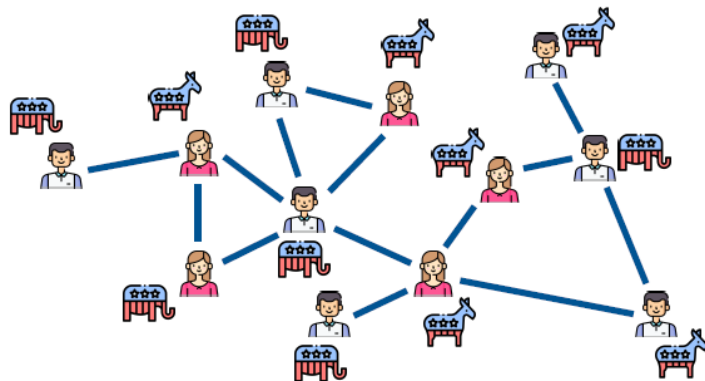
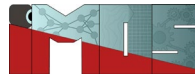
Source: P. Frossard

Examples of graph structured data



- nodes
 - road junctions
- edges
 - road connections
- signal
 - traffic congestion at junctions

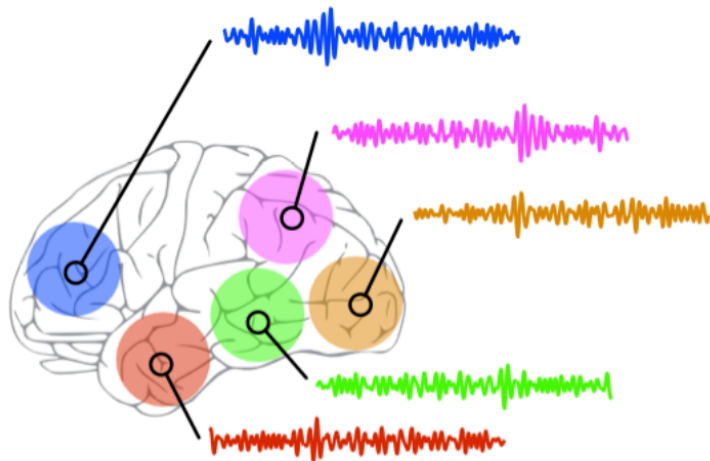
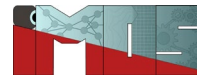
Source: P. Frossard



- nodes
 - individuals
- edges
 - friendship between individuals
- signal
 - political view

Source: P. Frossard

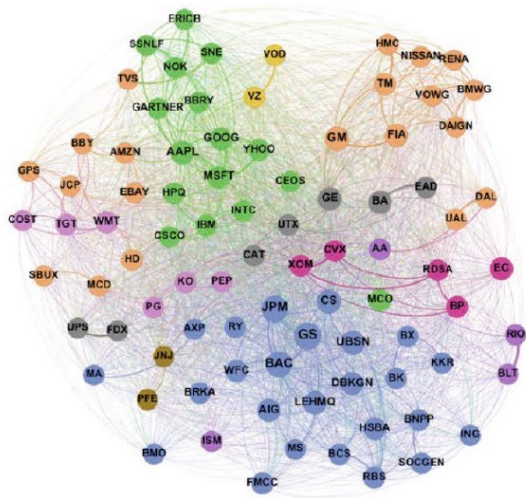
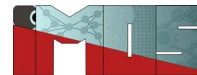
Examples of graph structured data



- nodes
 - brain regions
- edges
 - structural connectivity between brain regions
- signal
 - blood-oxygen-level-dependent (BOLD) time series

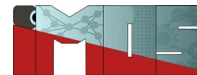
Source: P. Frossard

Examples of graph structured data



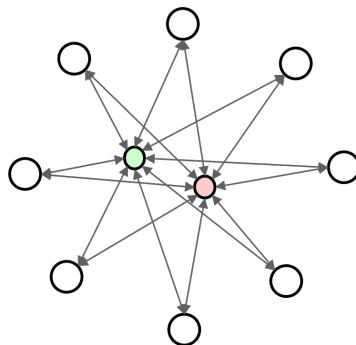
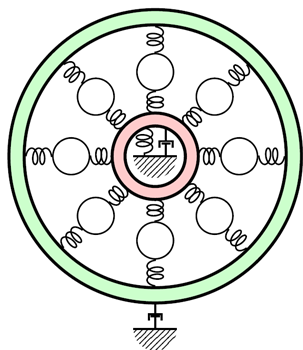
- nodes
 - companies
- edges
 - co-occurrence of companies in financial news
- signal
 - stock prices of these companies

Source: P. Frossard



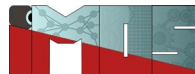
- Nodes: Sensors of a (bridge) sensor network)
- Edges: proximity of the sensors /similarity of the signals
- Signal: strain and / or accelerometer measurements

Bearing dynamics can be represented as graphs

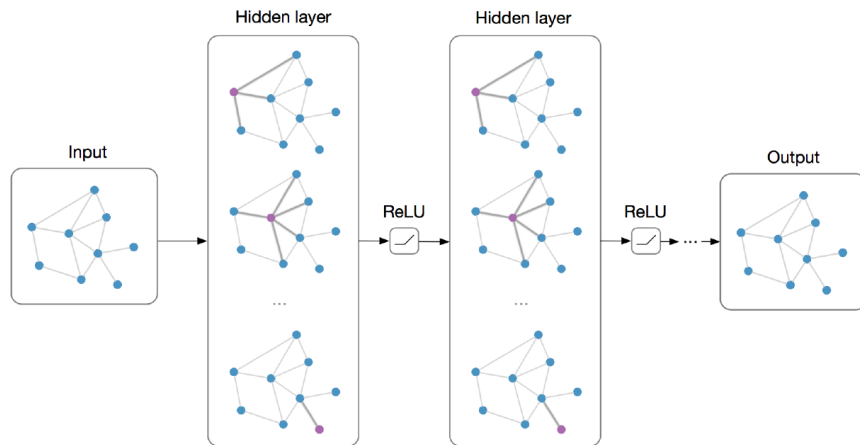
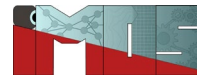


Sharma, V., Ravesloot, J., Taal, C. and Fink, O., 2023. Graph Neural Networks for Dynamic Modeling of Roller Bearing, PHM Society conference 2023

Task that can be solved with GNNs



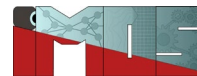
- (supervised) graph level classification
- Node classification
- Link prediction



Main Idea: Pass messages between pairs of nodes and agglomerate

Alternative Interpretation: Pass messages between nodes to refine node (and possibly edge) representations

Source: T. Kipf

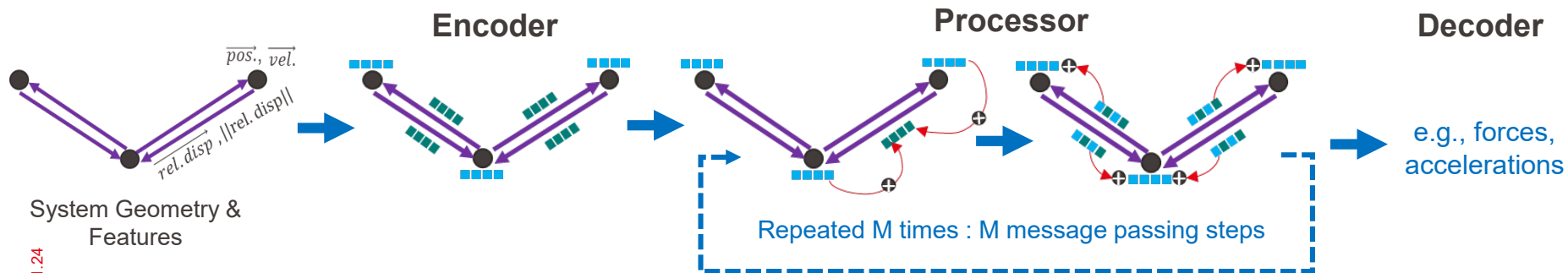


Example : Spring Mass Systems

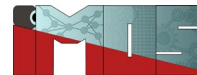
- Each node represents the mass
- Each edge represents the spring



GNN : Message Passing on Graphs

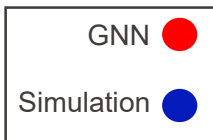


11.11.24



Example : Spring Mass Systems learned dynamics by GNN

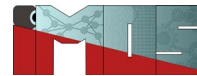
timestep = 25



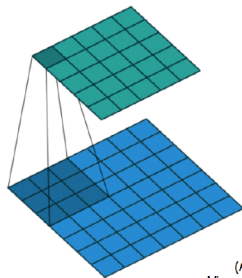
Train : 4, 5, 6, 7, 9, 10 masses
Test : 8 masses (**out of training**)

Source: V. Sharma

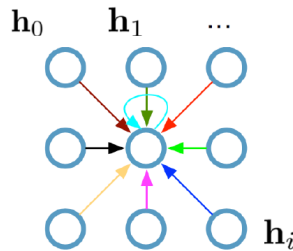
Recap: Convolutional Neural Networks (CNNs) on Grids



Single CNN layer with 3x3 filter:



(Animation by Vincent Dumoulin)



Update for a single pixel:

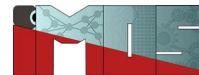
- Transform messages individually $\mathbf{W}_i \mathbf{h}_i$
- Add everything up $\sum_i \mathbf{W}_i \mathbf{h}_i$

$\mathbf{h}_i \in \mathbb{R}^F$ are (hidden layer) activations of a pixel/node

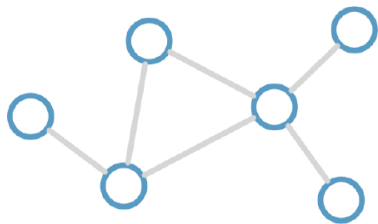
Full update:

$$\mathbf{h}_4^{(l+1)} = \sigma \left(\mathbf{W}_0^{(l)} \mathbf{h}_0^{(l)} + \mathbf{W}_1^{(l)} \mathbf{h}_1^{(l)} + \cdots + \mathbf{W}_8^{(l)} \mathbf{h}_8^{(l)} \right)$$

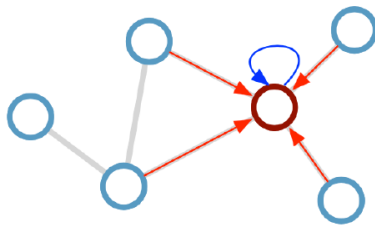
Source: T. Kipf



Consider this undirected graph:



Calculate update for node in red:



Desirable properties:

- Weight sharing over all locations
- Invariance to permutations
- Linear complexity $O(E)$
- Applicable both in transductive and inductive settings

Update rule:

$$\mathbf{h}_i^{(l+1)} = \sigma \left(\mathbf{h}_i^{(l)} \mathbf{W}_0^{(l)} + \sum_{j \in \mathcal{N}_i} \frac{1}{c_{ij}} \mathbf{h}_j^{(l)} \mathbf{W}_1^{(l)} \right)$$

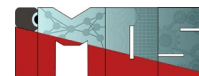
Scalability: subsample messages [Hamilton et al., NIPS 2017]

$\mathcal{N}_i$: neighbor indices

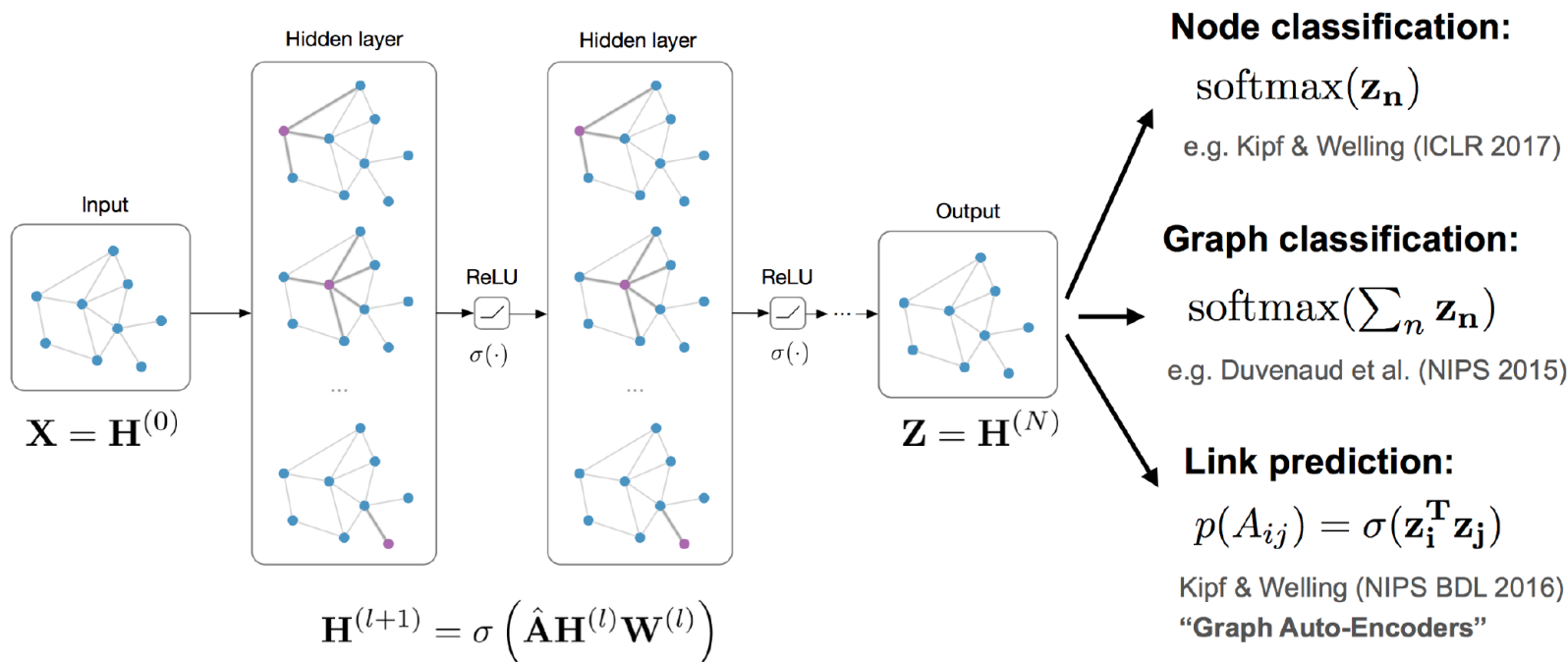
c_{ij} : norm. constant
(fixed/trainable)

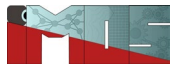
Source: T. Kipf

Classification and Link Prediction with GNNs / GCNs



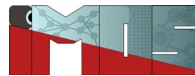
Input: Feature matrix $\mathbf{X} \in \mathbb{R}^{N \times E}$, preprocessed adjacency matrix $\hat{\mathbf{A}}$





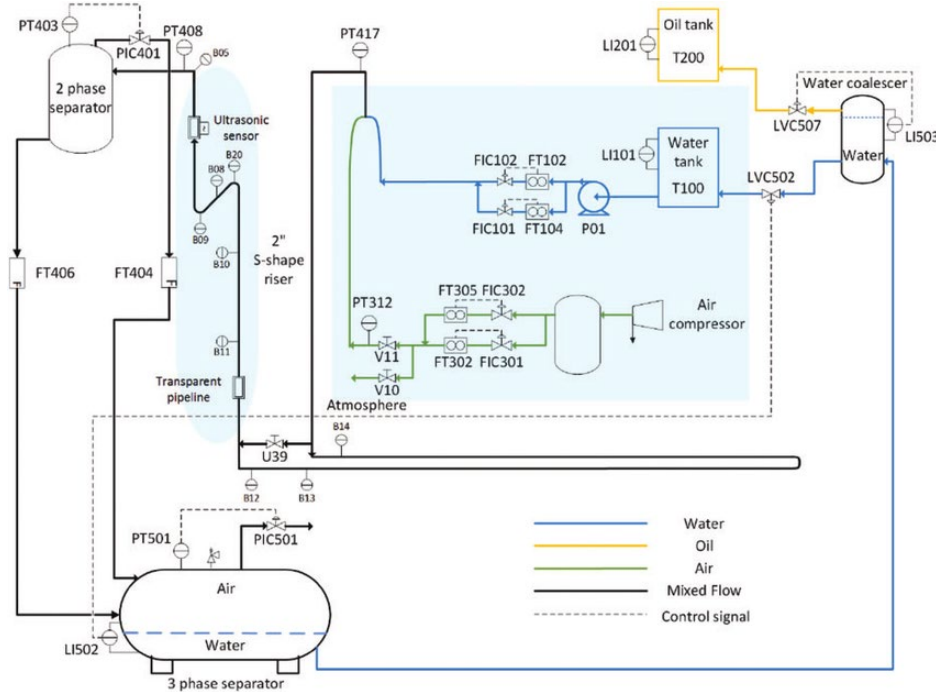
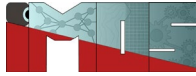
Example: Industrial IoT systems

Changing / evolving relationships between time series



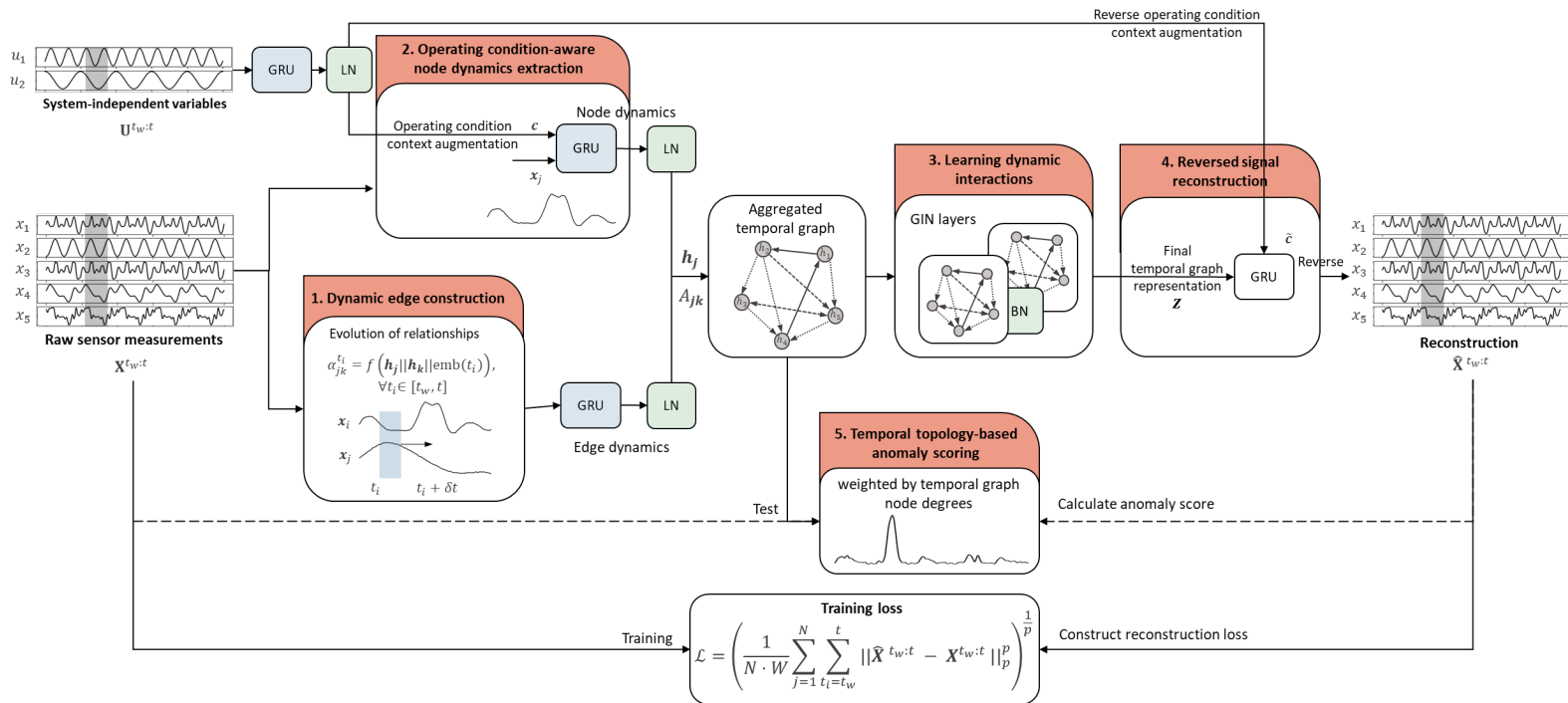
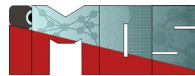
- Usually, graph topology between time series either given or derived once → static graph
- Changing environmental or operating conditions
- Impact of degradation
- Process optimization
- Maintenance
- ...

Anomaly detection in multi-flow facility

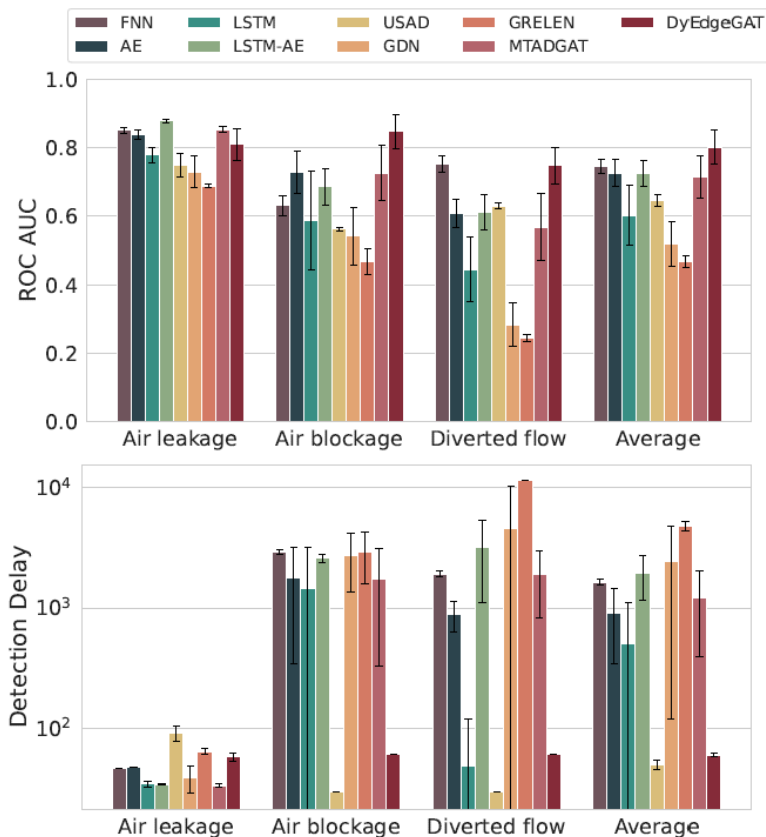
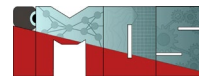


Source: Gedda, R., Beilina, L. and Tan, R., 2023. Change Point Detection for Process Data Analytics Applied to a Multiphase Flow Facility. *CMES-Computer Modeling in Engineering & Sciences*, 134(3).

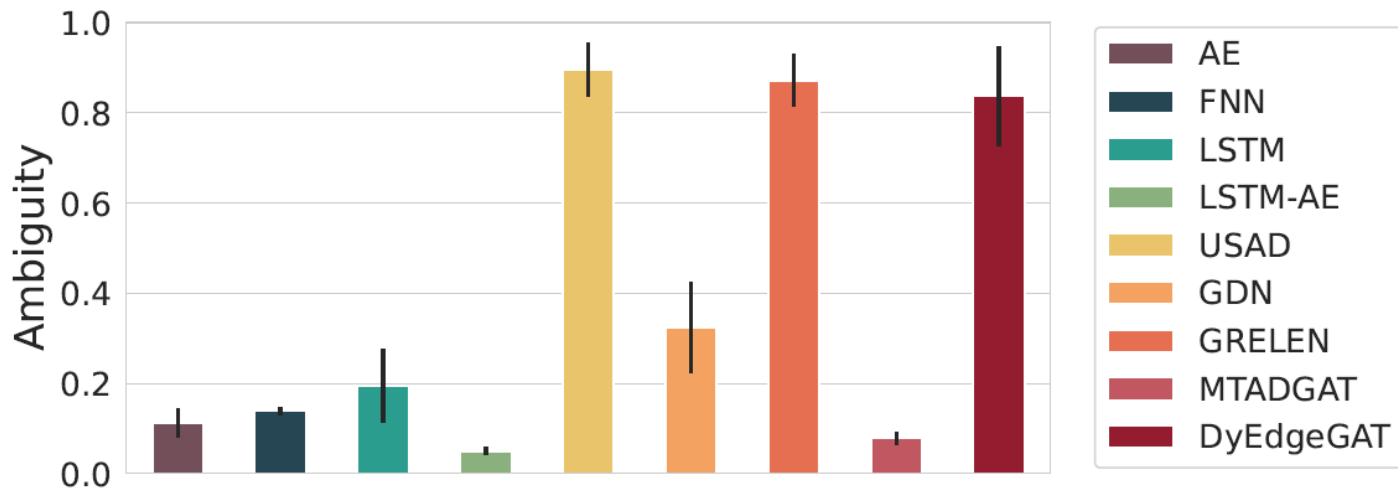
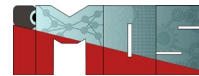
DyEdgeGAT: Dynamic Edge via Graph Attention for Early Fault Detection in IIoT Systems



EPFL Dynamic Edge via Graph Attention (DyEdgeGAT)

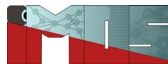


Zhao, M., & Fink, O. (2023). DyEdgeGAT: Dynamic Edge via Graph Attention for Early Fault Detection in IIoT Systems, IEEE Internet of Things Journal

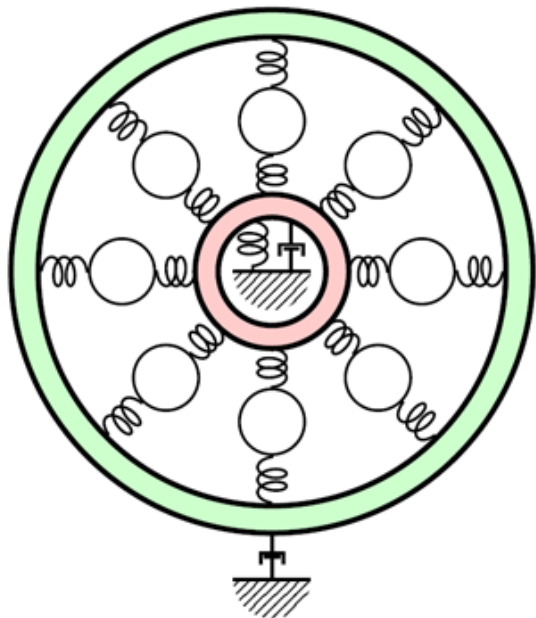


$$\text{Ambiguity} = 1 - 2 \cdot |\text{AUC} - 0.5|$$

Ambiguity quantifies the model's inability to differentiate between normal operations and novel conditions

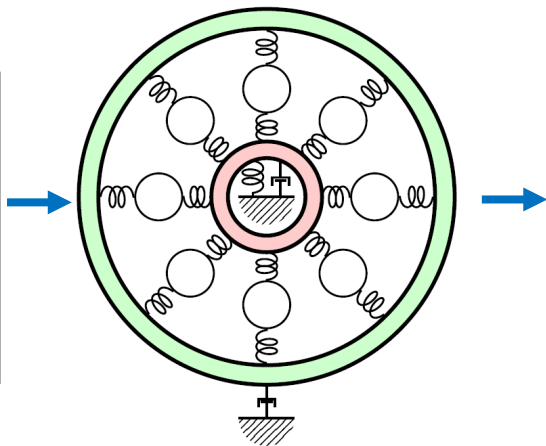
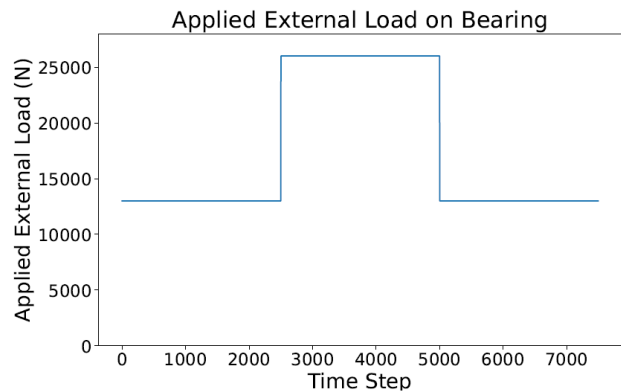
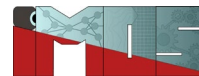


Example: Modelling bearing as a graph



- 2D dynamic lumped bearing model, (based on P. K. Gupta, 1979)
- Differential equations of motion
- Lundberg & Palmgren model for Hertzian contact
- N209 CRB bearing (line contacts)
- Assumptions: rigid rings, zero-mass rolling elements

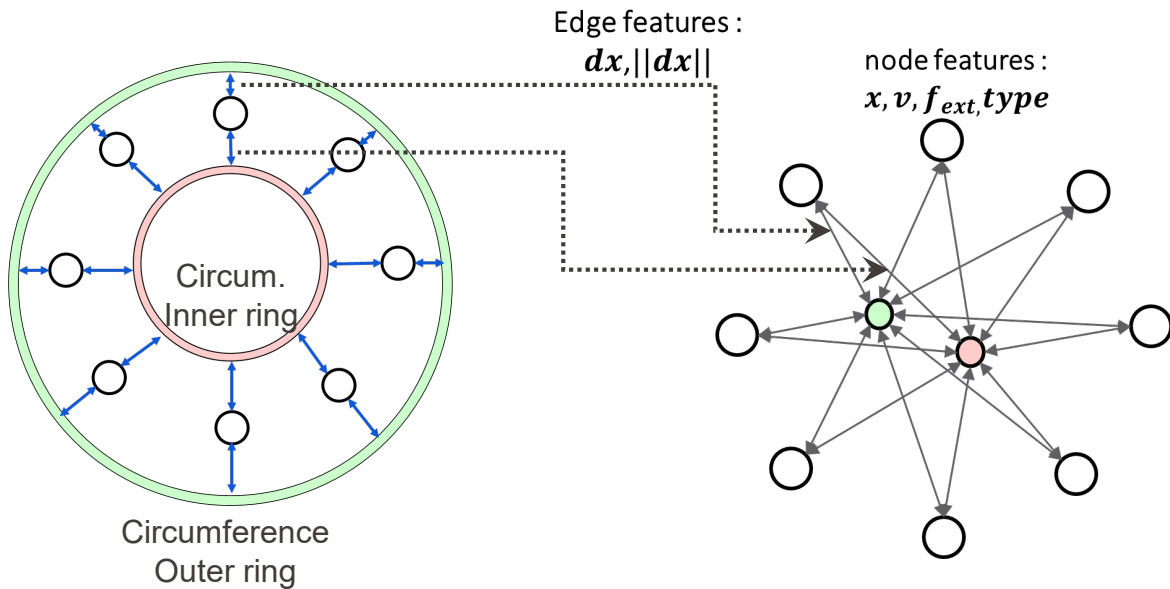
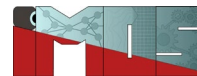
based on simple model but theory
also applies to complex models!



Positions $\vec{x}_i$
Velocities $\vec{v}_i$
Internal loads $\vec{f}_i$

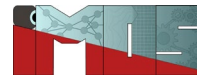
- Load changes to generate dynamic step responses
- [1-20] kN OR loads, [13, 14, 15, 16] rollers
- (Rotation is not included yet)

GNN Inputs and Outputs



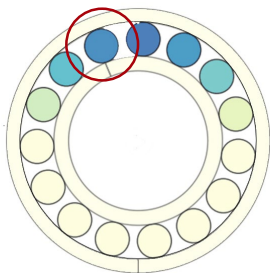
Sharma, V., Ravesloot, J., Taal, C. and Fink, O., 2023. Graph Neural Networks for Dynamic Modeling of Roller Bearing, PHM Society conference 2023

Results: Generalizability

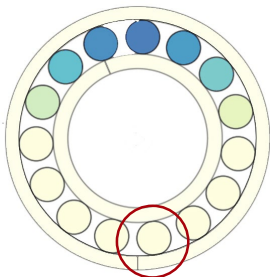
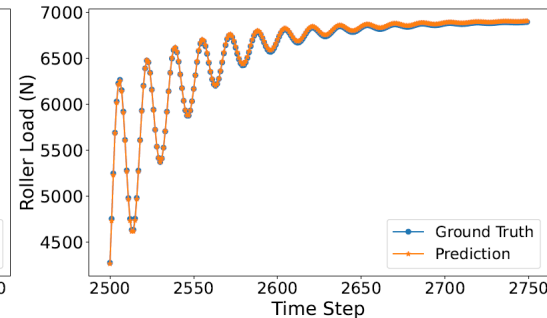
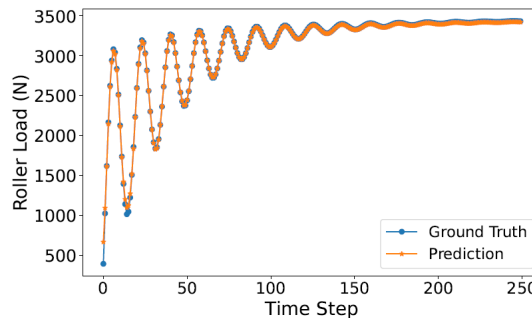


Training : SKF N209 CRB (13, 14, 16 rollers)

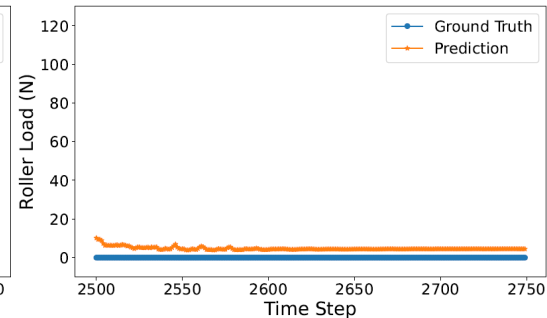
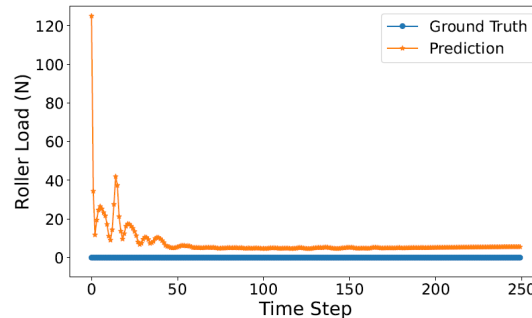
Testing: 15 Rollers, 13kN

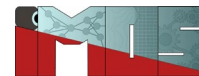


Predicted and True Loads on the Top Roller (# 8) at each time-step

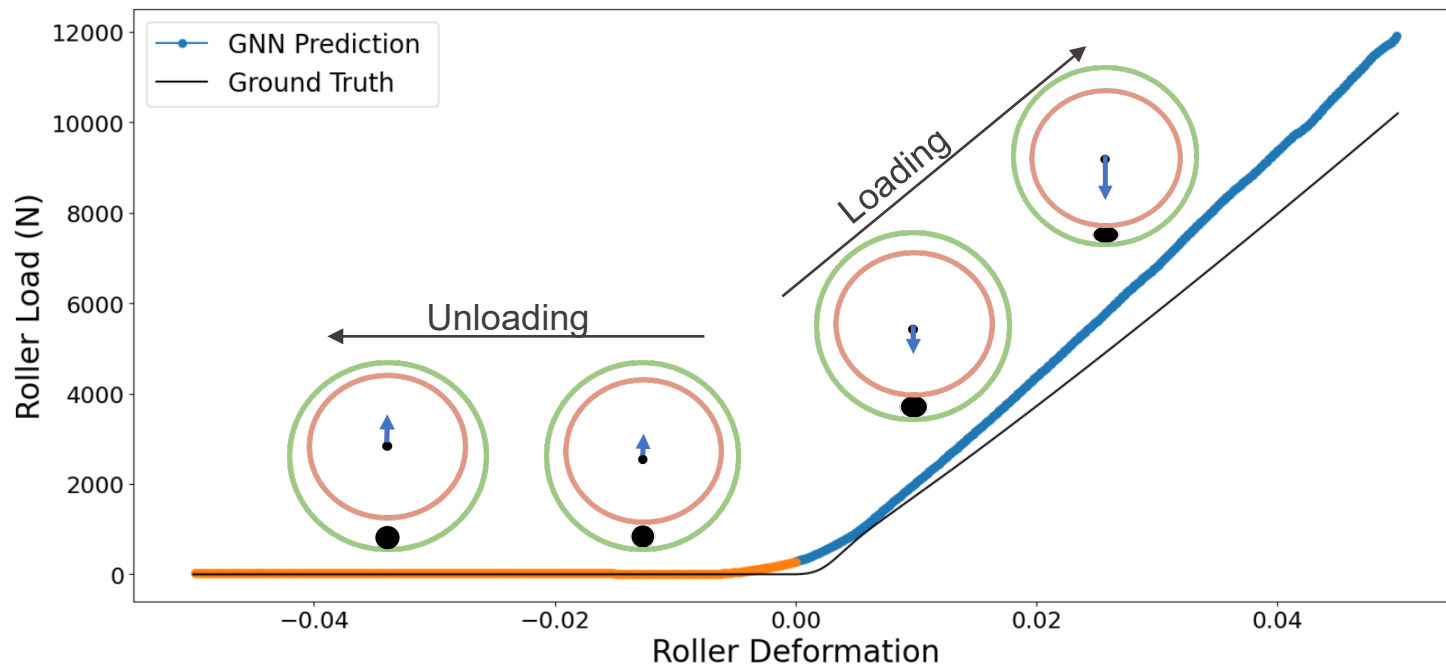


Predicted and True Loads on the Bottom Roller (# 0) at each time-step





Predicted Load vs Roller Deformation for Bottom Roller (#0)



- **GNN can infer the unloading behavior without direct training. (Conventional Networks cannot infer this behavior)**