

Optical methods in chemistry
or
Photon tools for chemical sciences

Session 4:

Course layout – contents overview and general structure

- Introduction and ray optics
- Wave optics
- Beams
- From cavities to lasers
- More lasers and optical tweezers
- From diffraction and Fourier optics
- Microscopy
- Spectroscopy
- Electromagnetic optics
- Absorption, dispersion, and non-linear optics
- Ultrafast lasers
- Introduction to x-rays
- X-ray diffraction and spectroscopy
- Summary

Today's learning goal:

Understanding cavities and the principles of lasers

Optical resonantors ("cavities")



Charles Fabry
(1867–1945)



Fabry - Perot



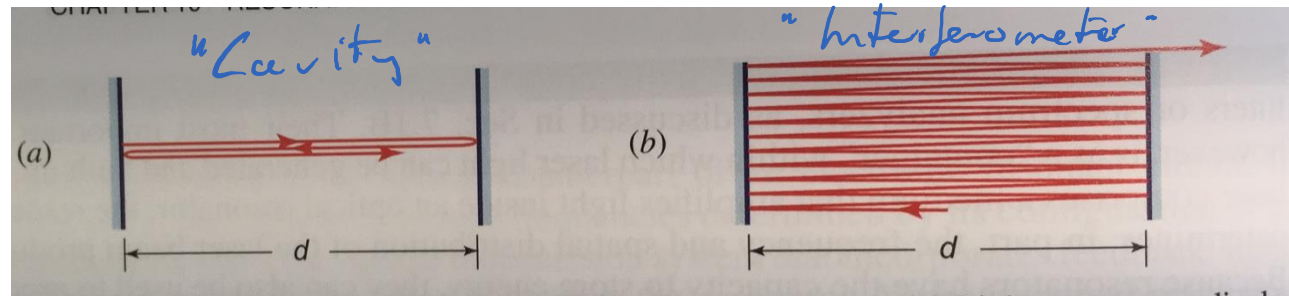
Alfred Perot
(1863–1925)



Interferometer / Resonator

Fabry-Perot Resonator

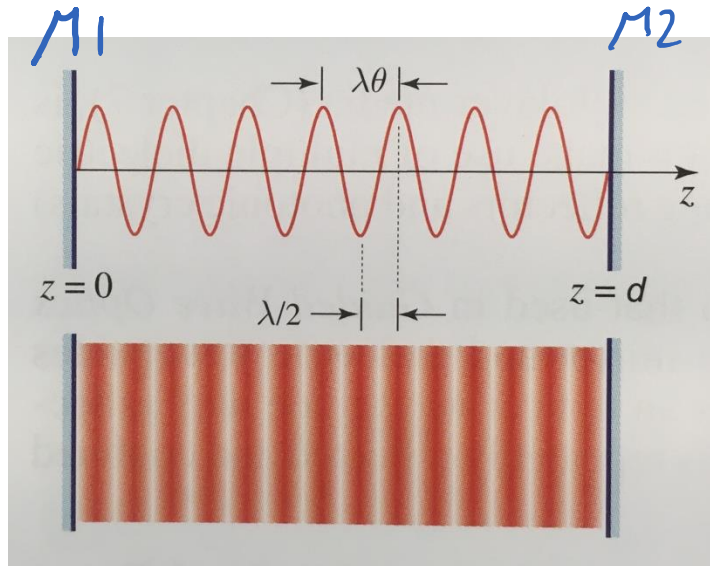
Idea: Trap light between highly reflective mirrors



Idea

- send light back / forth
- "trap" light in that manner
- interference condition → standing wave

Standing waves represent resonator modes



Standing wave

if "fits" → constructive interference condition

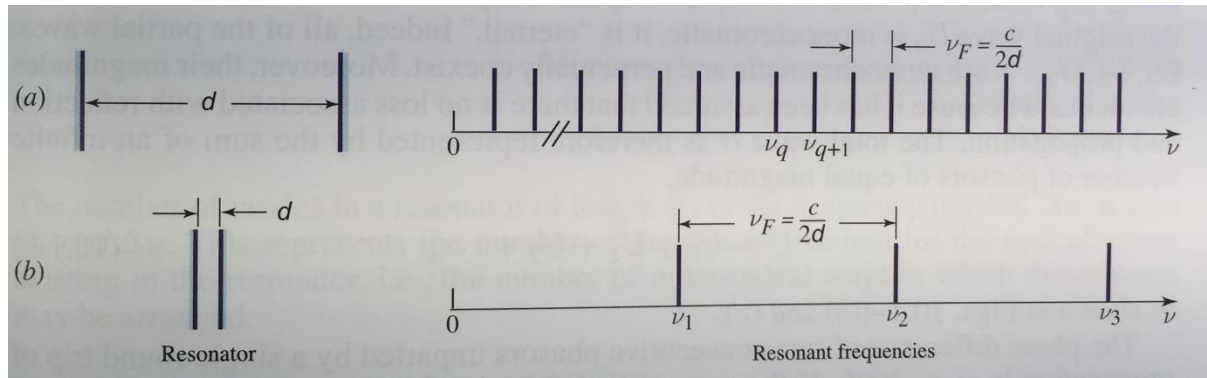
$$\hookrightarrow n\lambda = 2d \quad \text{or} \quad n \cdot \frac{\lambda}{2} = d$$

in frequency

$$\nu_n = n \cdot \frac{c}{2d} \quad \text{with} \quad \nu = \frac{c}{\lambda}$$

Properties of the Fabry Perot Resonator

→ in frequency space



} narrower resonator →
broader spacing!

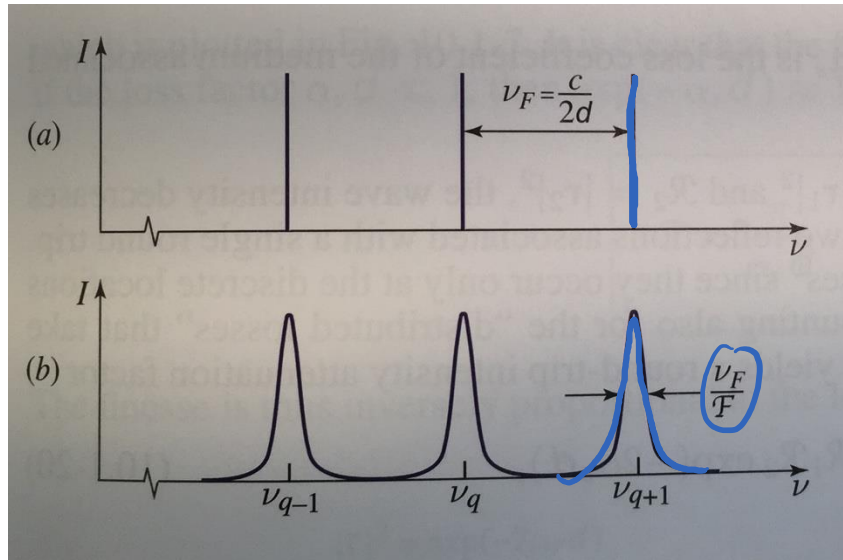
Frequency spacing

$$\nu_F = \frac{c}{2d} \rightarrow \text{free spectral range}$$

↳ in wavelength: roundtrip distance at resonance must be an integer of the wavelength $2d = n\lambda_n$

$$n = 1, 2, 3, \dots$$

Ideal vs real resonator – real is with losses



ideal

real

For a cavity with losses
 (→ a real cavity) the ideal
 δ -like behavior is altered

↳ add spectral width

$$\delta_\nu = \frac{\nu_F}{F}$$

F – “finesse” of the cavity

$F \sim \frac{\pi}{\tau}$ and τ – Transmission

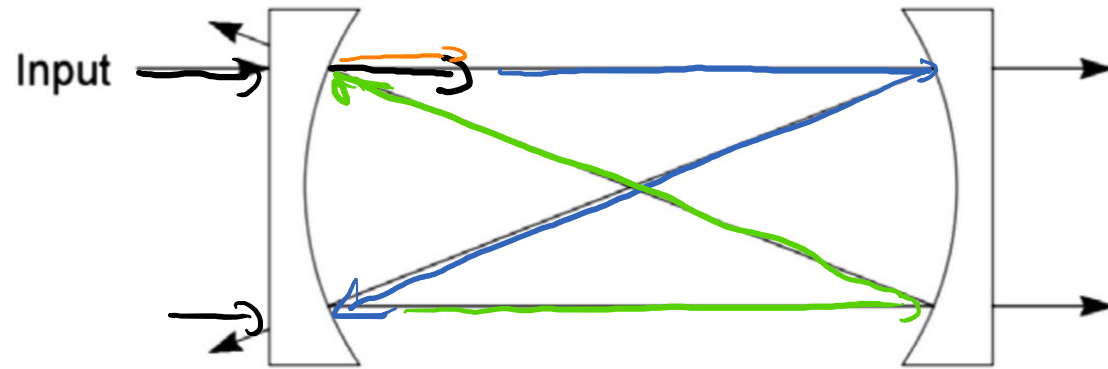
Losses increasing → Finesse decreasing
 → δ_ν increasing

Quality factor $Q \approx \frac{\text{stored energy}}{\text{energy loss/cycle}}$

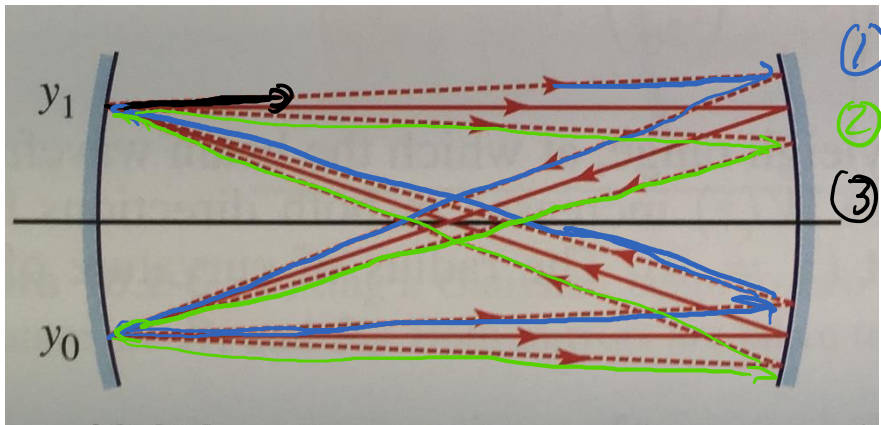
$$Q \approx \frac{\nu_0}{\nu_F} F \quad \nu_0 - \text{optimal frequency}$$

Spherical Resonator $\rightarrow$ ray optics

Note: spherical resonator more stable than planar resonator



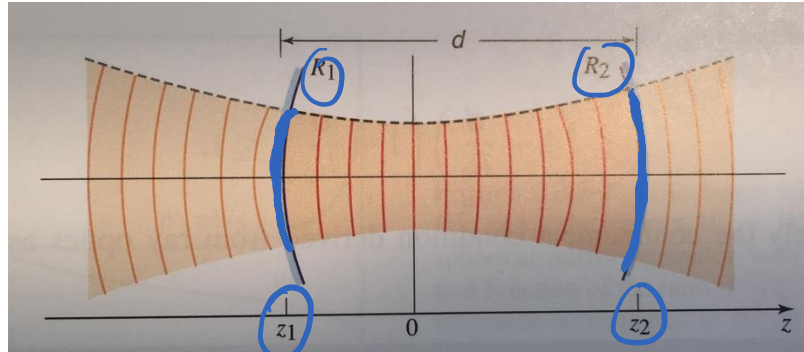
} intuitive with ray optics



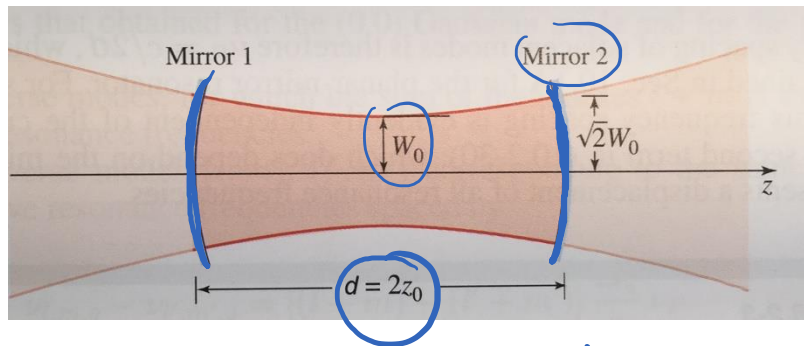
$\rightarrow$ after two round trip same paths
 $\rightarrow$ paraxial beams

Gaussian Beam Resonator

→ Spherical resonator matches Gaussian beam

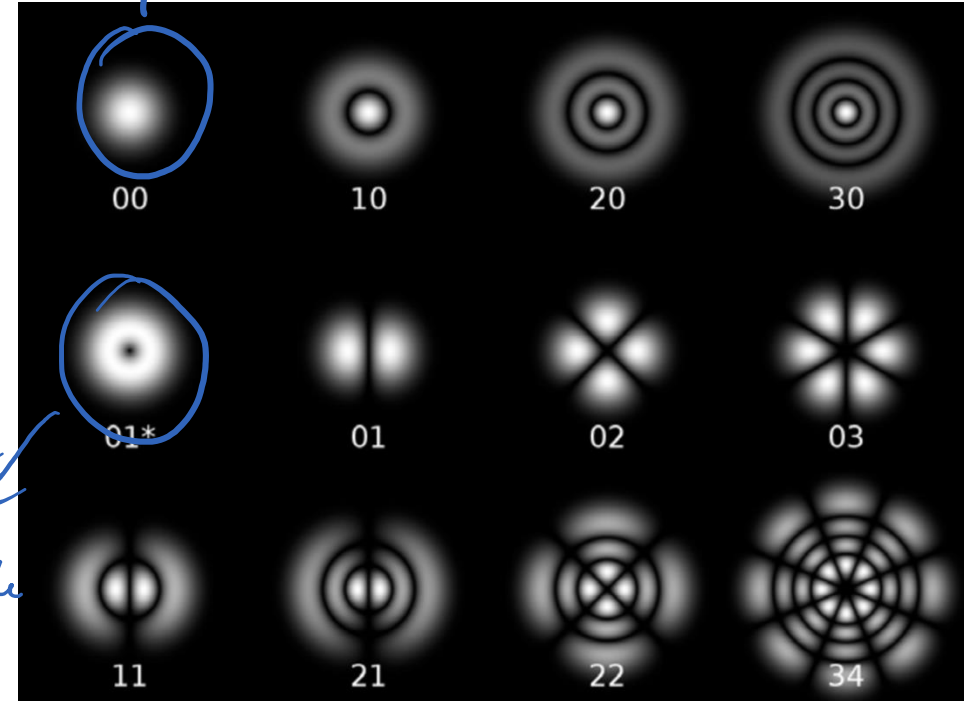


match of
curvature
&
wavefront



↳ very stable cavity

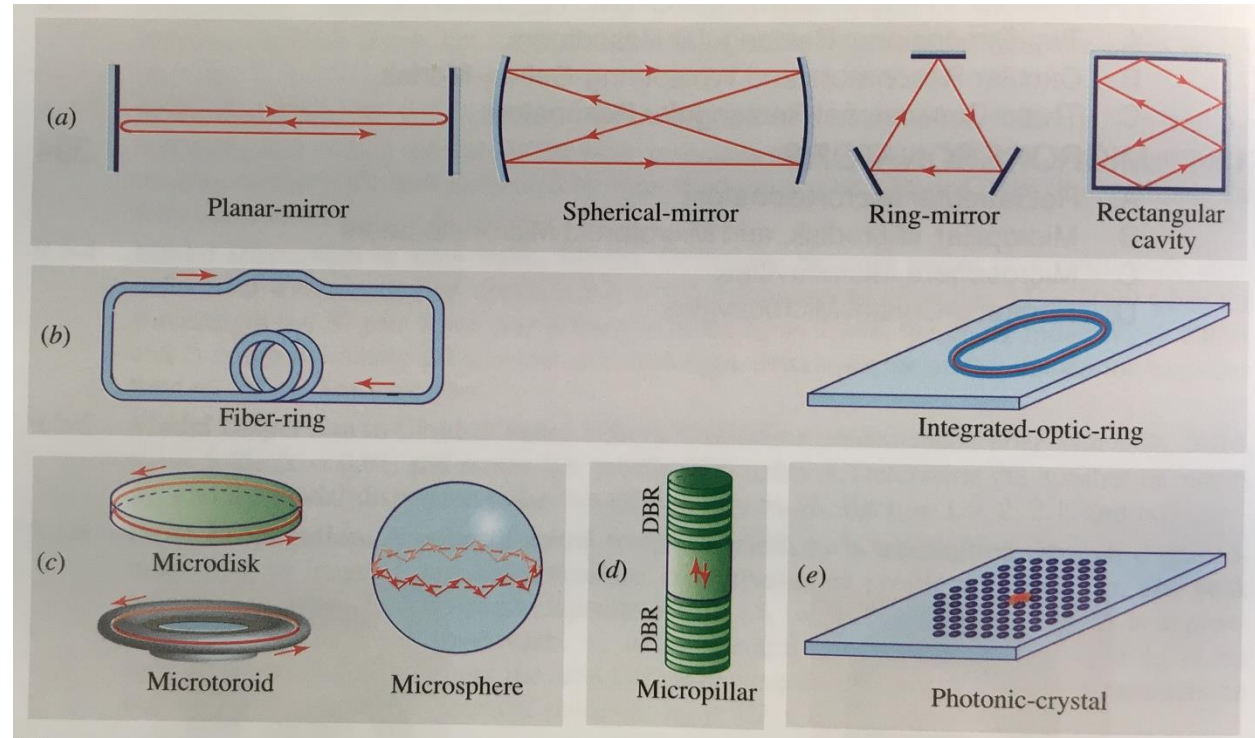
most
common
↑
Laguerre-Gaussian modes



Donut
mode

The Gaussian beam is a mode of the spherical resonator!

Note: There are many other possible cavity configurations!



Application Note: Cavity Ring Down Spectroscopy

- Absorption spectroscopy guided by Beer-Lambert-Law

Extinction $E_\lambda = \log \frac{I_0}{I} = E_\lambda C l$

Handwritten annotations:
- E_λ : extinction factor
- C : concentration
- l : length

- What do to for samples with weak absorption / weak transitions?

Max l

- Solution: Use a cavity!

$$I = I_0 \exp[-\alpha l]$$

Handwritten annotations:
- α : small
- l : max
- $l = c t_e$ (in time)

$$= I_0 \exp[-\alpha c t_e]$$

measure decay time instead → "ring down"

→ light in cavity → 2m of round trips

Homework Reading: Cavity Ring Down Spectroscopy

[View Article Online / Journal Homepage / Table of Contents for this issue](#)

- Idea: Instead of measuring absorption measure decay time

Cavity ring-down spectroscopy

Martyn D. Wheeler, Stuart M. Newman, Andrew J. Orr-Ewing† and Michael N. R. Ashfold
School of Chemistry, University of Bristol, Cantock's Close, Bristol, UK BS8 1TS

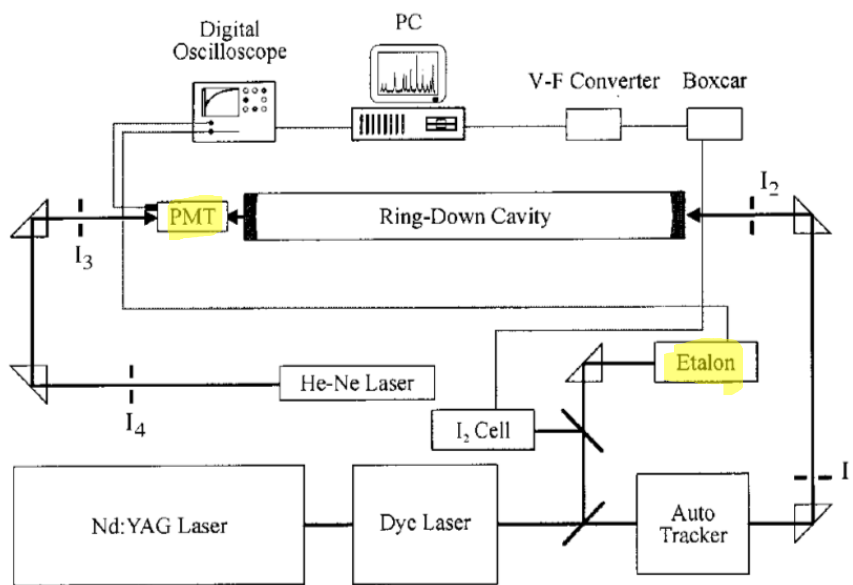


Fig. 2 Schematic diagram of the CRD apparatus at Bristol. Abbreviations in the figure are: photomultiplier tube (PMT), voltage-to-frequency converter (V-F) and irises (I) used to assist cavity alignment. The iodine cell and etalon provide accurate calibration of the laser wavelength.

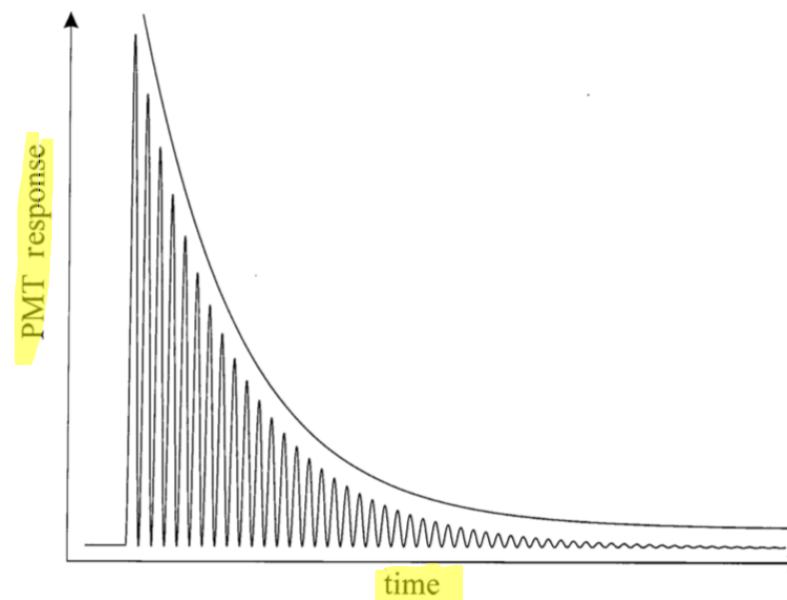
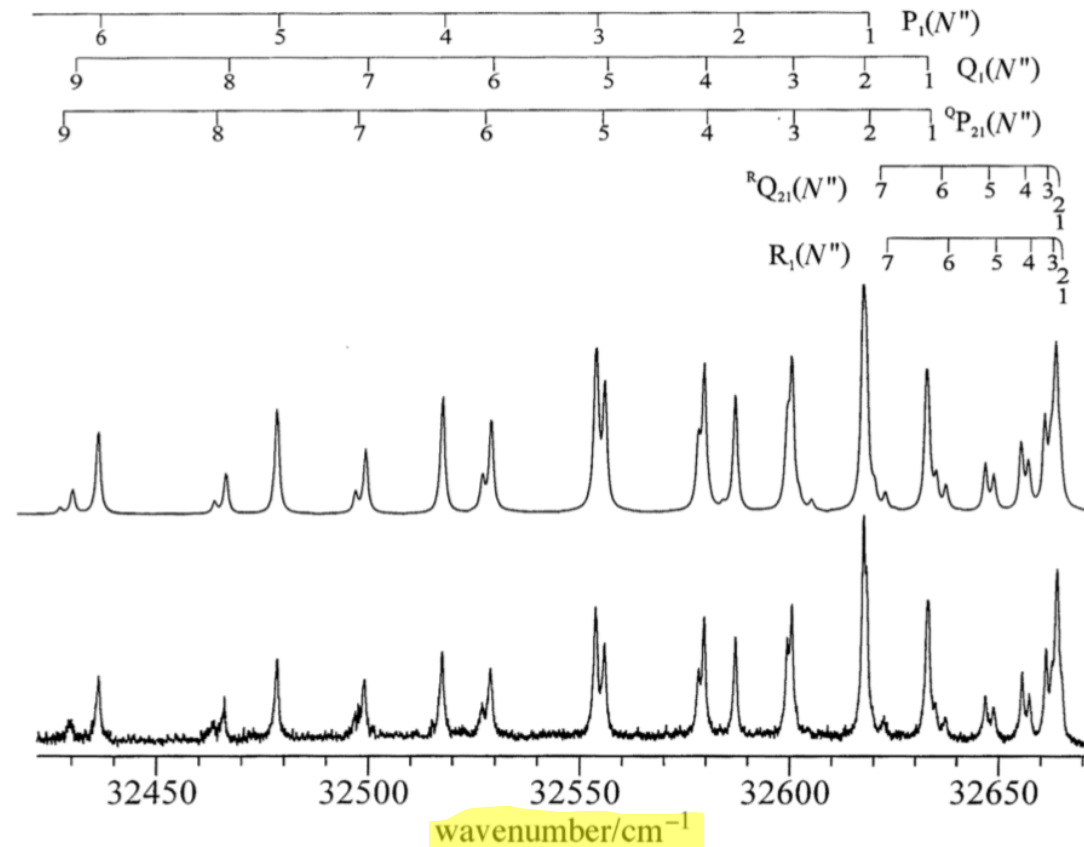


Fig. 3 Schematic diagram of the expected response of the photomultiplier tube to a train of laser pulses leaking through one cavity end mirror after successive cavity round trips. Also shown is the exponential envelope arising from smoothing of the pulse train by the time response of the experimental detection apparatus.

Example spectra

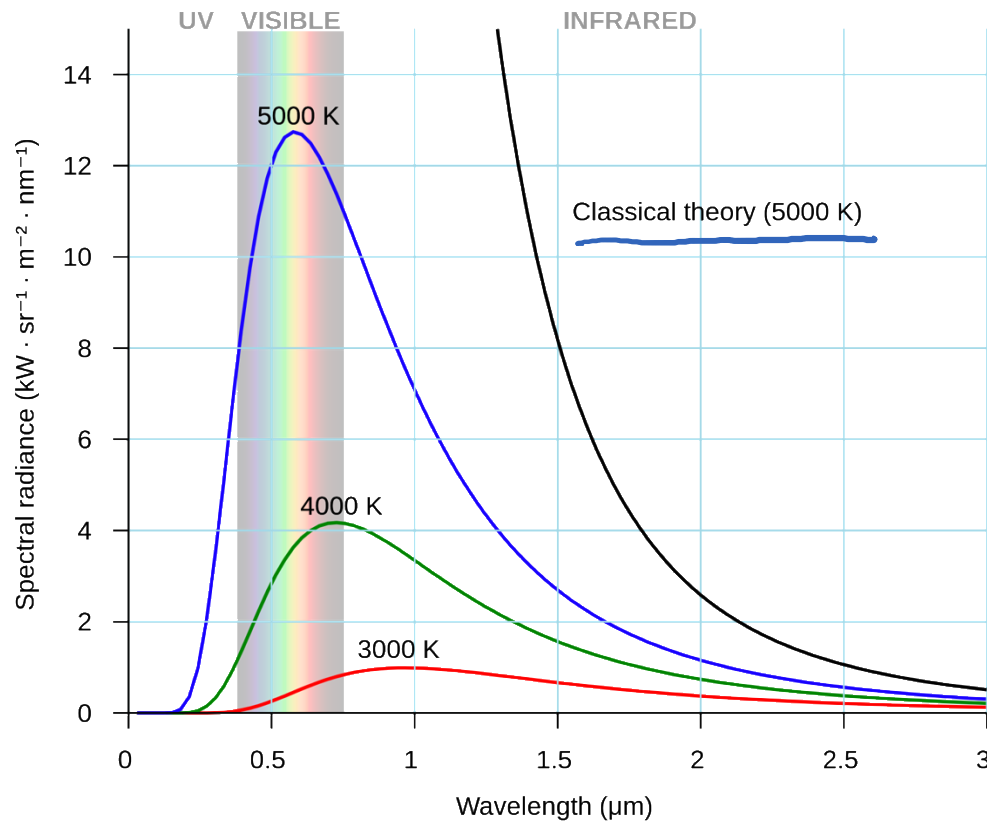


Think about
resolution!

Fig. 8 CRD spectrum (bottom) and simulation (top) of the $A\ ^2\Sigma^+ - X\ ^2\Pi\ (1, 0)$ band of SH. The combs above the spectra indicate rotational line assignments. The simulation includes a Lorentzian component to the rotational linewidths of $1\ \text{cm}^{-1}$ because of lifetime broadening.

And now, towards lasers

Black body radiation: Energy is quantized



- Stefan Boltzmann Law

$$\text{Radiance} \propto T^4$$

- Wiens displacement law

max moves with $\lambda_{\text{max}} \rightarrow \frac{b}{T}$ ← Wiens constant

- Plancks law (Nobel prize 1918)

$$B \approx \frac{2 \hbar \nu^3}{c^2} \frac{1}{\exp\left[\frac{\hbar \nu}{kT} - 1\right]}$$

spectral radiance

$\Rightarrow h \rightarrow \text{energy is quantized!}$

Photoelectric effect (side note) → quantized electromagnetic field

- Einstein Nobel prize 1921
- Light has particle nature

Electrons from metal surface

$$E_{kin} = h\nu - \phi$$

↑

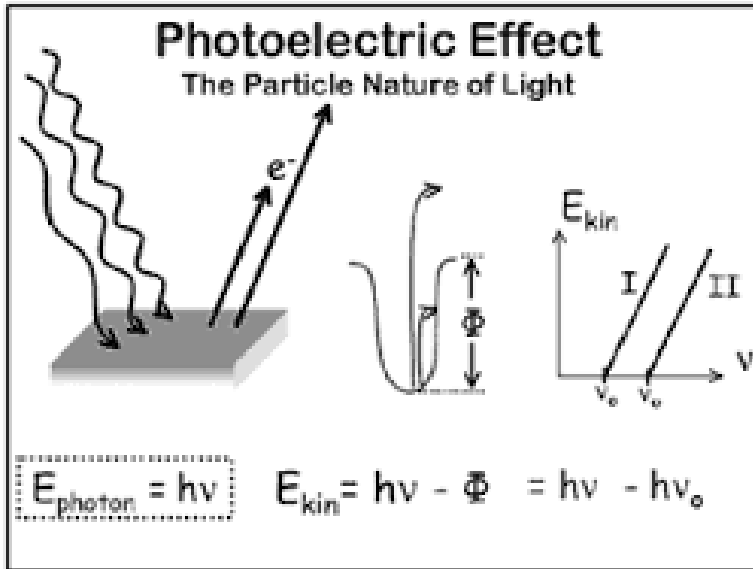
↑

"photon energy"

metal / element
specific
effect

↑

discrete
energy



$$E_{\text{photon}} = h\nu$$

$$E_{\text{kin}} = h\nu - \phi = h\nu - h\nu_0$$

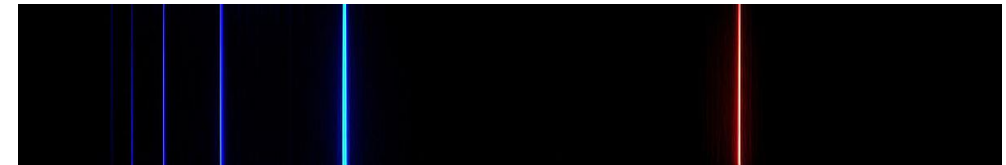
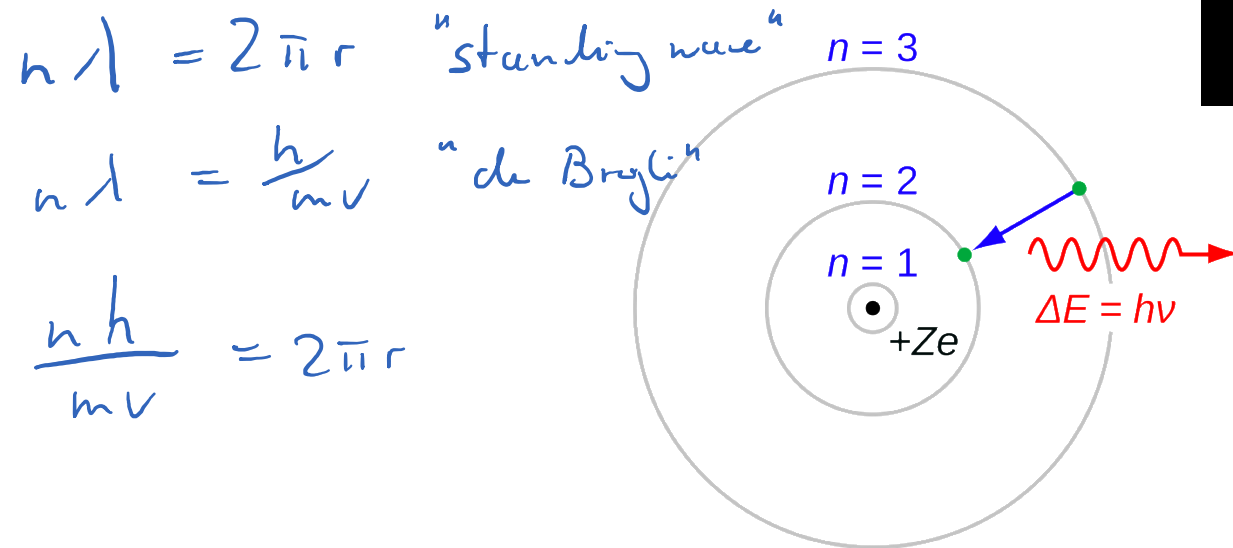
UC Berkeley's Digital Chem1A

⇒ Light behaves as particles
with discrete energy
called "Photons"

Bohr model and Rydberg atoms

- Bohr model: semiclassical approach
- Nobel prize 1922
- Dense nucleus with surrounding electrons
- Discrete energy states
- A lot of shortcomings but works

- Rydberg atom:
- excited states in Bohr model
- Principle quantum numbers n
- Transition under emission / absorption of photon
- Balmer series of hydrogen



Balmer series

$$\frac{1}{\lambda} = R_H \left(\frac{1}{2^2} - \frac{1}{n^2} \right)$$

R_H - Rydberg constant

Fermis Golden Rule (from perturbation theory)

- Full quantum mechanical description of the atom (not here)
- Fermi Golden Rule describes transition probability between levels
- Including selection rules

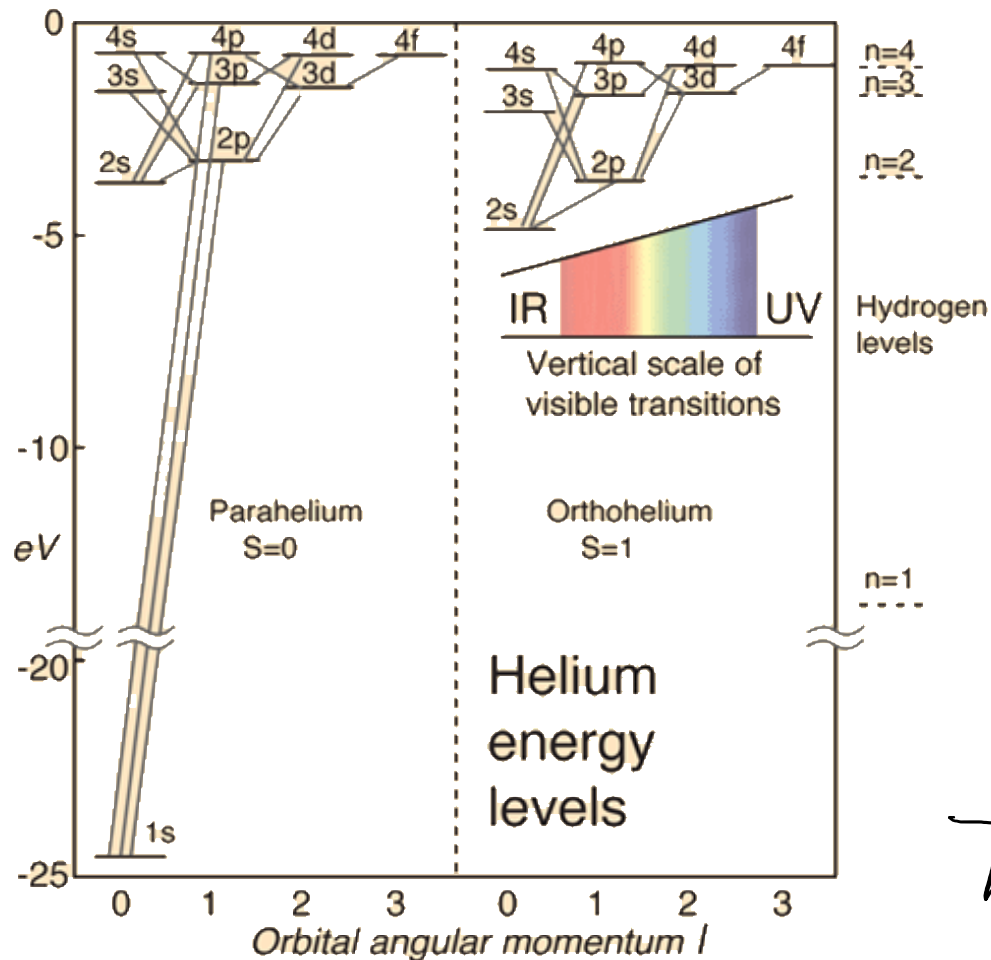
Transition rates

$$\Gamma_{ij} = \frac{2\pi}{\hbar} \underbrace{|\langle f | H' | i \rangle|^2}_{\text{transition matrix element}} \underbrace{\rho(E_f)}_{\text{density of final states}}$$

hand waving argument:

Transition probability depends on orbital overlap and energy + selection rules

Absorption, energy level diagram



$s-p$ dipole allowed $\Delta l = 1$

$s-s$
 $s-d$ } dipole forbidden

selection rule $\Delta l = 1$

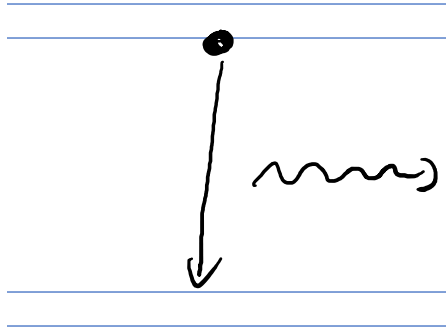
Note photon has $l = 1$

How to populate $2s$ level?

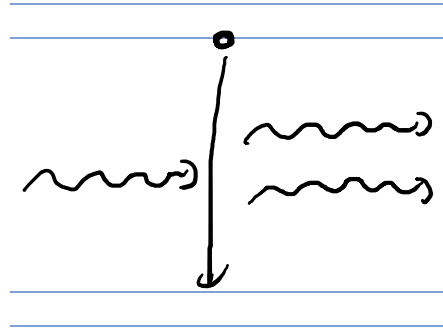
- decay from other levels
- electron impact ionization

Absorption, emission, stimulated emission - overview

Spontaneous emission

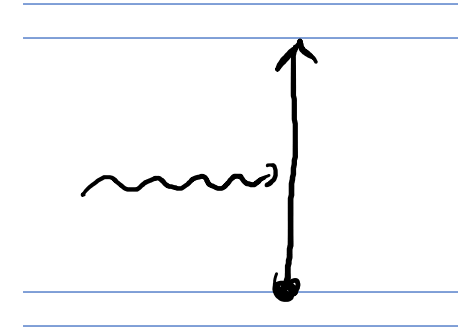


Stimulated Emission



stimulated photon is exact copy of incoming photon with respect to energy, direction, polarization, etc

(Stimulated) absorption



Remember

Population of any level follows Boltzmann distribution

$$N_i = N_0 \cdot \exp\left[-\frac{E_i}{k_B T}\right]$$

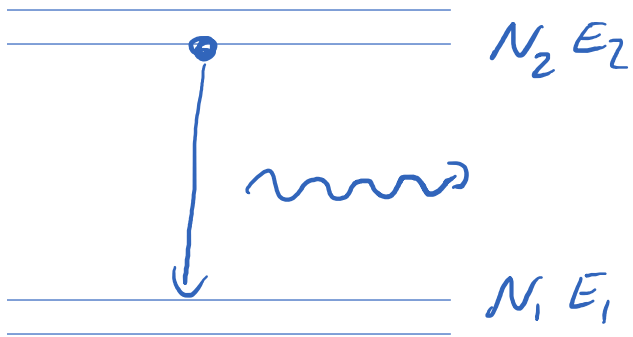
$E_i \rightarrow$ energy of level

↓
the higher the energy the lower the population

Which processes are equivalent? Stimulated emission & absorption! 19

Spontaneous emission

Spontaneous
emission



Energy difference is emitted as photon

$$E_2 - E_1 = h\nu \text{ energy of emitted photon}$$

Describe with Einstein coefficients

"transition is proportional to population"

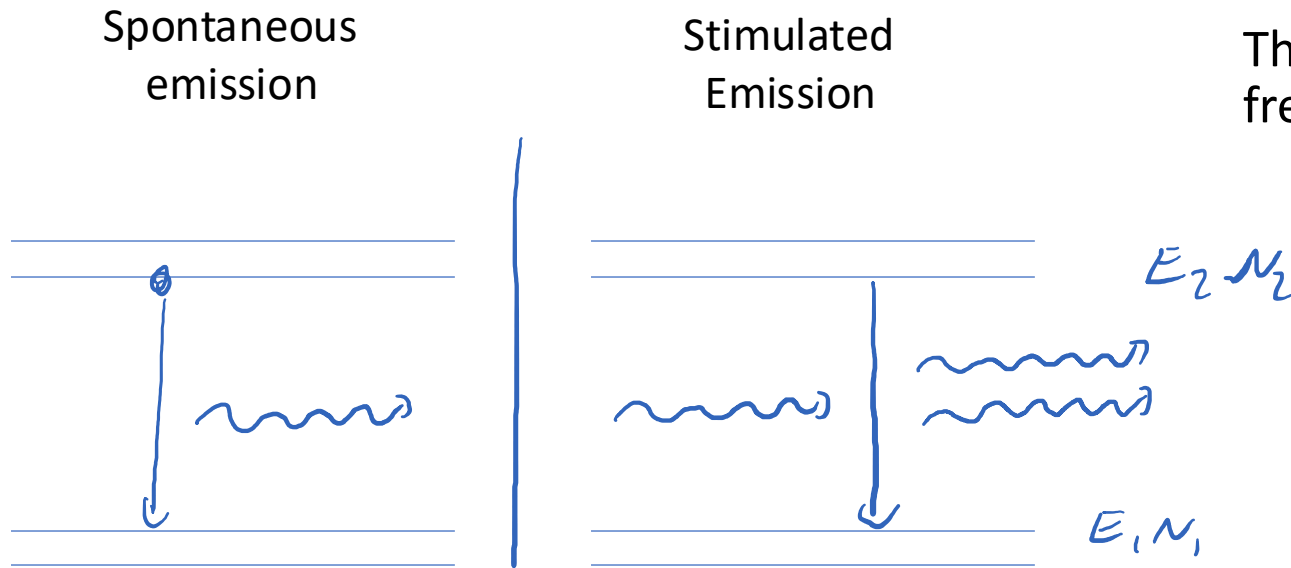
$$\frac{dN_2}{dt} = -A N_2$$

A - Einstein coefficient

Stimulated emission

One photon with $h\nu$ stimulates another transition

The second photon is identical in direction, frequency, phase and polarization



$$\frac{dN_2}{dt} = -\omega_{21} N_2$$

ω_{21} - stimulated transition probability

ω_{21} - stimulated transition probability

ω_{21} - depends on intensity of incoming light $\rightarrow$ flux

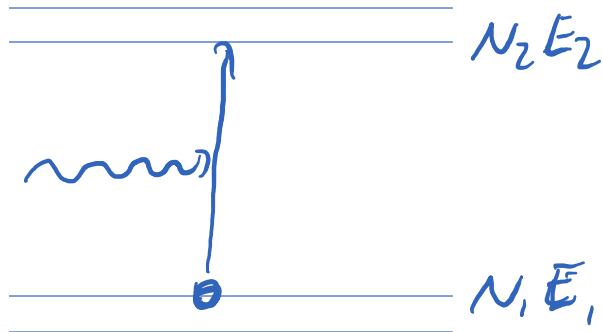
$$\omega_{21} = \sigma_{12} F = B_{21} S \rho$$

$\uparrow$ transition probability $\uparrow$ Flux $\uparrow$ Einstein coefficient $\uparrow$ energy density

Absorption

- The photon stimulates from lower to higher state

(Stimulated)
Absorption



$$\frac{dN_1}{dt} = -\omega_{12} N_1$$

similar $\omega_{12} = \sigma_{12} \bar{F} = B_{12} S_{\omega}$

Einstein showed $\sigma_{12} = \sigma_{21}$

$\Rightarrow$ electron within atom in ground state is equally probable of going up as one in excited state of going down

Atoms (systems) in thermal balance

In thermal balance the lower population is always higher than that of the upper population

↳ Boltzmann distribution

$$N_i = N_0 \exp \left[\frac{-E_i}{k_B T} \right]$$

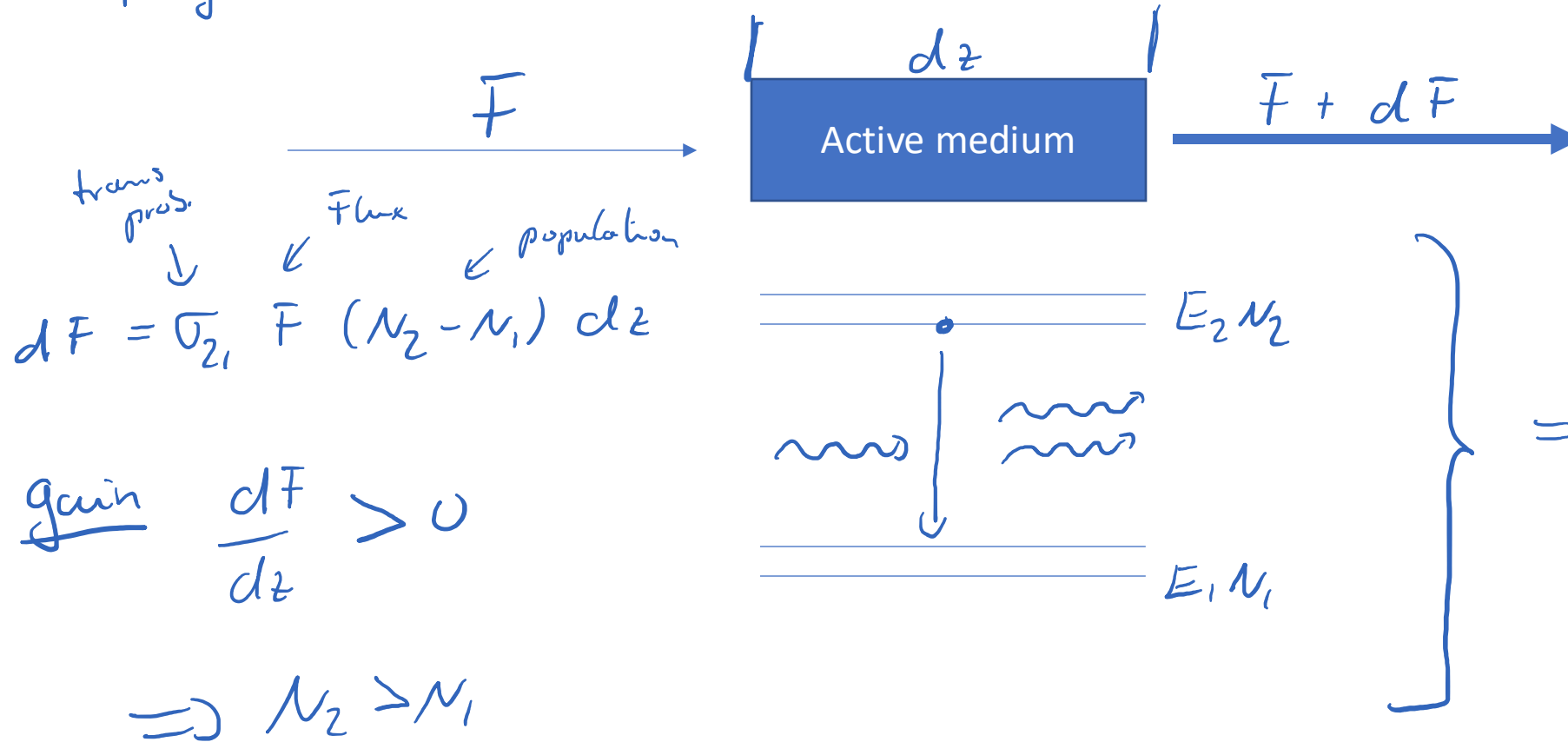
↳ higher energy levels are less populated

$$\frac{N_2}{N_1} = \exp \left[- \frac{(E_2 - E_1)}{k_B T} \right] = \exp \left[- \frac{\Delta E}{k_B T} \right]$$

$\Rightarrow N_2 < N_1 \Rightarrow$ absorption dominates in
thermal equilibrium (in 2 level system)

Fundamental concept of laser

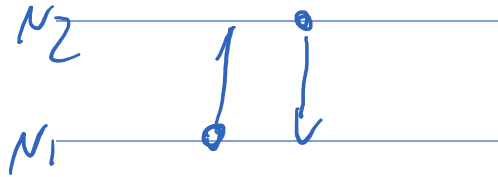
$\bar{F}$ - flux



Note: The gain must always be higher than the losses!

2, 3, 4 level systems

2 level system



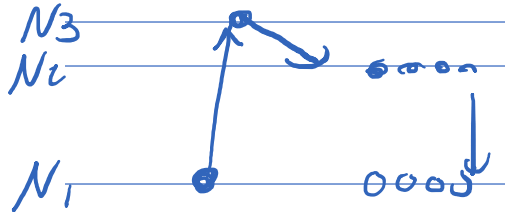
population inversion not possible
even with highest flux $N_2 = N_1$

↪ stimulated emission and absorption are in balance

high flux

medium
becomes
transparent!

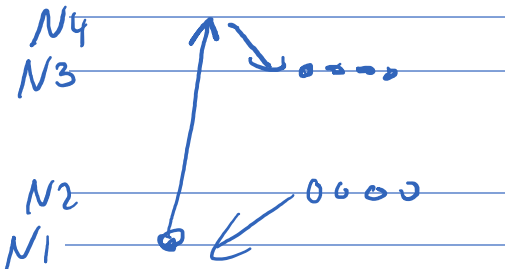
3 level system



metastable

} lasing line → N_2 populated over time → inversion

4 level system

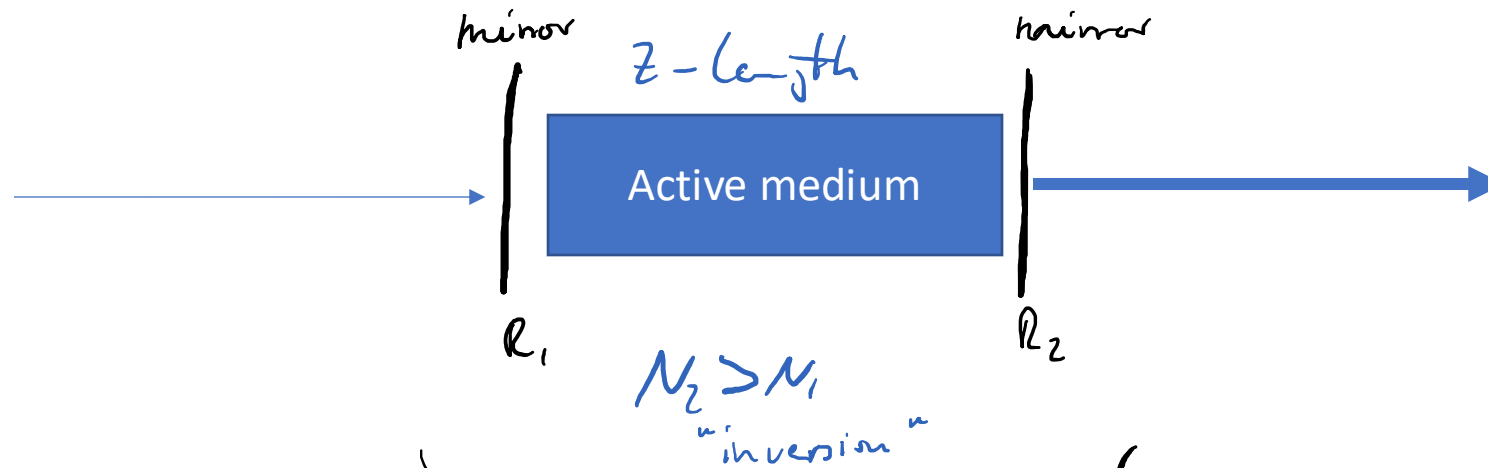


long lifetime

always empty

} lasing line

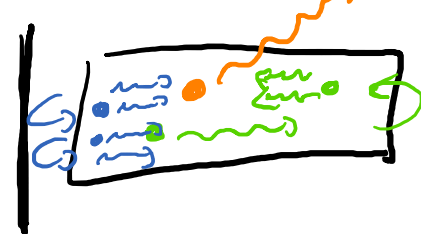
Fundamental concept of laser oscillator:



$$\frac{dF}{dz} > 0 \quad \text{"gain"}$$

$$dF = \sigma_{21} F (N_2 - N_1) dz$$

$$\leadsto \text{gain} \sim \exp[\sigma_{21} (N_2 - N_1) z]$$



exponential growth
of output on axis!

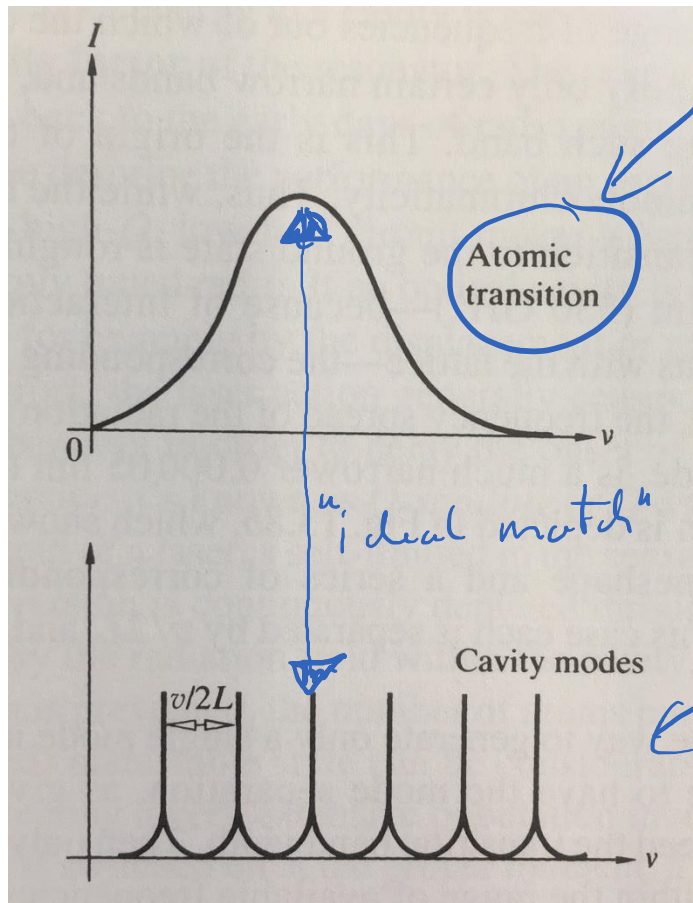
Note: The gain must always be higher than the losses! $\rightarrow$ add minor reflectivities

$$R_1 R_2 \exp[\sigma_{21} (N_2 - N_1) l] \geq 1$$

Lasing condition ²⁶

Lasers and laser cavities

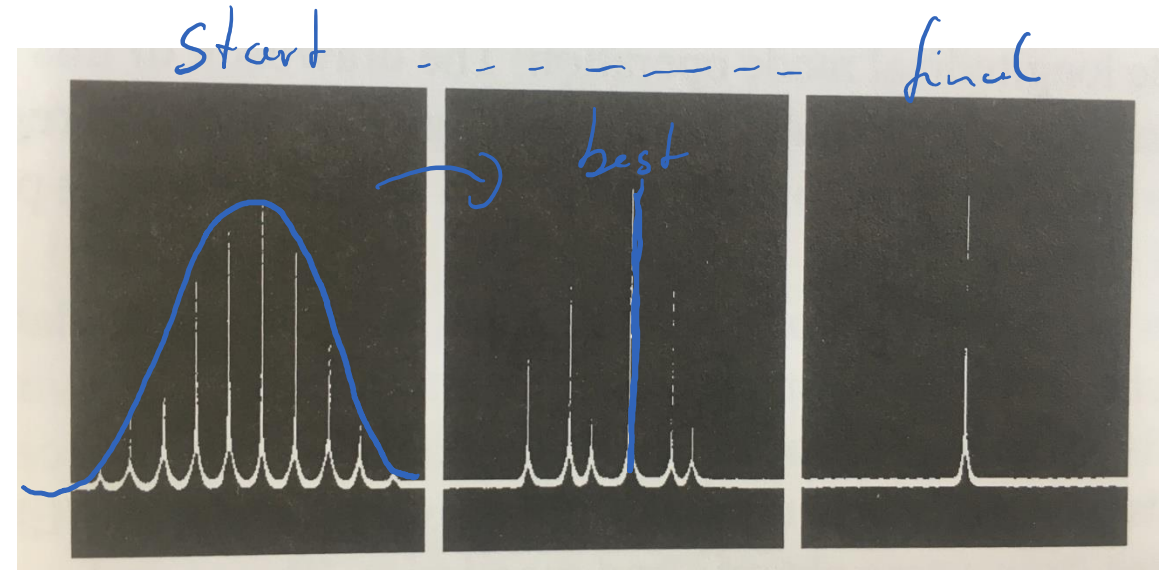
Atomic lines vs cavity modes



broadened
by lifetime,
Doppler, etc

cavity only
supports
selected
modes

Mode selection

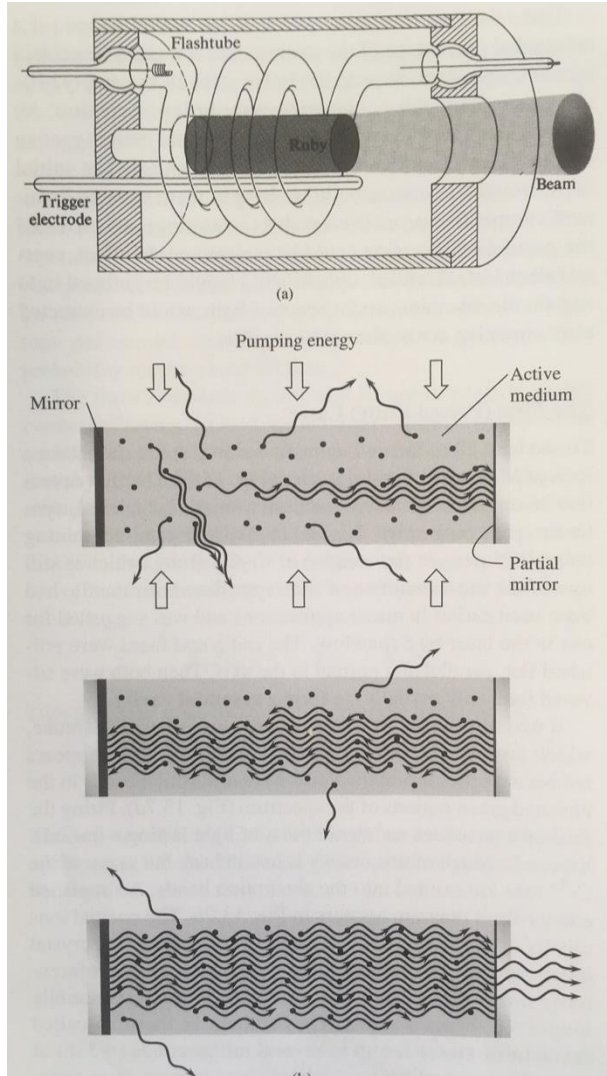


convolution
cavity & atomic
lines

only strongest
mode survives!

Cavity important part
of laser

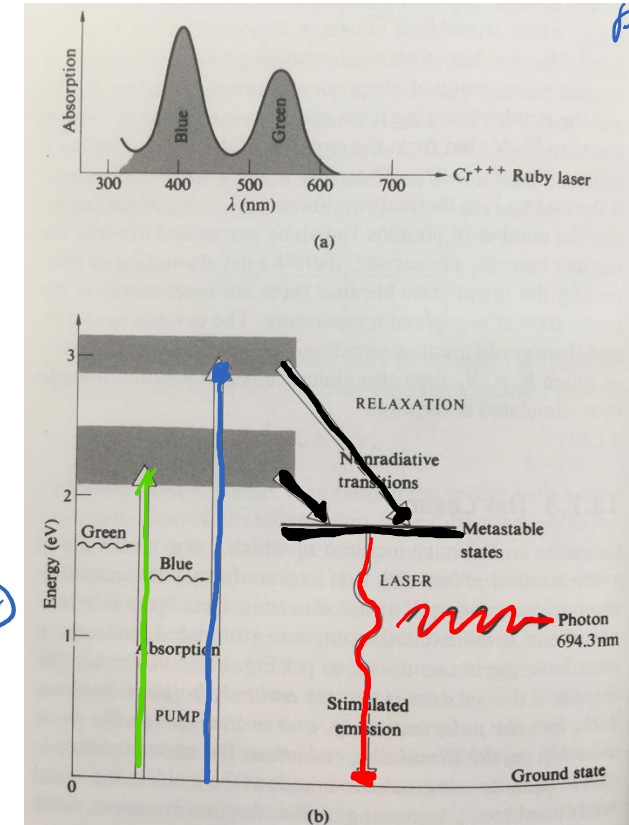
The Ruby laser



1st Laser

Al_2O_3 crystal
with Cr_2O_3
active sites

broad absorption
↳ absorbs energy
from flash light
pumping



The end.

Fabry Perot Interferometer

Na D line:

