

Introduction to Chemical Engineering

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Office hours: Mondays 16h-19h (CH H4 625) or schedule by email

Fridays, 14h15 - 17h00

2024-2025

Course Schedule

Date	Subject
13-Sep	1. Fundamentals of Material Balances 1.1. Process definition and classification 1.2. Material balance calculations
20-Sep	1.3. Balances on multiple-unit processes
27-Sep	Review on Mass Balances (non-reactive)
04-Oct	1.4. Chemical reaction stoichiometry 1.5.1 Balances on reactive processes (part 1)
11-Oct	1.5.2 Balances on reactive processes (part 2) 1.6. Balances on multiple unit reactive processes Review on Mass Balances (non-reactive & reactive)
18-Oct	2. Fundamentals of Energy and Energy Balances 2.1. Energy balances on closed systems 2.2. Open systems at steady state 3. Balances on Non-Reactive Processes 3.1. Energy balance calculation 3.2. Changes in Pressure, Temperature, Phases
01-Nov	4. Balances on Reactive Processes 4.1. Introduction to the Enthalpy of Reaction 4.2. Heat of Reaction Method 4.3. Heat of Formation Method 4.4 General Procedure to solve energy balance in reactive systems
08-Nov	Review on Balances on Non-Reactive Processes Problems: Mass and Energy Balances on non-Reactive Systems
15-Nov	Midterm Exam: Mass & Energy Balances non-Reactive Systems
22-Nov	Review Midterm

Date	Subject
29-Nov	Review on Heat of Reaction vs Heat of Formation Methods 4.5 Hess's Law to compute the Heat of Reaction 4.6 Heat of Combustion
06-Dec	5. Energy balances on mixing processes 5.1 Distinction between ideal and real solutions 5.2 Heat of Solution
13-Dec	Review and Study Session • Material balances • Energy balances

Recommended textbook:

Elementary Principles of Chemical Processes,
Richard M. Felder & Ronald W. Rousseau

Session IX: Friday 13 December 2024

During this session, we will review the following concepts

1. Material balances
2. Energy balances

Material Balances

Material Balances: overview

It all starts with the mother of all equations:

$$\begin{array}{ccccccccc} \textbf{Input} & + & \textbf{generation} & - & \textbf{output} & - & \textbf{consumption} & = & \textbf{accumulation} \\ \left(\begin{array}{c} \text{Entering} \\ \text{through} \\ \text{boundaries} \end{array} \right) & & \left(\begin{array}{c} \text{Produced} \\ \text{in the} \\ \text{system} \end{array} \right) & & \left(\begin{array}{c} \text{Leaving} \\ \text{through} \\ \text{boundaries} \end{array} \right) & & \left(\begin{array}{c} \text{Consumed} \\ \text{within} \\ \text{system} \end{array} \right) & & \left(\begin{array}{c} \text{Build up} \\ \text{within} \\ \text{system} \end{array} \right) \end{array}$$

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(Almost) all the systems we study represent **steady-state continuous processes**:

$$\begin{array}{ccccccccc} \textbf{Input} & + & \textbf{generation} & - & \textbf{output} & - & \textbf{consumption} & = & \mathbf{0} \\ \left(\begin{array}{c} \text{Entering} \\ \text{through} \\ \text{boundaries} \end{array} \right) & & \left(\begin{array}{c} \text{Produced} \\ \text{in the} \\ \text{system} \end{array} \right) & & \left(\begin{array}{c} \text{Leaving} \\ \text{through} \\ \text{boundaries} \end{array} \right) & & \left(\begin{array}{c} \text{Consumed} \\ \text{within} \\ \text{system} \end{array} \right) & & \end{array}$$

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From there, we have seen 2 possible methods:

Species Material Balances

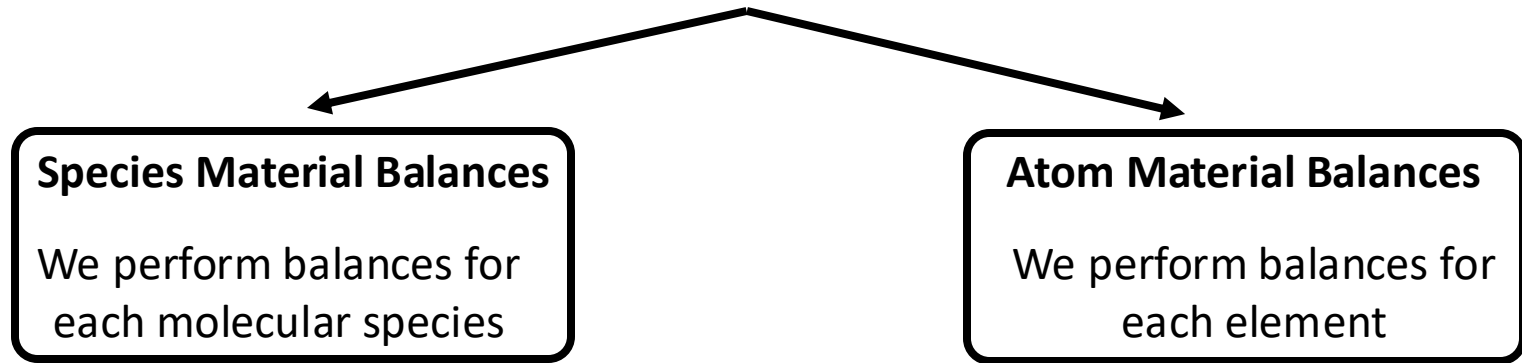
We perform balances for each molecular species

Atom Material Balances

We perform balances for each element

Material Balances: species vs atom balances

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We perform balances for each element

Non-reactive systems:

$$\text{input} + \text{generated} - \text{output} - \text{consumed} = 0$$

$$\text{input} - \text{output} = 0$$

$$\text{input} = \text{output}$$

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$$\text{input} + \text{generated} - \text{output} - \text{consumed} = 0$$

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$$\boxed{\text{input} = \text{output}}$$

Atom Material Balances

We perform balances for each element

Reactive systems:

$$\text{input} + \text{generated} - \text{output} - \text{consumed} = 0$$

$$\text{input} - \text{output} + \text{generated} - \text{consumed} = 0$$

$$\text{input} - \text{output} + (\text{generated} - \text{consumed}) = 0$$

$$\text{input} - \text{output} + \text{reacted} = 0$$

$$\boxed{\text{input} + \text{reacted} = \text{output}}$$

Material Balances: species vs atom balances

From there, we have seen 2 possible methods:

Species Material Balances

We perform balances for each molecular species

Non-reactive systems:

input = output

$$n_{CH_4,in} = n_{CH_4,out}$$

Atom Material Balances

We perform balances for each element

Reactive systems:

input + **reacted** = output

$$n_{CH_4,in} + \nu_{CH_4} \cdot \xi = n_{CH_4,out}$$

Reactant:

$$\xi < 0$$

consumed

Product:

$$\xi > 0$$

generated

Material Balances: species vs atom balances

From there, we have seen 2 possible methods:

Species Material Balances

We perform balances for each molecular species

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Non-reactive systems:

input = output

$$n_{C,in} = n_{C,out}$$

Reactive systems:

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Material Balances: species vs atom balances

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Non-reactive systems:

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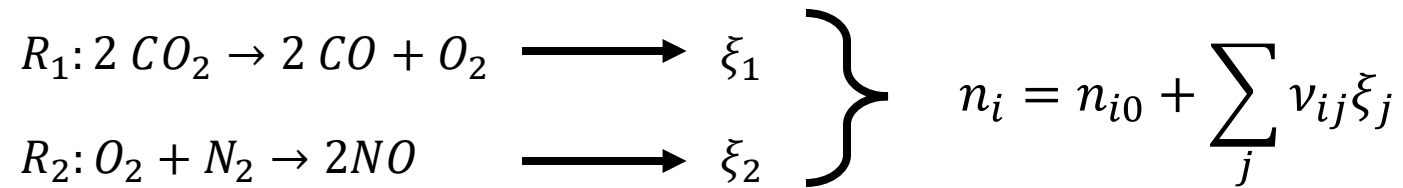
input = output

$$n_{C,in} = n_{C,out}$$

- No consideration of the extent of reaction with atom balance
- However, do not forget to multiply by the stoichiometric coefficient, e.g, in 1 mole of CH₄, there is 1 mole of Carbon BUT 4 moles of Hydrogen!

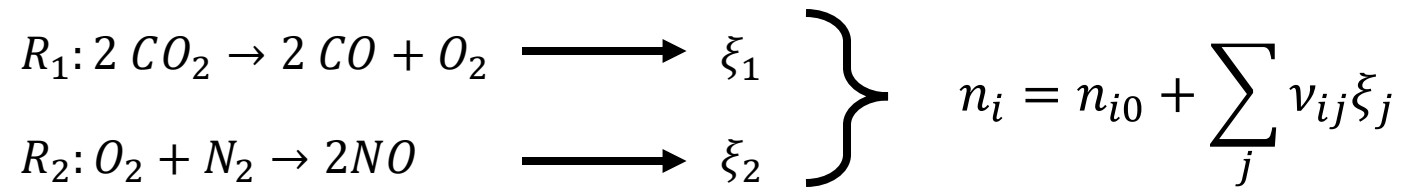
Material Balances: Considerations on Reactive Systems

Multiple reactions $\rightarrow$ multiple extents of reactions (species material balance)



Material Balances: Considerations on Reactive Systems

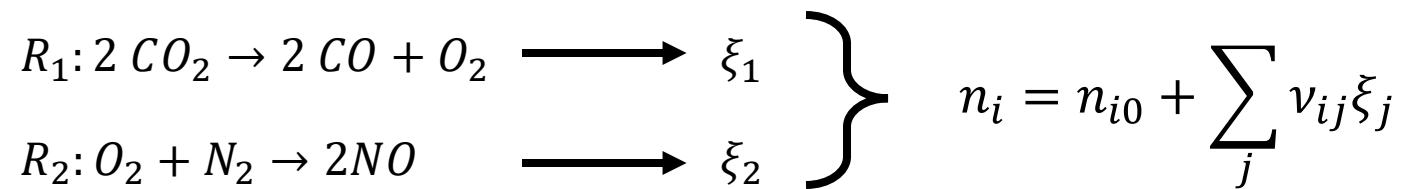
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If 2 reactions or more, it is generally easier to go with atomic material balance method

Material Balances: Considerations on Reactive Systems

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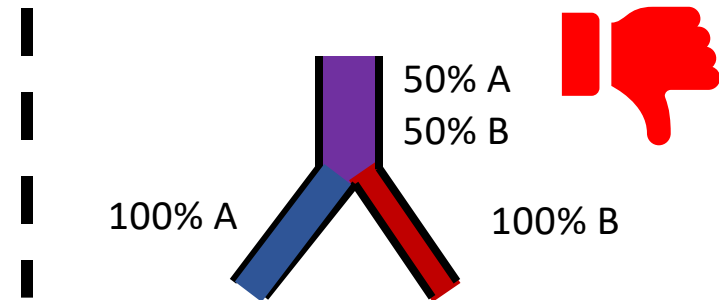
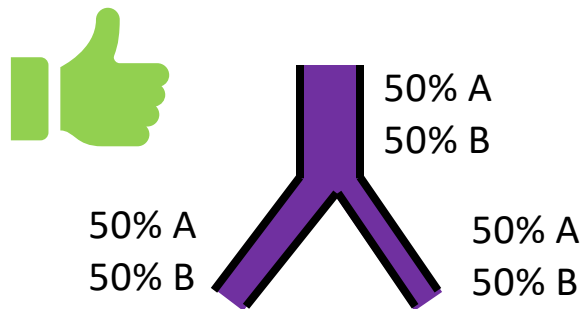


If 2 reactions or more, it is generally easier to go with atomic material balance method

In **reactive systems, moles of species are not conserved** (look at reaction 1, we start with a total of 2 moles (CO_2) and ends up with a total of 3 moles (2 moles CO and 1 mole O_2). HOWEVER, the moles of elements are conserved $\rightarrow$ if **we use the molecular species balance method, do not forget to convert the moles to mass when solving your material balances!**

Material Balances: General Considerations

At a splitting point, the composition of the stream is maintained (unless mentioned otherwise)



Material Balances: Limiting and Excess Reactants

Limiting reactant in reactive process = reactant that would be completely consumed if the reaction proceeded to completion.

All other reactants must either be fed in (1) stoichiometric proportion to the limiting reactant (the feed rates are in the ratio of the stoichiometric coefficients) or (2) in excess of the limiting reactant (in greater than stoichiometric proportion to it).



$$\% \text{ excess} = \frac{\text{amount fed} - \text{amount theoretically required}}{\text{amount theoretically required}}$$

Material Balances: Procedure for Calculations

1. Choose **as basis of calculation** an amount or flow rate of one of the process streams
 1. Basis can already be given in the problem
 2. If no stream amount or flow rate is specified, take as a basis an arbitrary amount or flow rate of a stream with known composition
2. **Draw a flowchart** and fill in all known variable values, including the basis of calculation, then label the unknown stream variables on the chart
3. Express what the **problem statement asks you** to determine in terms of the labeled variables
4. If you are given mixed mass and mole units for a stream, **convert all quantities to one basis or the other.**
5. OPTIONNAL: Perform a degree-of-freedom analysis
6. OPTIONNAL: If the number of unknowns equals the number of equations relating them, write the equation in an efficient order (minimizing simultaneous equations), and circle the variables for which you will solve
7. **Solve the equations**
8. **Calculate the quantities requested in the problem statement** if they have not already been calculated
9. OPTIONNAL: Scale if you chose a different basis than the one initially suggested.

Energy Balances

Energy Balances: overview

Again, with the mother of all equations:

$$E_{\text{accumulated}} = E_{\text{input}} - E_{\text{output}} + E_{\text{gen}} + E_{\text{transferred}}$$

Where $E_{\text{transferred}} = Q - W$

Conventions:

- $Q > 0$ when heat is transferred **from the surrounding to the system**
- $W > 0$ when work is **done by the system on the surroundings** *

* The opposite convention is sometimes used. The choice is arbitrary, if it is used consistently

Energy Balances: overview

Again, with the mother of all equations:

$$E_{\text{accumulated}} = E_{\text{input}} - E_{\text{output}} + E_{\text{gen}} + E_{\text{transferred}}$$

Closed

$$\Delta U + \Delta E_k + \Delta E_p = Q - W$$

- Δ : final – initial

Open

$$\Delta \dot{H} + \Delta \dot{E}_k + \Delta \dot{E}_p = \dot{Q} - \dot{W}_s$$

- Δ : output – input

Energy Balances: overview

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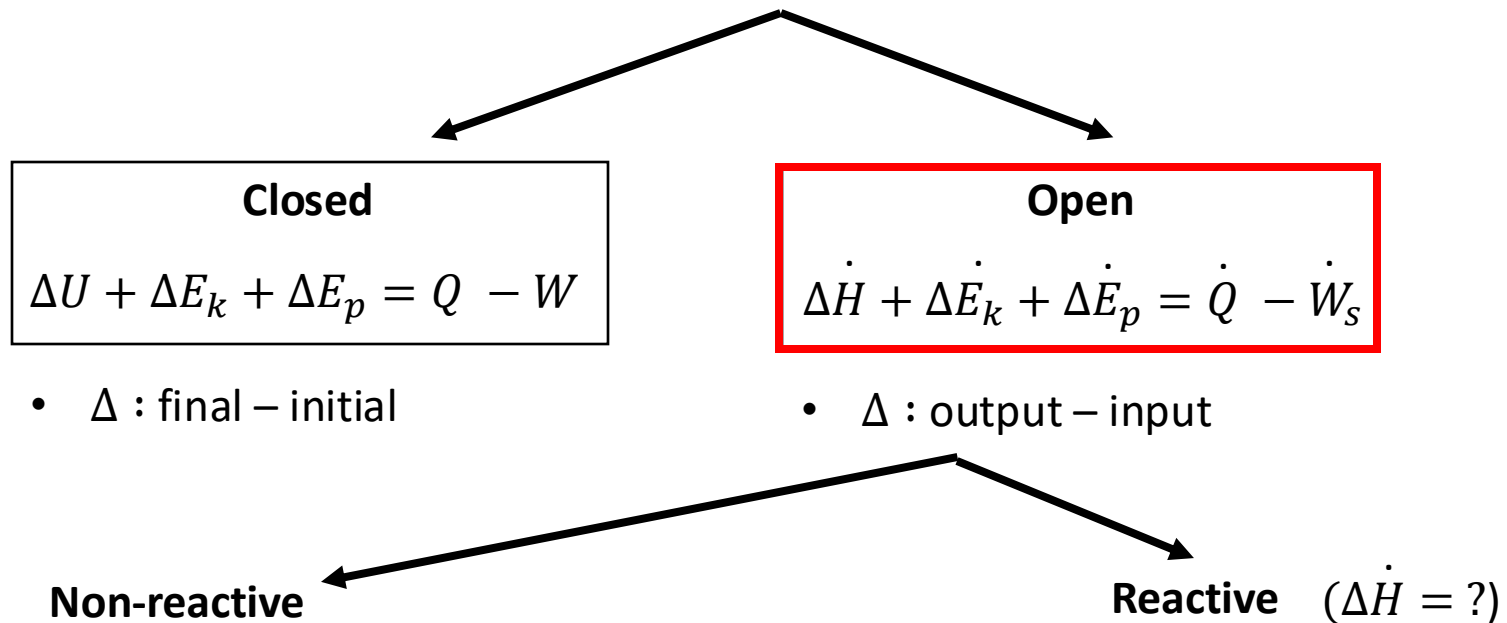
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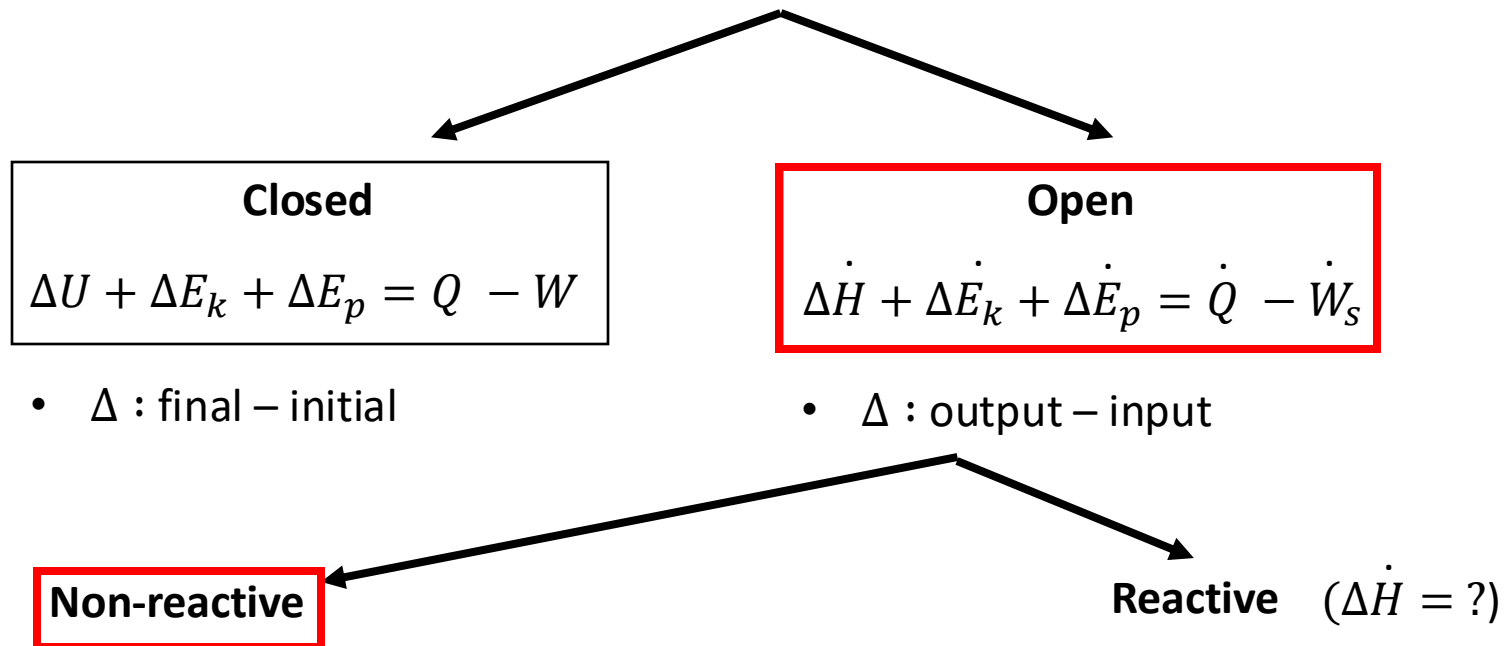
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Energy Balances: overview

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Reference state

Arbitrarily designate a reference state for substance at which $\hat{U}$ or $\hat{H}$ is declared to equal zero.

Tabulate $\hat{U}$ or $\hat{H}$ for the substance relative to the reference state

Energy Balances: Hypothetical Process Paths

In the systems we study, there are internal energy and **enthalpy changes associated with key processes**. We are specifically interested in the following:

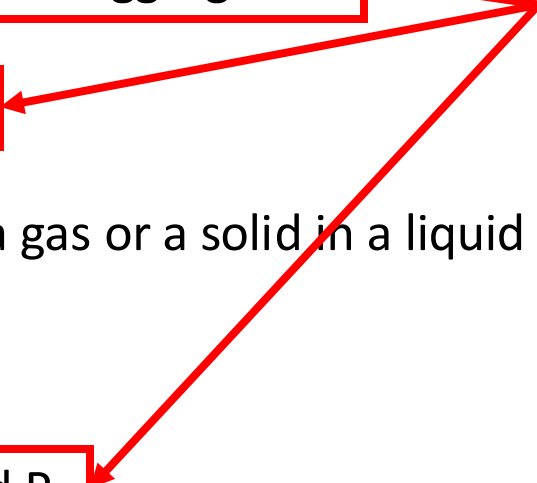
- Changes in P at constant T and state of aggregation
- Changes in T at constant P and state of aggregation
- Phase changes at constant T and P
- Mixing of 2 liquids or dissolving of a gas or a solid in a liquid at constant T and P
- Chemical reaction at constant T and P

Energy Balances: Hypothetical Process Paths

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- Changes in P at constant T and state of aggregation *
- Changes in T at constant P and state of aggregation
- Phase changes at constant T and P
- Mixing of 2 liquids or dissolving of a gas or a solid in a liquid at constant T and P **
- Chemical reaction at constant T and P

The ones you are expected to know



* For the processes and species seen in this class, we can neglect the enthalpy changes associated with changes in P(ressure).

** Enthalpy changes due to mixing were briefly covered in the last lecture. These will not be subject to examination

Changes in T at constant P and state of aggregation

There are 2 ways to calculate the enthalpy change associated to a change of temperature from T_1 (initial temperature) to T_2 (final temperature).

Let's take an example: 15 kmol/min of air is cooled from 430 C to 100C. Calculate the required heat removal rate.

Changes in T at constant P and state of aggregation

There are 2 ways to calculate the enthalpy change associated to a change of temperature from T1 (initial temperature) to T2 (final temperature).

Let's take an example: 15 kmol/min of air is cooled from 430 C to 100C. Calculate the required heat removal rate.

Most common (harder) way: Integrate the heat capacity formula from table B2

$$\Delta \hat{H} \text{ (kJ/mol)} = \int_{430^{\circ}\text{C}}^{100^{\circ}\text{C}} C_p(T) dT$$

$$C_p(T) = 0.02894 + (0.4147 \times 10^{-5})T + (0.3191 \times 10^{-8})T^2 - (1.965 \times 10^{-12})T^3$$

The integral expands to:

$$\Delta \hat{H} = \left[0.02894(T) + \frac{0.4147 \times 10^{-5}}{2}(T^2) + \frac{0.3191 \times 10^{-8}}{3}(T^3) - \frac{1.965 \times 10^{-12}}{4}(T^4) \right]_{430^{\circ}\text{C}}^{100^{\circ}\text{C}}$$

Plugging in the limits of integration ($T = 100^{\circ}\text{C}$ and $T = 430^{\circ}\text{C}$):

$$\Delta \hat{H} = \left[0.02894(100 - 430) + \frac{0.4147 \times 10^{-5}}{2}(100^2 - 430^2) + \frac{0.3191 \times 10^{-8}}{3}(100^3 - 430^3) - \frac{1.965 \times 10^{-12}}{4}(100^4 - 430^4) \right]$$

This evaluates to:

$$\Delta \hat{H} = (-9.5502 - 0.3627 - 0.0835 + 0.0167) \text{ kJ/mol} = -9.98 \text{ kJ/mol.}$$

Changes in T at constant P and state of aggregation

There are 2 ways to calculate the enthalpy change associated to a change of temperature from T1 (initial temperature) to T2 (final temperature).

Let’s take an example: 15 kmol/min of air is cooled from 430 C to 100C.
Calculate the required heat removal rate.

Easy way (not always possible): Use tabulated enthalpies (with linear interpolation)

Initial

Final

$$\left\{ \begin{aligned} \hat{H}(400\text{ C}) &= 11.24 \frac{\text{kJ}}{\text{mol}} \\ \hat{H}(430\text{ C}) &= 11.24 + 0.3 (14.37 - 11.24) = 12.17 \\ \hat{H}(500\text{ C}) &= 14.37 \frac{\text{kJ}}{\text{mol}} \end{aligned} \right.$$

$$\left\{ \begin{aligned} \hat{H}(100\text{ C}) &= 2.19 \frac{\text{kJ}}{\text{mol}} \end{aligned} \right.$$

$$\Delta \hat{H} = \widehat{H}_{final} - \widehat{H}_{initial} = 2.19 - 12.17 = -9.98 \frac{\text{kJ}}{\text{mol}}$$

Table B.8 Specific Enthalpies of Selected Gases: SI Units

$\hat{H}(\text{kJ/mol})$							
Reference state: Gas, $P_{\text{ref}} = 1 \text{ atm}$, $T_{\text{ref}} = 25^\circ\text{C}$							
T	Air	O ₂	N ₂	H ₂	CO	CO ₂	H ₂ O
0	-0.72	-0.73	-0.73	-0.72	-0.73	-0.92	-0.84
25	0.00	0.00	0.00	0.00	0.00	0.00	0.00
100	2.19	2.24	2.19	2.16	2.19	2.90	2.54
200	5.15	5.31	5.13	5.06	5.16	7.08	6.01
300	8.17	8.47	8.12	7.96	8.17	11.58	9.57
400	11.24	11.72	11.15	10.89	11.25	16.35	13.23
500	14.37	15.03	14.24	13.83	14.38	21.34	17.01
600	17.55	18.41	17.39	16.81	17.57	26.53	20.91
700	20.80	21.86	20.59	19.81	20.82	31.88	24.92
800	24.10	25.35	23.86	22.85	24.13	37.36	29.05
900	27.46	28.89	27.19	25.93	27.49	42.94	33.32
1000	30.86	32.47	30.56	29.04	30.91	48.60	37.69
1100	34.31	36.07	33.99	32.19	34.37	54.33	42.18
1200	37.81	39.70	37.46	35.39	37.87	60.14	46.78
1300	41.34	43.38	40.97	38.62	41.40	65.98	51.47
1400	44.89	47.07	44.51	41.90	44.95	71.89	56.25
1500	48.45	50.77	48.06	45.22	48.51	77.84	61.09

Note on interpolating from tabulated values

$$H(T) = H(T_1) + \frac{(T - T_1)}{(T_2 - T_1)} \times [H(T_2) - H(T_1)]$$

Where:

- $H(T)$ is the enthalpy at the desired temperature T ,
- T_1 and T_2 are the temperatures between which the interpolation is performed,
- $H(T_1)$ and $H(T_2)$ are the enthalpy values at T_1 and T_2 , respectively.

For the example

- $T = 430^\circ\text{C}$,
- $T_1 = 400^\circ\text{C}$,
- $T_2 = 500^\circ\text{C}$,
- $H(T_1) = 11.24 \text{ kJ/mol}$,
- $H(T_2) = 14.37 \text{ kJ/mol}$.

$$H(430^\circ\text{C}) = 11.24 + \frac{(430 - 400)}{(500 - 400)} \times (14.37 - 11.24)$$

$$H(430^\circ\text{C}) = 11.24 + 0.30 \times 3.13$$

$$H(430^\circ\text{C}) = 11.24 + 0.939 = 12.17 \text{ kJ/mol.}$$

Phase changes at constant T and P

Latent Heat:

The specific enthalpy change ($\Delta\hat{H}$) during a phase transition (e.g., melting, vaporization) at constant temperature and pressure is called the **latent heat**. It is distinct from **sensible heat**, which involves temperature changes without a phase change (that we have just seen).

Heat of Vaporization (from liquid to gas):

- For water at 100°C and 1 atm, the latent heat of vaporization is 40.6 kJ/mol.
- The **heat of condensation** is the negative of the heat of vaporization (-40.6 kJ/mol) because condensation is the reverse process of vaporization.

Heat of Fusion (from solid to liquid):

The **heat of fusion** (or melting) is the enthalpy difference between the solid and liquid forms of a substance at a given T and P.

Similarly, the **heat of solidification** is the negative of the heat of fusion.

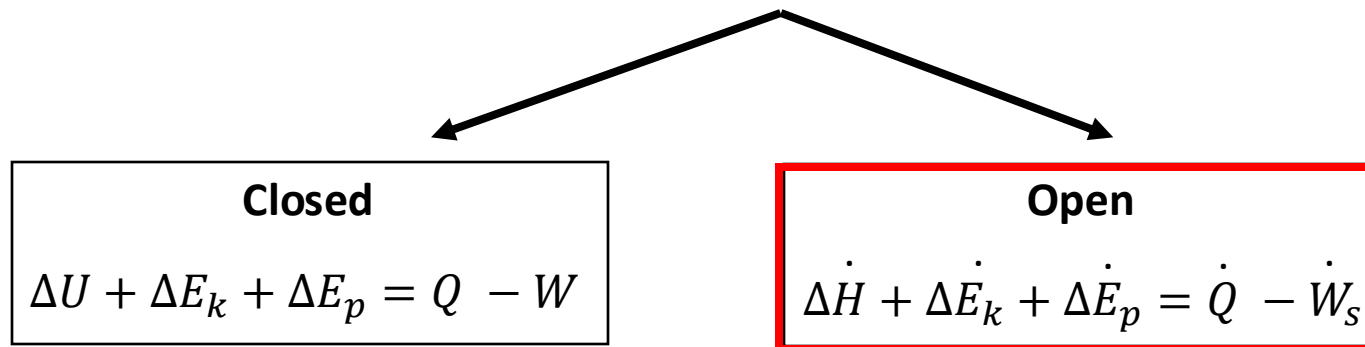
Tabulated Values:

Standard heats of fusion and vaporization are typically provided at the melting or boiling points of a substance at 1 atm. **These values can be found in Table B1 (more on this later)**

Energy Balances: overview

Again, with the mother of all equations:

$$E_{\text{accumulated}} = E_{\text{input}} - E_{\text{output}} + E_{\text{gen}} + E_{\text{transferred}}$$



- Δ : final – initial

- Δ : output – input

Non-reactive

Reactive ($\Delta H = ?$)

Heat of reaction method

Heat of formation method

Energy Balances: Heat of Formation vs Heat of Reaction

Reactive ($\Delta\dot{H} = ?$)

Heat of reaction method

$$\Delta\dot{H} = \dot{\xi}\Delta H_r^0 + \sum_{out} \dot{n}_i \widehat{H}_i - \sum_{in} \dot{n}_i \widehat{H}_i$$

Heat of formation method

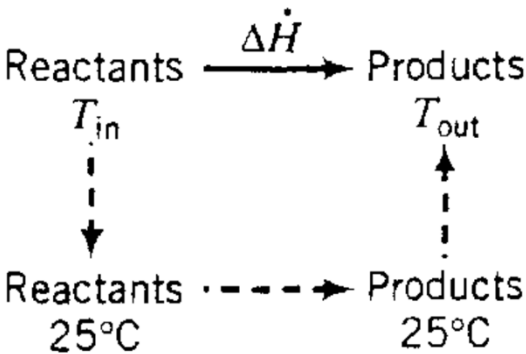
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Energy Balances: Heat of Formation vs Heat of Reaction

Reactive ($\Delta\dot{H} = ?$)

Heat of reaction method

$$\Delta\dot{H} = \dot{\xi}\Delta H_r^0 + \sum_{out} \dot{n}_i \widehat{H}_i - \sum_{in} \dot{n}_i \widehat{H}_i$$

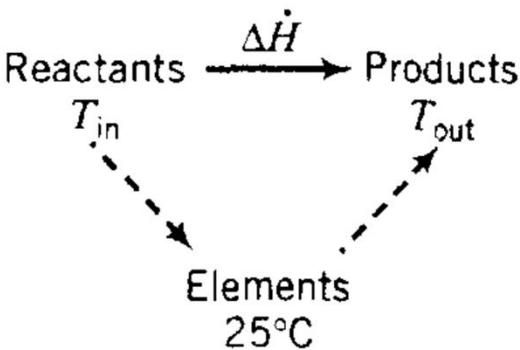


(a) Process path for heat of reaction method

Reference states: reactants and products species at 25 C at 1 atm in the phases (solid, liquid or gas) for which the heat of reaction is known

Heat of formation method

$$\Delta\dot{H} = \sum_{out} \dot{n}_i \widehat{H}_i - \sum_{in} \dot{n}_i \widehat{H}_i$$



(b) Process path for heat of formation method

Reference states: elemental species that constitute the reactants and products at 25 C at 1 atm

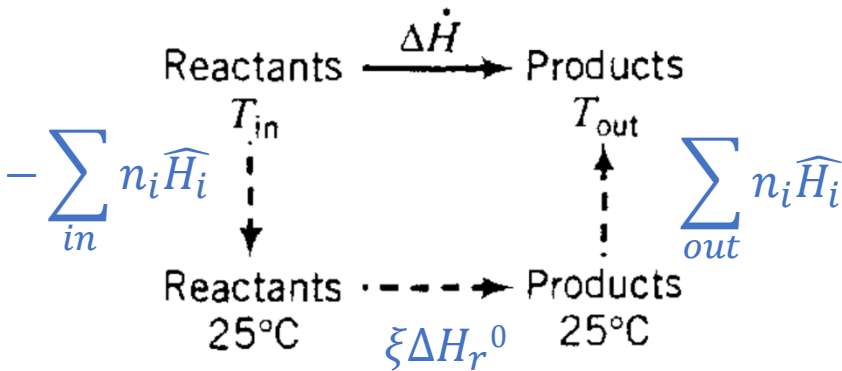
In both methods, reference states for nonreactive species may be chosen for convenience

Energy Balances: Heat of Formation vs Heat of Reaction

Reactive ($\Delta \dot{H} = ?$)

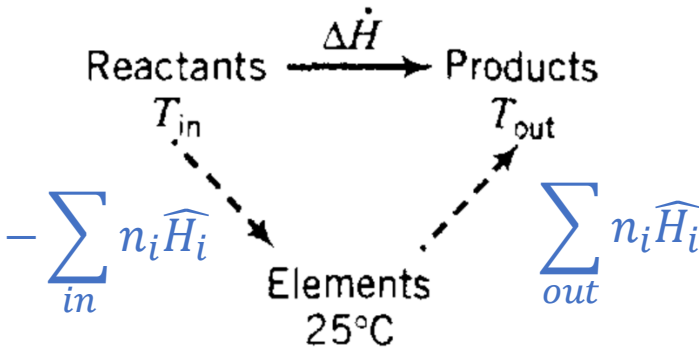
Heat of reaction method

$$\Delta \dot{H} = \dot{\xi} \Delta H_r^0 + \sum_{out} \dot{n}_i \widehat{H}_i - \sum_{in} \dot{n}_i \widehat{H}_i$$



Heat of formation method

$$\Delta \dot{H} = \sum_{out} n_i \widehat{H}_i - \sum_{in} n_i \widehat{H}_i$$



Hess's Law

$$\Delta \hat{H}_r^\circ = \sum_i \nu_i \Delta \hat{H}_{fi}^\circ = \sum_{\text{products}} |\nu_i| \Delta \hat{H}_{fi}^\circ - \sum_{\text{reactants}} |\nu_i| \Delta \hat{H}_{fi}^\circ$$

Appendix B

Physical Property Tables

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B.1 Selected Physical Property Data

Compound	Formula	Mol. Wt.	SG (20°/4°)	$T_m(^{\circ}\text{C})^b$	$\Delta\hat{H}_m(T_m)^{c,j}$ kJ/mol	$T_b(^{\circ}\text{C})^d$	$\Delta\hat{H}_v(T_b)^{e,j}$ kJ/mol	$T_c(\text{K})^f$	$P_c(\text{atm})^g$	$(\Delta\hat{H}_f^{\circ})^{h,j}$ kJ/mol	$(\Delta\hat{H}_c^{\circ})^{i,j}$ kJ/mol
Acetaldehyde	CH ₃ CHO	44.05	0.783 ^{18°}	-123.7	—	20.2	25.1	461.0	—	-166.2(g)	-1192.4(g)
Acetic acid	CH ₃ COOH	60.05	1.049	16.6	12.09	118.2	24.39	594.8	57.1	-486.18(l)	-871.69(l)
										-438.15(g)	-919.73(g)
Acetone	C ₃ H ₆ O	58.08	0.791	-95.0	5.69	56.0	30.2	508.0	47.0	-248.2(l)	-1785.7(l)
										-216.7(g)	-1821.4(g)
Acetylene	C ₂ H ₂	26.04	—	—	—	-81.5	17.6	309.5	61.6	+226.75(g)	-1299.6(g)
Ammonia	NH ₃	17.03	—	-77.8	5.653	-33.43	23.351	405.5	111.3	-67.20(l)	-382.58(g)
										-46.19(g)	-382.58(g)

(latent) heat of fusion/melting H_m : specific enthalpy from solid to liquid stage = - latent heat of solidification

(latent) heat of vaporization H_v : specific enthalpy change from liquid to gaseous stage = - latent heat of condensation

^bMelting point at 1 atm.

^cHeat of fusion at T_m and 1 atm.

^dBoiling point at 1 atm.

^eHeat of vaporization at T_b and 1 atm.

^fCritical temperature.

^gCritical pressure.

^hHeat of formation at 25°C and 1 atm.

ⁱHeat of combustion at 25°C and 1 atm. Standard states of products are CO₂(g), H₂O(l), SO₂(g), HCl(aq), and N₂(g). To calculate $\Delta\hat{H}_c^{\circ}$ with H₂O(g) as a product, 44.01 n_w to the tabulated value, where n_w = moles H₂O formed/mole fuel burned.

B.2 Heat Capacities

Table B.2 Heat Capacities^a

Form 1: $C_p[\text{kJ}/(\text{mol}\cdot^\circ\text{C})]$ or $[\text{kJ}/(\text{mol}\cdot\text{K})] = a + bT + cT^2 + dT^3$
Form 2: $C_p[\text{kJ}/(\text{mol}\cdot^\circ\text{C})]$ or $[\text{kJ}/(\text{mol}\cdot\text{K})] = a + bT + cT^{-2}$

Example: $(C_p)_{\text{acetone(g)}} = 0.07196 + (20.10 \times 10^{-5})T - (12.78 \times 10^{-8})T^2 + (34.76 \times 10^{-12})T^3$, where T is in $^\circ\text{C}$.

Note: The formulas for gases are strictly applicable at pressures low enough for the ideal gas equation of state to apply.

Compound	Formula	Mol. Wt.	State	Form	Temp. Unit	$a \times 10^3$	$b \times 10^5$	$c \times 10^8$	$d \times 10^{12}$	Range (Units of T)
Acetone	CH ₃ COCH ₃	58.08	l	1	$^\circ\text{C}$	123.0	18.6			−30–60
			g	1	$^\circ\text{C}$	71.96	20.10	−12.78	34.76	0–1200
Acetylene	C ₂ H ₂	26.04	g	1	$^\circ\text{C}$	42.43	6.053	−5.033	18.20	0–1200
Air		29.0	g	1	$^\circ\text{C}$	28.94	0.4147	0.3191	−1.965	0–1500
			g	1	K	28.09	0.1965	0.4799	−1.965	273–1800
Ammonia	NH ₃	17.03	g	1	$^\circ\text{C}$	35.15	2.954	0.4421	−6.686	0–1200
Ammonium sulfate	(NH ₄) ₂ SO ₄	132.15	c	1	K	215.9				275–328
Benzene	C ₆ H ₆	78.11	l	1	$^\circ\text{C}$	126.5	23.4			6–67
			g	1	$^\circ\text{C}$	74.06	32.95	−25.20	77.57	0–1200
Isobutane	C ₄ H ₁₀	58.12	g	1	$^\circ\text{C}$	89.46	30.13	−18.91	49.87	0–1200
n-Butane	C ₄ H ₁₀	58.12	g	1	$^\circ\text{C}$	92.30	27.88	−15.47	34.98	0–1200
Isobutene	C ₄ H ₈	56.10	g	1	$^\circ\text{C}$	82.88	25.64	−17.27	50.50	0–1200
Calcium carbide	CaC ₂	64.10	c	2	K	68.62	1.19	−8.66 × 10 ¹⁰	—	298–720
Calcium carbonate	CaCO ₃	100.09	c	2	K	82.34	4.975	−12.87 × 10 ¹⁰	—	273–1033
Calcium hydroxide	Ca(OH) ₂	74.10	c	1	K	89.5				276–373
Calcium oxide	CaO	56.08	c	2	K	41.84	2.03	−4.52 × 10 ¹⁰		273–1173
Carbon	C	12.01	c	2	K	11.18	1.095	−4.891 × 10 ¹⁰		273–1373

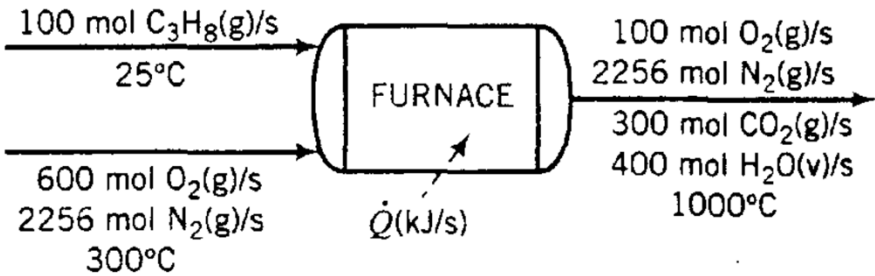
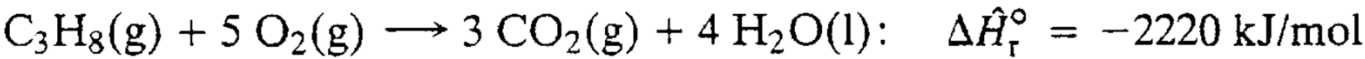
Know Thy Tables

Some specific enthalpies are already computed for you → Gain of time during the exam!

Table B.8 Specific Enthalpies of Selected Gases: SI Units

$\hat{H}(\text{kJ/mol})$							
Reference state: Gas, $P_{\text{ref}} = 1 \text{ atm}$, $T_{\text{ref}} = 25^\circ\text{C}$							
T	Air	O ₂	N ₂	H ₂	CO	CO ₂	H ₂ O
0	-0.72	-0.73	-0.73	-0.72	-0.73	-0.92	-0.84
25	0.00	0.00	0.00	0.00	0.00	0.00	0.00
100	2.19	2.24	2.19	2.16	2.19	2.90	2.54
200	5.15	5.31	5.13	5.06	5.16	7.08	6.01
300	8.17	8.47	8.12	7.96	8.17	11.58	9.57
400	11.24	11.72	11.15	10.89	11.25	16.35	13.23
500	14.37	15.03	14.24	13.83	14.38	21.34	17.01
600	17.55	18.41	17.39	16.81	17.57	26.53	20.91
700	20.80	21.86	20.59	19.81	20.82	31.88	24.92
800	24.10	25.35	23.86	22.85	24.13	37.36	29.05
900	27.46	28.89	27.19	25.93	27.49	42.94	33.32
1000	30.86	32.47	30.56	29.04	30.91	48.60	37.69
1100	34.31	36.07	33.99	32.19	34.37	54.33	42.18
1200	37.81	39.70	37.46	35.39	37.87	60.14	46.78
1300	41.34	43.38	40.97	38.62	41.40	65.98	51.47
1400	44.89	47.07	44.51	41.90	44.95	71.89	56.25
1500	48.45	50.77	48.06	45.22	48.51	77.84	61.09

Energy Balances: Heat of Formation vs Heat of Reaction



$$\begin{aligned} \dot{\xi} &= \frac{|(\dot{n}_{\text{C}_3\text{H}_8})_{\text{out}} - (\dot{n}_{\text{C}_3\text{H}_8})_{\text{in}}|}{|\nu_{\text{C}_3\text{H}_8}|} \\ &= \frac{|0 - 100| \text{ mol/s}}{1} = 100 \text{ mol/s} \end{aligned}$$

Heat of reaction method

References: C₃H₈(g), O₂(g), N₂(g), CO₂(g), H₂O(l) at 25°C and 1 atm

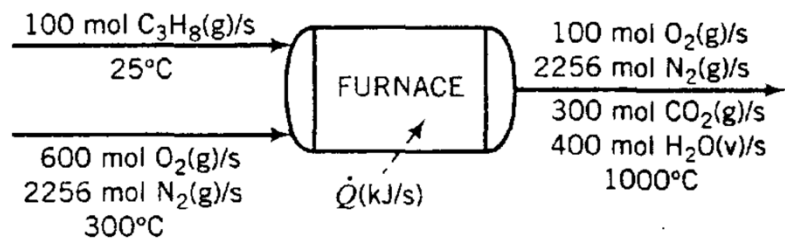
Substance	$\dot{n}_{\text{in}}$ (mol/s)	$\hat{H}_{\text{in}}$ (kJ/mol)	$\dot{n}_{\text{out}}$ (mol/s)	$\hat{H}_{\text{out}}$ (kJ/mol)
C ₃ H ₈	100	0	—	—
O ₂	600	$\hat{H}_2$	100	$\hat{H}_4$
N ₂	2256	$\hat{H}_3$	2256	$\hat{H}_5$
CO ₂	—	—	300	$\hat{H}_6$
H ₂ O	—	—	400	$\hat{H}_7$

Heat of formation method

References: C(s), H₂(g), O₂(g), N₂(g) at 25°C and 1 atm

Substance	$\dot{n}_{\text{in}}$ (mol/s)	$\hat{H}_{\text{in}}$ (kJ/mol)	$\dot{n}_{\text{out}}$ (mol/s)	$\hat{H}_{\text{out}}$ (kJ/mol)
C ₃ H ₈	100	$\hat{H}_1$	—	—
O ₂	600	$\hat{H}_2$	100	$\hat{H}_4$
N ₂	2256	$\hat{H}_3$	2256	$\hat{H}_5$
CO ₂	—	—	300	$\hat{H}_6$
H ₂ O	—	—	400	$\hat{H}_7$

Energy Balances: Heat of Formation vs Heat of Reaction



$\Delta \hat{H}_r^\circ = -2220 \text{ kJ/mol}$ $\xi = 100 \text{ mol/s}$

Heat of reaction method

Know your tables!

References: C₃H₈(g), O₂(g), N₂(g), CO₂(g), H₂O(l) at 25°C and 1 atm

Substance	$\dot{n}_{in}$ (mol/s)	$\hat{H}_{in}$ (kJ/mol)	$\dot{n}_{out}$ (mol/s)	$\hat{H}_{out}$ (kJ/mol)
C ₃ H ₈	100	0	—	—
O ₂	600	$\hat{H}_2$	100	$\hat{H}_4$
N ₂	2256	$\hat{H}_3$	2256	$\hat{H}_5$
CO ₂	—	—	300	$\hat{H}_6$
H ₂ O	—	—	400	$\hat{H}_7$

Table B.1 (Continued)

Compound	Formula	Mol. Wt.	SG (20°/4°)	$T_m(^{\circ}\text{C})^a$	$\Delta \hat{H}_m(T_m)^{b,c}$ kJ/mol	$T_b(^{\circ}\text{C})^d$	$\Delta \hat{H}_v(T_b)^{e,f}$ kJ/mol	$T_c(\text{K})^f$	$P_c(\text{atm})^g$	$(\Delta \hat{H}_f^\circ)^{h,i}$ kJ/mol	$(\Delta \hat{H}_c^\circ)^{j,k}$ kJ/mol
Sodium thiosulfate	Na ₂ S ₂ O ₃	158.11	1.667	—	—	—	—	—	—	-1117.1(c)	—
Sulfur (rhombic)	S ₈	256.53	2.07	113	10.04	444.6	83.7	—	—	0(c)	—
Sulfur (monoclinic)	S ₈	256.53	1.96	119	14.17	444.6	83.7	—	—	+0.30(c)	—
Sulfur dioxide	SO ₂	64.07	—	-75.48	7.402	-10.02	24.91	430.7	77.8	-296.90(g)	—
Sulfur trioxide	SO ₃	80.07	—	16.84	25.48	43.3	41.80	491.4	83.8	-395.18(g)	—
Sulfuric acid	H ₂ SO ₄	98.08	1.834 ^l	10.35	9.87	Decomposes at 340°C	—	—	—	-811.32(l)	—
Toluene	C ₇ H ₈	92.13	0.866	-94.99	6.619	110.62	33.47	593.9	40.3	-907.51(aq)	—
Water	H ₂ O	18.016	1.00 ^u	0.00	6.0095	100.00	40.656	647.4	218.3	+12.00(l)	-3909.9(l)
m-Xylene	C ₈ H ₁₀	106.16	0.864	-47.87	11.569	139.10	36.40	619	34.6	+50.00(g)	-3947.9(g)
o-Xylene	C ₈ H ₁₀	106.16	0.880	-25.18	13.598	144.42	36.82	631.5	35.7	-285.84(l)	—
p-Xylene	C ₈ H ₁₀	106.16	0.861	13.26	17.11	138.35	36.07	618	33.9	-241.83(g)	-455.9(l)
Zinc	Zn	65.38	7.140	419.5	6.674	907	114.77	—	—	-25.42(l)	-455.9(l)
										+17.24(g)	-4594.5(g)
										-24.44(l)	-4552.9(l)
										+18.99(g)	-4596.3(g)
										-24.43(l)	-4552.91(l)
										17.95(g)	-4595.2(g)
										0(c)	—

$\hat{H}_2 = \Delta \hat{H}$ for O₂(25°C) → O₂(300°C) = 8.47 kJ/mol (from Table B.8)

$\hat{H}_3 = 8.12 \text{ kJ/mol}$

$\hat{H}_4 = 32.47 \text{ kJ/mol}$

$\hat{H}_6 = 48.60 \text{ kJ/mol}$

$\hat{H}_7 = \Delta \hat{H}$ for H₂O(l, 25°C) → H₂O(g, 1000°C)

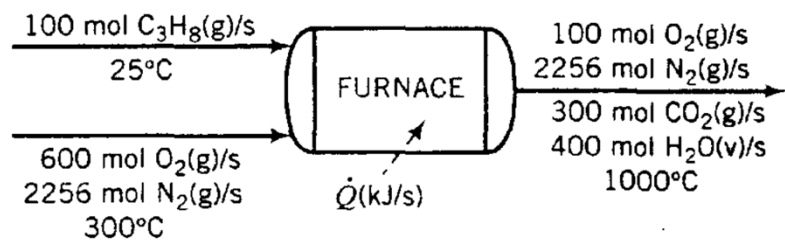
$\int_{25^{\circ}\text{C}}^{100^{\circ}\text{C}} C_{p,l} dT + \Delta \hat{H}_v(100^{\circ}\text{C}) + \int_{100^{\circ}\text{C}}^{1000^{\circ}\text{C}} C_{p,v} dT.$

2 different Cps for 2 different phases

Table B.2 Heat Capacities^a

Form 1: $C_p[\text{kJ}/(\text{mol}\cdot^{\circ}\text{C})]$ or $[\text{kJ}/(\text{mol}\cdot\text{K})] = a + bT + cT^2 + dT^3$										
Form 2: $C_p[\text{kJ}/(\text{mol}\cdot^{\circ}\text{C})]$ or $[\text{kJ}/(\text{mol}\cdot\text{K})] = a + bT + cT^{-2}$										
Example: $(C_p)_{\text{acetone(g)}} = 0.07196 + (20.10 \times 10^{-5})T - (12.78 \times 10^{-8})T^2 + (34.76 \times 10^{-12})T^3$, where T is in $^{\circ}\text{C}$.										
Note: The formulas for gases are strictly applicable at pressures low enough for the ideal gas equation of state to apply.										
Compound	Formula	Mol. Wt.	State	Form	Temp. Unit	$a \times 10^3$	$b \times 10^5$	$c \times 10^8$	$d \times 10^{12}$	Range (Units of T)
Water	H ₂ O	18.016	l	1	$^{\circ}\text{C}$	75.4				0-100
			g	1	$^{\circ}\text{C}$	33.46	0.6880	0.7604	-3.593	0-1500

Energy Balances: Heat of Formation vs Heat of Reaction



$\Delta \hat{H}_r^\circ = -2220 \text{ kJ/mol}$ $\xi = 100 \text{ mol/s}$

Heat of reaction method

Know your tables!

References: C₃H₈(g), O₂(g), N₂(g), CO₂(g), H₂O(l) at 25°C and 1 atm

Substance	$\dot{n}_{in}$ (mol/s)	$\hat{H}_{in}$ (kJ/mol)	$\dot{n}_{out}$ (mol/s)	$\hat{H}_{out}$ (kJ/mol)
C ₃ H ₈	100	0	—	—
O ₂	600	$\hat{H}_2$	100	$\hat{H}_4$
N ₂	2256	$\hat{H}_3$	2256	$\hat{H}_5$
CO ₂	—	—	300	$\hat{H}_6$
H ₂ O	—	—	400	$\hat{H}_7$

Table B.1 (Continued)

Compound	Formula	Mol. Wt.	SG (20°/4°)	$T_m(^{\circ}\text{C})^a$	$\Delta \hat{H}_m(T_m)^{b,c}$ kJ/mol	$T_b(^{\circ}\text{C})^d$	$\Delta \hat{H}_v(T_b)^{e,f}$ kJ/mol	$T_c(\text{K})^f$	$P_c(\text{atm})^g$	$(\Delta \hat{H}_f^\circ)^{h,i}$ kJ/mol	$(\Delta \hat{H}_c^\circ)^{j,k}$ kJ/mol
Sodium thiosulfate	Na ₂ S ₂ O ₃	158.11	1.667	—	—	—	—	—	—	-1117.1(c)	—
Sulfur (rhombic)	S ₈	256.53	2.07	113	10.04	444.6	83.7	—	—	0(c)	—
Sulfur (monoclinic)	S ₈	256.53	1.96	119	14.17	444.6	83.7	—	—	+0.30(c)	—
Sulfur dioxide	SO ₂	64.07	—	-75.48	7.402	-10.02	24.91	430.7	77.8	-296.90(g)	—
Sulfur trioxide	SO ₃	80.07	—	16.84	25.48	43.3	41.80	491.4	83.8	-395.18(g)	—
Sulfuric acid	H ₂ SO ₄	98.08	1.834 ^l	10.35	9.87	Decomposes at 340°C	—	—	—	-811.32(l)	—
Toluene	C ₇ H ₈	92.13	0.866	-94.99	6.619	110.62	33.47	593.9	40.3	-907.51(aq)	—
Water	H ₂ O	18.016	1.00 ^u	0.00	6.0095	100.00	40.656	647.4	218.3	+12.00(l)	-3909.9(l)
m-Xylene	C ₈ H ₁₀	106.16	0.864	-47.87	11.569	139.10	36.40	619	34.6	+50.00(g)	-3947.9(g)
o-Xylene	C ₈ H ₁₀	106.16	0.880	-25.18	13.598	144.42	36.82	631.5	35.7	-285.84(l)	—
p-Xylene	C ₈ H ₁₀	106.16	0.861	13.26	17.11	138.35	36.07	618	33.9	-241.83(g)	—
Zinc	Zn	65.38	7.140	419.5	6.674	907	114.77	—	—	-25.42(l)	-455.9(l)
										+17.24(g)	-4594.5(g)
										-24.44(l)	-4552.9(l)
										+18.99(g)	-4596.3(g)
										-24.43(l)	-4552.91(l)
										17.95(g)	-4595.2(g)
										0(c)	—

$\hat{H}_2 = \Delta \hat{H}$ for O₂(25°C) → O₂(300°C) = 8.47 kJ/mol (from Table B.8)

$\hat{H}_3 = 8.12 \text{ kJ/mol}$

$\hat{H}_4 = 32.47 \text{ kJ/mol}$

$\hat{H}_6 = 48.60 \text{ kJ/mol}$

$\hat{H}_7 = \Delta \hat{H}$ for H₂O(l, 25°C) → H₂O(g, 1000°C)

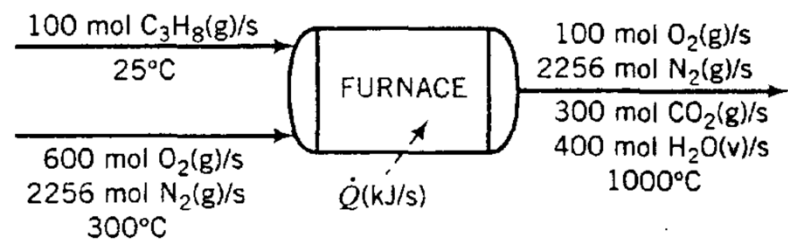
$\Delta \hat{H} = \xi \Delta \hat{H}_r^\circ + \sum \dot{n}_{out} \hat{H}_{out} - \sum \dot{n}_{in} \hat{H}_{in} = -1.26 \times 10^5 \text{ kJ/s}$

2 different Cps for 2 different phases

Table B.2 Heat Capacities^a

Form 1: $C_p[\text{kJ}/(\text{mol} \cdot ^\circ\text{C})]$ or $[\text{kJ}/(\text{mol} \cdot \text{K})] = a + bT + cT^2 + dT^3$ Form 2: $C_p[\text{kJ}/(\text{mol} \cdot ^\circ\text{C})]$ or $[\text{kJ}/(\text{mol} \cdot \text{K})] = a + bT + cT^{-2}$										
Example: $(C_p)_{\text{acetone(g)}} = 0.07196 + (20.10 \times 10^{-5})T - (12.78 \times 10^{-8})T^2 + (34.76 \times 10^{-12})T^3$, where T is in °C.										
Note: The formulas for gases are strictly applicable at pressures low enough for the ideal gas equation of state to apply.										
Compound	Formula	Mol. Wt.	State	Form	Temp. Unit	$a \times 10^3$	$b \times 10^5$	$c \times 10^8$	$d \times 10^{12}$	Range (Units of T)
Water	H ₂ O	18.016	l	1	°C	75.4	—	—	—	0–100
				1	°C	33.46	0.6880	0.7604	-3.593	0–1500

Energy Balances: Heat of Formation vs Heat of Reaction



$$\Delta \hat{H}_r^\circ = -2220 \text{ kJ/mol} \quad \dot{\xi} = 100 \text{ mol/s}$$

Heat of reaction method

References: C₃H₈(g), O₂(g), N₂(g), CO₂(g), H₂O(l) at 25°C and 1 atm

Substance	$\dot{n}_{in}$ (mol/s)	$\hat{H}_{in}$ (kJ/mol)	$\dot{n}_{out}$ (mol/s)	$\hat{H}_{out}$ (kJ/mol)
C ₃ H ₈	100	0	—	—
O ₂	600	$\hat{H}_2$	100	$\hat{H}_4$
N ₂	2256	$\hat{H}_3$	2256	$\hat{H}_5$
CO ₂	—	—	300	$\hat{H}_6$
H ₂ O	—	—	400	$\hat{H}_7$

$$\begin{aligned} \hat{H}_2 &= \Delta \hat{H} \text{ for } \text{O}_2(25^\circ\text{C}) \rightarrow \text{O}_2(300^\circ\text{C}) = 8.47 \text{ kJ/mol (from Table B.8)} \\ \hat{H}_3 &= 8.12 \text{ kJ/mol} \\ \hat{H}_4 &= 32.47 \text{ kJ/mol} \\ \hat{H}_6 &= 48.60 \text{ kJ/mol} \\ \hat{H}_7 &= \Delta \hat{H} \text{ for } \text{H}_2\text{O(l, } 25^\circ\text{C)} \rightarrow \text{H}_2\text{O(g, } 1000^\circ\text{C)} \\ \Delta \dot{H} &= \dot{\xi} \Delta \hat{H}_r^\circ + \sum \dot{n}_{out} \hat{H}_{out} - \sum \dot{n}_{in} \hat{H}_{in} = -1.26 \times 10^5 \text{ kJ/s.} \end{aligned}$$

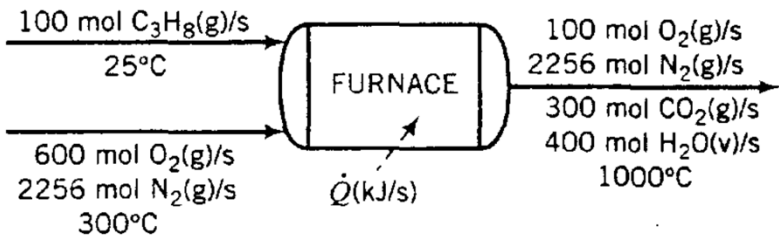
Heat of formation method

References: C(s), H₂(g), O₂(g), N₂(g) at 25°C and 1 atm

Substance	$\dot{n}_{in}$ (mol/s)	$\hat{H}_{in}$ (kJ/mol)	$\dot{n}_{out}$ (mol/s)	$\hat{H}_{out}$ (kJ/mol)
C ₃ H ₈	100	$\hat{H}_1$	—	—
O ₂	600	$\hat{H}_2$	100	$\hat{H}_4$
N ₂	2256	$\hat{H}_3$	2256	$\hat{H}_5$
CO ₂	—	—	300	$\hat{H}_6$
H ₂ O	—	—	400	$\hat{H}_7$

For a reactant or product, start with the elemental species at 25°C and 1 atm (the references) and form 1 mol of the process species at 25°C and 1 atm at **gaseous stage** (from Table B.1). Then bring the species from 25°C and 1 atm to its process state, calculating using the appropriate heat capacities from Tables

Energy Balances: Heat of Formation vs Heat of Reaction



Next, we calculate the specific enthalpy of O_2 at 300°C (the process state) relative to O_2 at 25°C (the reference state) as:

$$\hat{H}_2 = 8.47 \text{ kJ/mol (from Table B.8).}$$

There is no heat of formation term since O_2 is an elemental species. We proceed in the same manner to calculate:

$$\hat{H}_3 = 8.12 \text{ kJ/mol, } \hat{H}_4 = 32.47 \text{ kJ/mol, } \hat{H}_5 = 30.56 \text{ kJ/mol,}$$

$$\hat{H}_6 = -344.9 \text{ kJ/mol, and } \hat{H}_7 = -204.1 \text{ kJ/mol.}$$

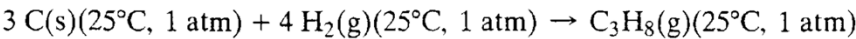
To calculate $\hat{H}_6$ and $\hat{H}_7$, we form the corresponding species ($CO_2(g)$ and $H_2O(v)$) at 25°C from their elements ($\Delta \hat{H} = \Delta \hat{H}_f^\circ$), then heat them from 25°C to 1000°C ($\Delta \hat{H} = \hat{H}_{1000^\circ C}$ from Table B.8), and add the formation and heating terms.

$$\Delta \hat{H}_r^\circ = -2220 \text{ kJ/mol} \quad \dot{\xi} = 100 \text{ mol/s}$$

Heat of formation method

References: C(s), $H_2(g)$, $O_2(g)$, $N_2(g)$ at 25°C and 1 atm

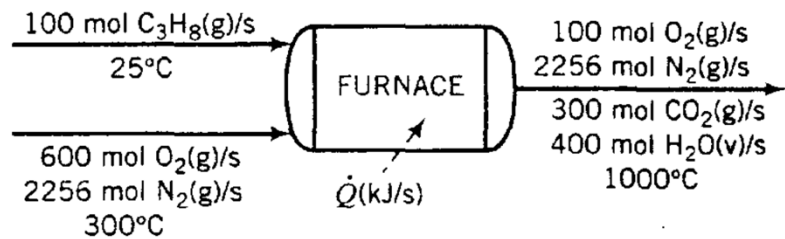
Substance	$\dot{n}_{in}$ (mol/s)	$\hat{H}_{in}$ (kJ/mol)	$\dot{n}_{out}$ (mol/s)	$\hat{H}_{out}$ (kJ/mol)
C_3H_8	100	$\hat{H}_1$	—	—
O_2	600	$\hat{H}_2$	100	$\hat{H}_4$
N_2	2256	$\hat{H}_3$	2256	$\hat{H}_5$
CO_2	—	—	300	$\hat{H}_6$
H_2O	—	—	400	$\hat{H}_7$



$$\hat{H}_1 = (\Delta \hat{H}_f^\circ)_{C_3H_8(g)} = -103.8 \text{ kJ/mol (from Table B.1)}$$

This is the enthalpy of propane at 25°C (the process state) relative to C(s) and $H_2(g)$ at 25°C (the reference states). If the propane had entered at a temperature T_0 other than 25°C, a term of the form $\int_{25^\circ C}^{T_0} C_p dT$ would be added to the heat of formation of propane.

Energy Balances: Heat of Formation vs Heat of Reaction



Next, we calculate the specific enthalpy of O_2 at 300°C (the process state) relative to O_2 at 25°C (the reference state) as:

$$\hat{H}_2 = 8.47 \text{ kJ/mol (from Table B.8).}$$

There is no heat of formation term since O_2 is an elemental species. We proceed in the same manner to calculate:

$$\hat{H}_3 = 8.12 \text{ kJ/mol}, \hat{H}_4 = 32.47 \text{ kJ/mol}, \hat{H}_5 = 30.56 \text{ kJ/mol},$$

$$\hat{H}_6 = -344.9 \text{ kJ/mol}, \text{ and } \hat{H}_7 = -204.1 \text{ kJ/mol.}$$

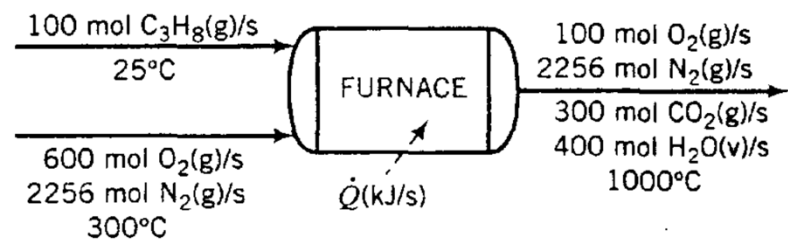
To calculate $\hat{H}_6$ and $\hat{H}_7$, we form the corresponding species ($\text{CO}_2(\text{g})$ and $\text{H}_2\text{O}(\text{v})$) at 25°C from their elements ($\Delta \hat{H} = \Delta \hat{H}_f^\circ$), then heat them from 25°C to 1000°C ($\Delta \hat{H} = \hat{H}_{1000^\circ\text{C}} - \hat{H}_{25^\circ\text{C}}$ from Table B.8), and add the formation and heating terms.

Table B.8 Specific Enthalpies of Selected Gases: SI Units

$\hat{H}(\text{kJ/mol})$							
Reference state: Gas, $P_{\text{ref}} = 1 \text{ atm}$, $T_{\text{ref}} = 25^\circ\text{C}$							
T	Air	O_2	N_2	H_2	CO	CO_2	H_2O
0	-0.72	-0.73	-0.73	-0.72	-0.73	-0.92	-0.84
25	0.00	0.00	0.00	0.00	0.00	0.00	0.00
100	2.19	2.24	2.19	2.16	2.19	2.90	2.54
200	5.15	5.31	5.13	5.06	5.16	7.08	6.01
300	8.17	8.47	8.12	7.96	8.17	11.58	9.57
400	11.24	11.72	11.15	10.89	11.25	16.35	13.23
500	14.37	15.03	14.24	13.83	14.38	21.34	17.01
600	17.55	18.41	17.39	16.81	17.57	26.53	20.91
700	20.80	21.86	20.59	19.81	20.82	31.88	24.92
800	24.10	25.35	23.86	22.85	24.13	37.36	29.05
900	27.46	28.89	27.19	25.93	27.49	42.94	33.32
1000	30.86	32.47	30.56	29.04	30.91	48.60	37.69
1100	34.31	36.07	33.99	32.19	34.37	54.33	42.18
1200	37.81	39.70	37.46	35.39	37.87	60.14	46.78
1300	41.34	43.38	40.97	38.62	41.40	65.98	51.47
1400	44.89	47.07	44.51	41.90	44.95	71.89	56.25
1500	48.45	50.77	48.06	45.22	48.51	77.84	61.09

Water	H_2O	18.016	1.00 ⁴	0.00	6.0095	100.00	40.656	647.4	218.3	-285.84(l)	—
										-241.83(g)	—

Energy Balances: Heat of Formation vs Heat of Reaction



$$\Delta \hat{H}_r^\circ = -2220 \text{ kJ/mol} \quad \xi = 100 \text{ mol/s}$$

Heat of reaction method

References: C₃H₈(g), O₂(g), N₂(g), CO₂(g), H₂O(l) at 25°C and 1 atm

Substance	$\dot{n}_{in}$ (mol/s)	$\hat{H}_{in}$ (kJ/mol)	$\dot{n}_{out}$ (mol/s)	$\hat{H}_{out}$ (kJ/mol)
C ₃ H ₈	100	0	—	—
O ₂	600	$\hat{H}_2$	100	$\hat{H}_4$
N ₂	2256	$\hat{H}_3$	2256	$\hat{H}_5$
CO ₂	—	—	300	$\hat{H}_6$
H ₂ O	—	—	400	$\hat{H}_7$

$$\begin{aligned} \hat{H}_2 &= 8.47 \text{ kJ/mol} & \hat{H}_5 &= 30.56 \text{ kJ/mol} \\ \hat{H}_3 &= 8.12 \text{ kJ/mol} & \hat{H}_6 &= 48.60 \text{ kJ/mol} \\ \hat{H}_4 &= 32.47 \text{ kJ/mol} & \hat{H}_7 &= 81.71 \text{ kJ/mol} \end{aligned}$$

$$\Delta H = \xi \Delta H_r^\circ + \sum_{out} n_i \hat{H}_i - \sum_{in} n_i \hat{H}_i = -1.26 \times 10^5 \frac{\text{kJ}}{\text{s}}$$

Heat of formation method

References: C(s), H₂(g), O₂(g), N₂(g) at 25°C and 1 atm

Substance	$\dot{n}_{in}$ (mol/s)	$\hat{H}_{in}$ (kJ/mol)	$\dot{n}_{out}$ (mol/s)	$\hat{H}_{out}$ (kJ/mol)
C ₃ H ₈	100	$\hat{H}_1$	—	—
O ₂	600	$\hat{H}_2$	100	$\hat{H}_4$
N ₂	2256	$\hat{H}_3$	2256	$\hat{H}_5$
CO ₂	—	—	300	$\hat{H}_6$
H ₂ O	—	—	400	$\hat{H}_7$

$$\begin{aligned} \hat{H}_1 &= -103.8 \text{ kJ/mol} & \hat{H}_5 &= 30.56 \text{ kJ/mol} \\ \hat{H}_2 &= 8.47 \text{ kJ/mol} & \hat{H}_6 &= -344.9 \text{ kJ/mol} \\ \hat{H}_3 &= 8.12 \text{ kJ/mol} & \hat{H}_7 &= -204.1 \text{ kJ/mol} \\ \hat{H}_4 &= 32.47 \text{ kJ/mol} \end{aligned}$$

$$\Delta H = \sum_{out} n_i \hat{H}_i - \sum_{in} n_i \hat{H}_i = -1.26 \times 10^5 \frac{\text{kJ}}{\text{s}}$$

Energy Balances: Procedure for Calculations

1. Perform all required material balances calculations (as much as possible)
2. Write the appropriate form of the energy balance (closed or open systems) and delete any of the terms that are either zero or negligible for the given process system
3. Choose a reference state (phase, temperature and pressure) for each species involved in the process
 1. If H or U for a species will be looked up in a table (such as the steam tables for water) choose the reference state used to generate the table
 2. Otherwise, choose one of the inlet or outlet states as the reference states for the species (so that at least one H or U may be set equal to zero)
4. Construct a table with columns for number of species and specific enthalpies/internal energies) relative to the chosen reference states
5. Calculate all the required values
6. Use the final energy balance formula to find the desired quantities

Reminders

The Midterm grade (M) **only benefits** your Overall grade (O)

- Two cases, depending on your final exam grade (F):

1. $M > F$: $O = M*0.3 + F*0.7$

2. $M < F$: $O = F$

No electronic devices, except for calculators

- Print physical property tables

Plan for Q&A session before exam → **Class Reps?**

If more questions/clarifications needed, still Q&A session!