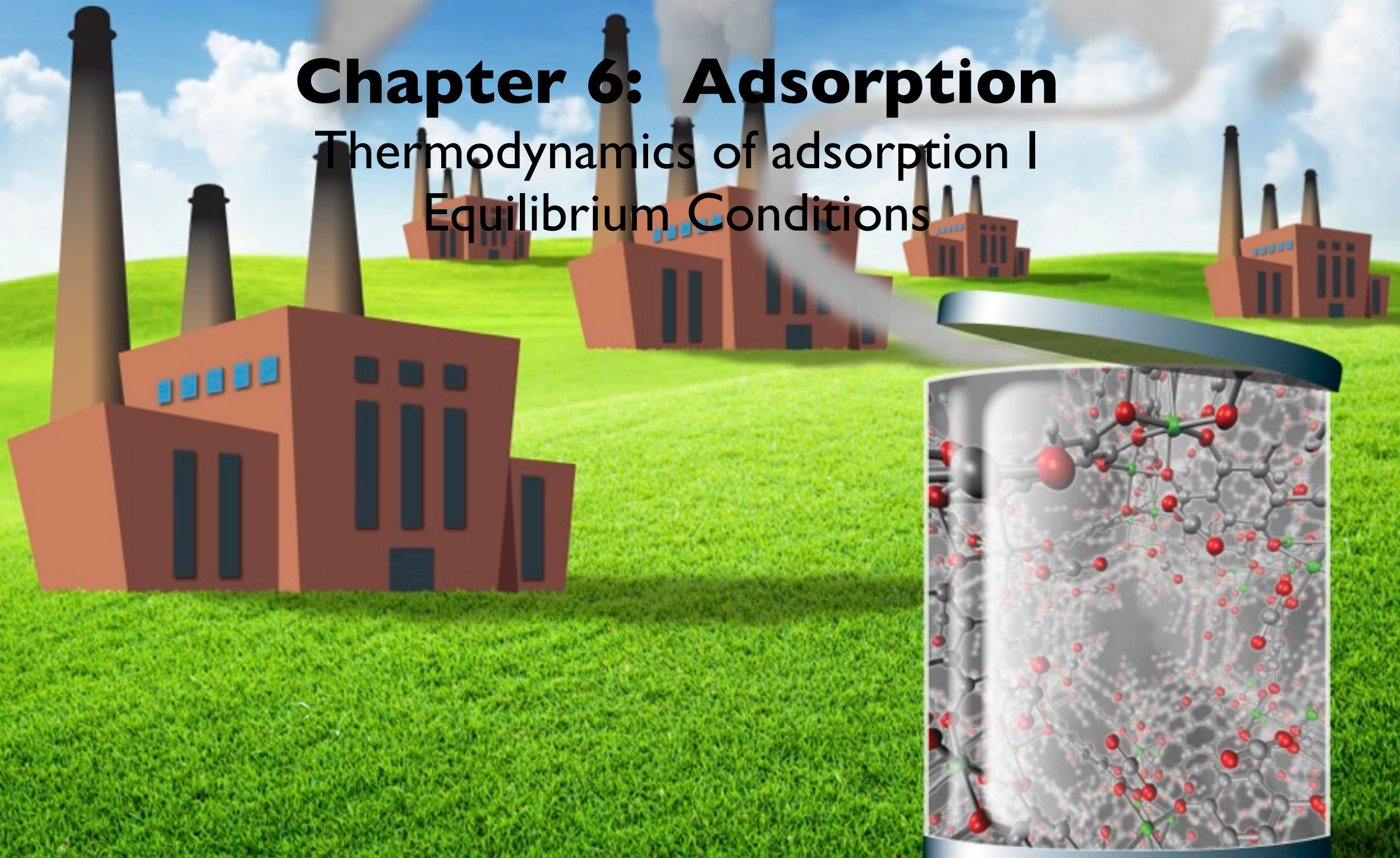


Introduction to Carbon Capture and Sequestration

Chapter 6: Adsorption

Thermodynamics of adsorption I
Equilibrium Conditions



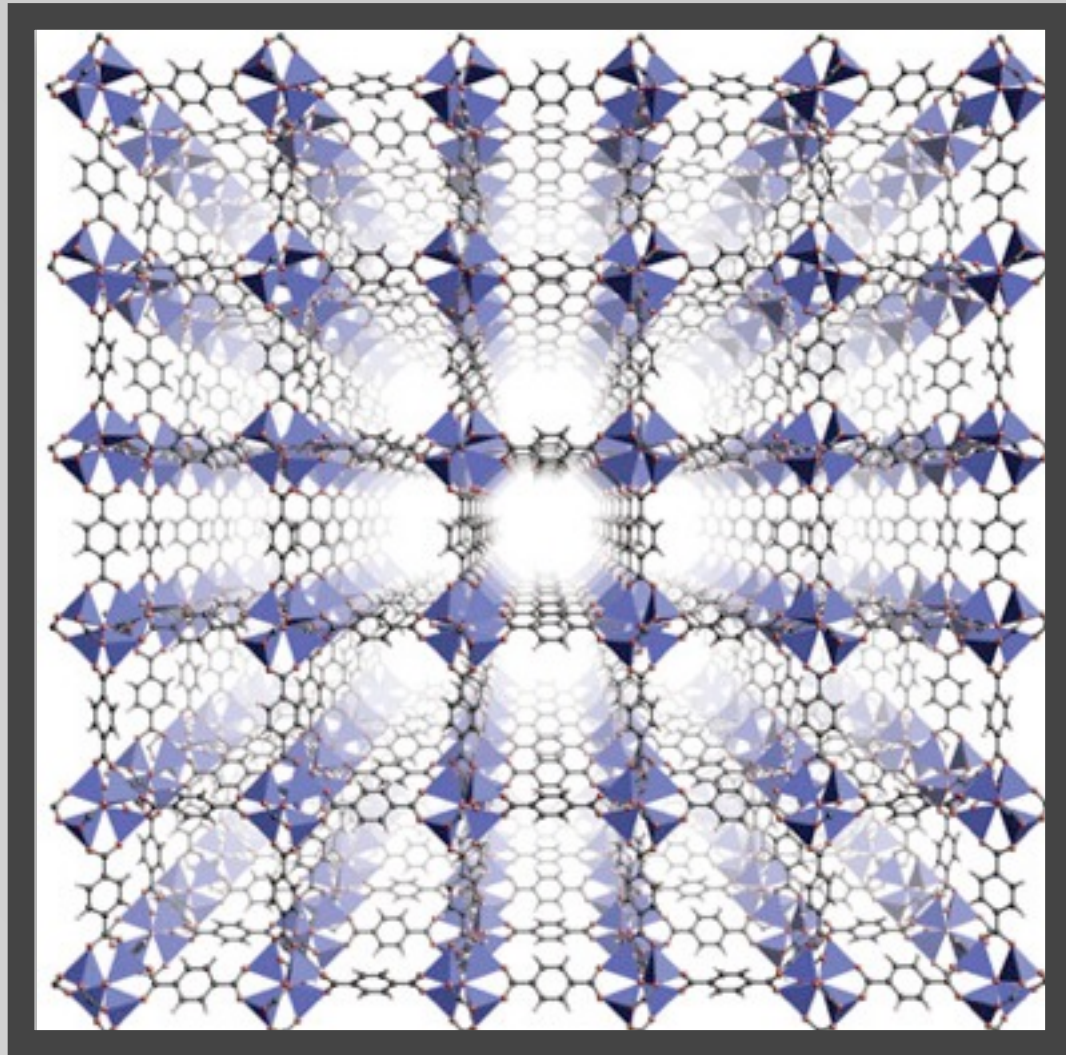
Chapter 6: Adsorption

Thermodynamics of Adsorption I

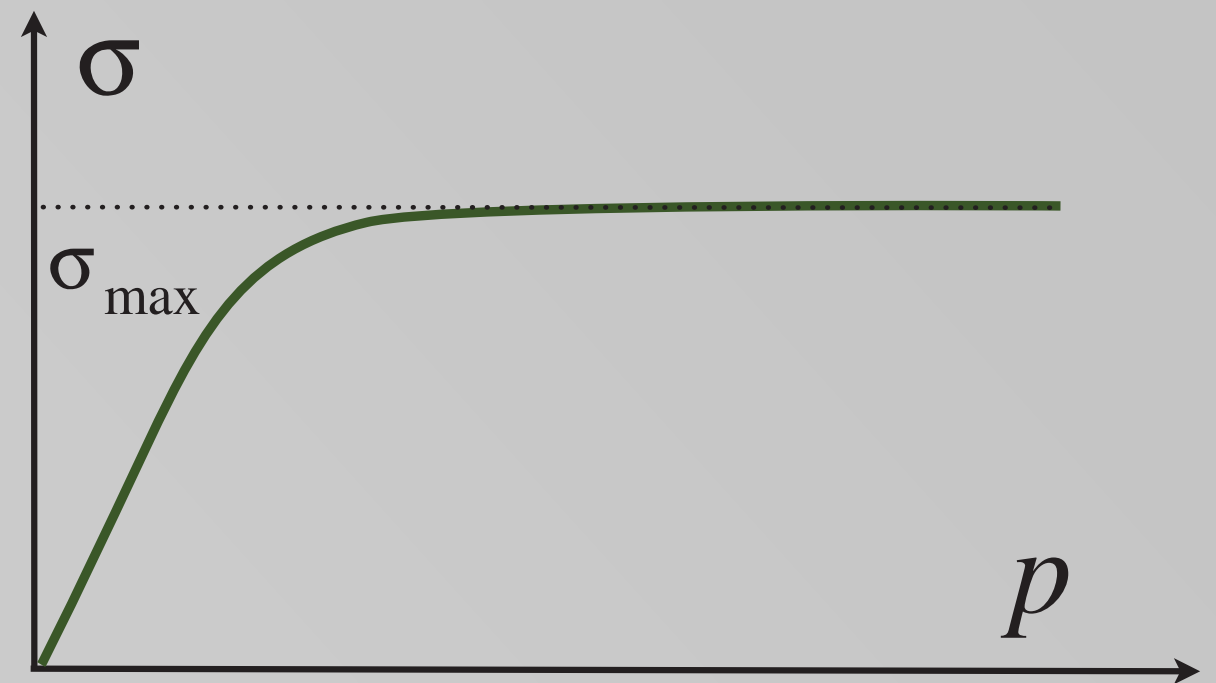
(equilibrium conditions)

- Pressure in solids
- Equilibrium conditions
- Adsorption in rocks and nano-porous materials

Thermodynamics of adsorption

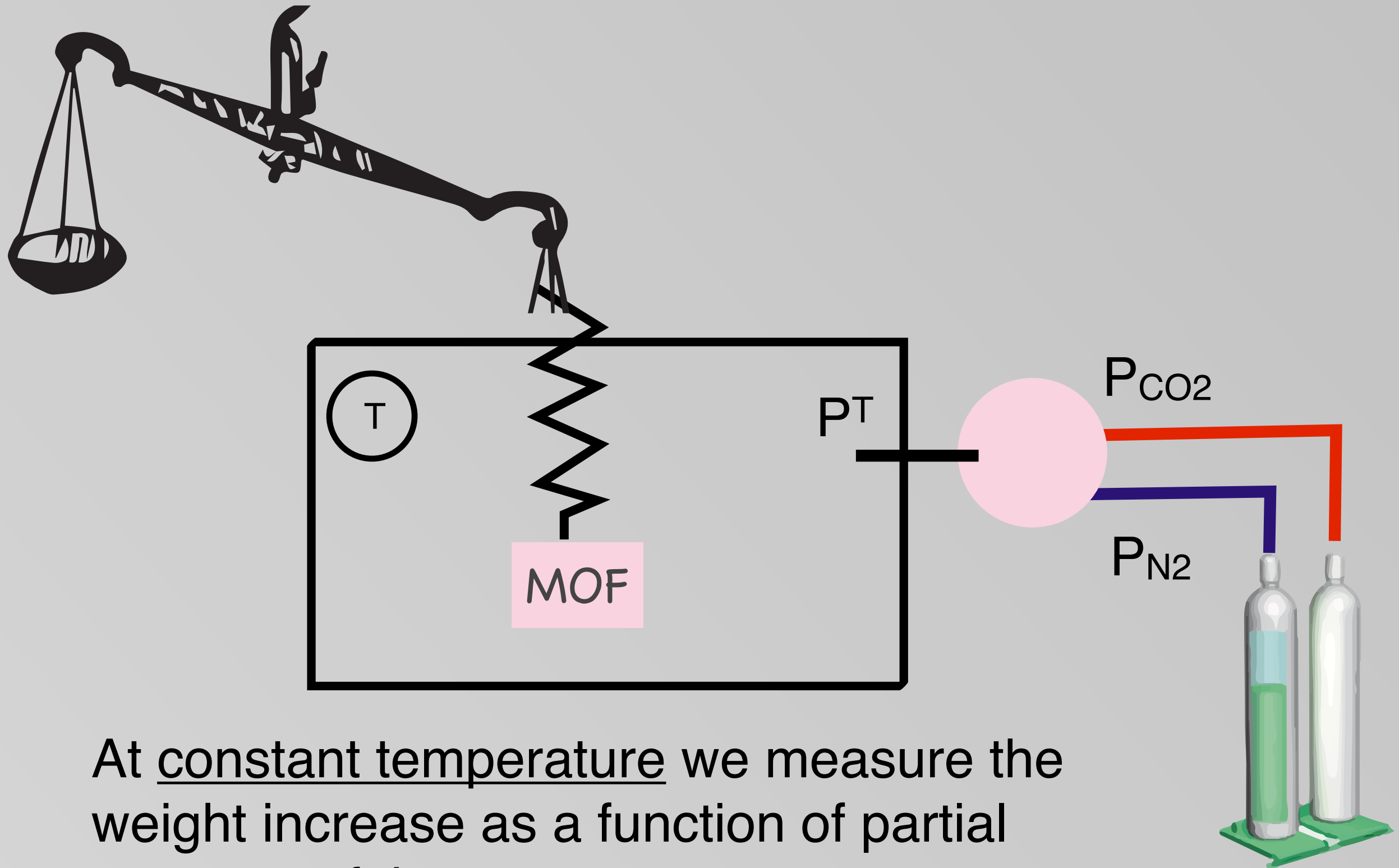


Metal Organic Framework



What are the appropriate thermodynamic variables?

Experimental setup



At constant temperature we measure the weight increase as a function of partial pressure of the gas

Thermodynamics of adsorption

What is the thermodynamic language of adsorption?

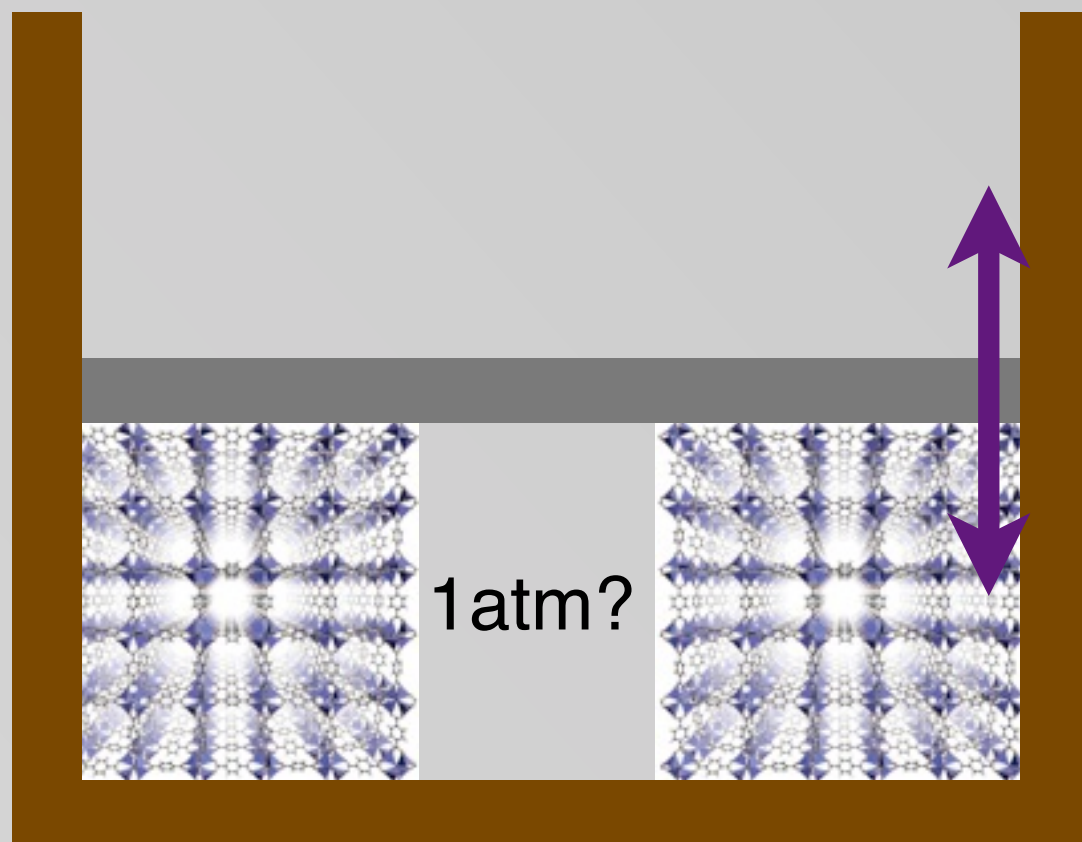
What are the equilibrium conditions?

Can we make a molecular model of adsorption?

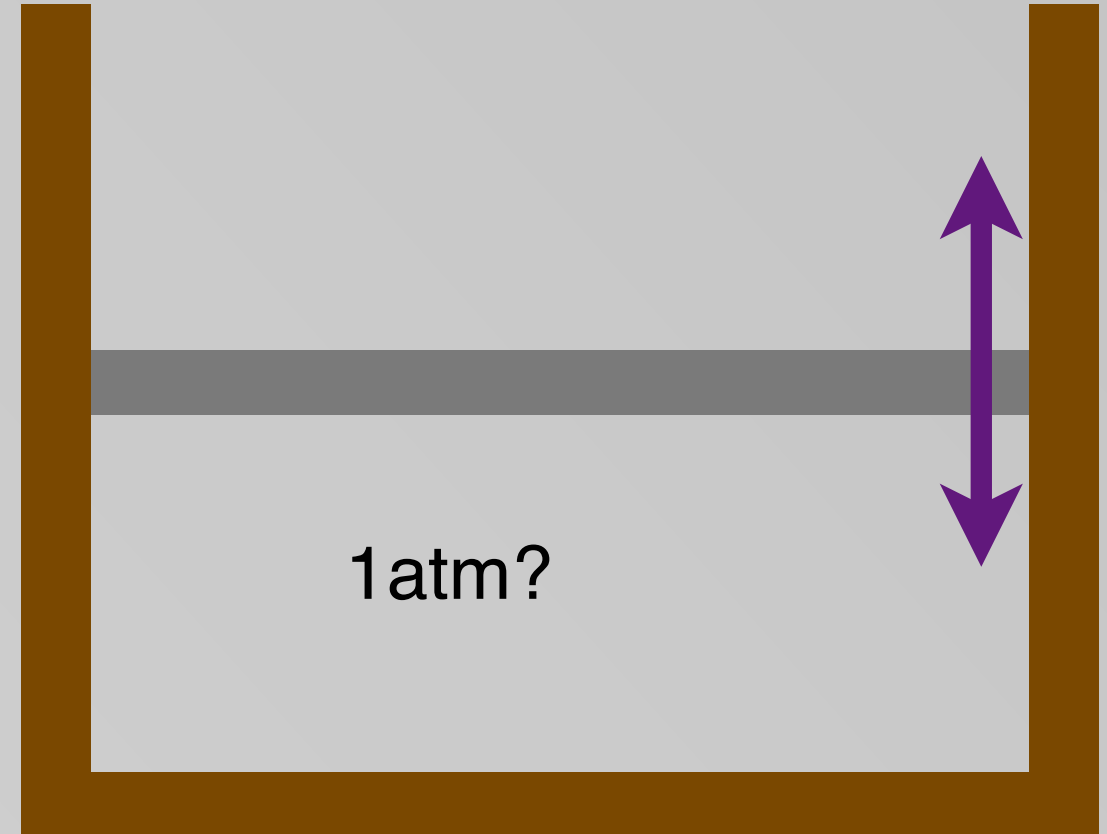
Pressure in Solids

How do we look at pressure in a solid?

Is pressure in a solid defined?



Gas + solid



Gas

Pressure

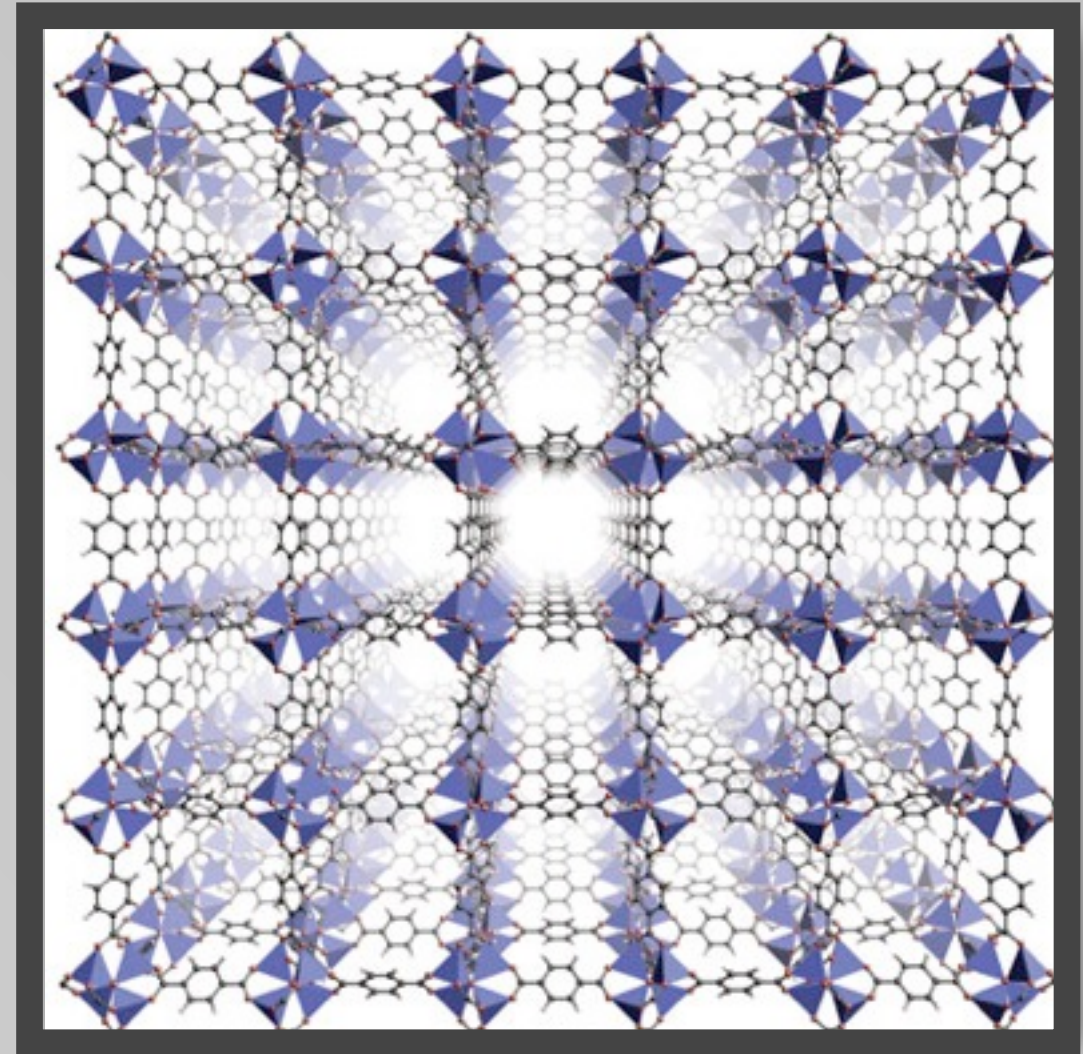
$$p = -\left(\frac{\partial F}{\partial V}\right)_{T,N}$$

In a solid the free energy change to change the volume can be **anisotropic**

Is described by a **stress tensor**

Unlike a fluid a solid can resist strain; forces are much larger

Does the adsorption isotherm of a brick change if we stand on it?

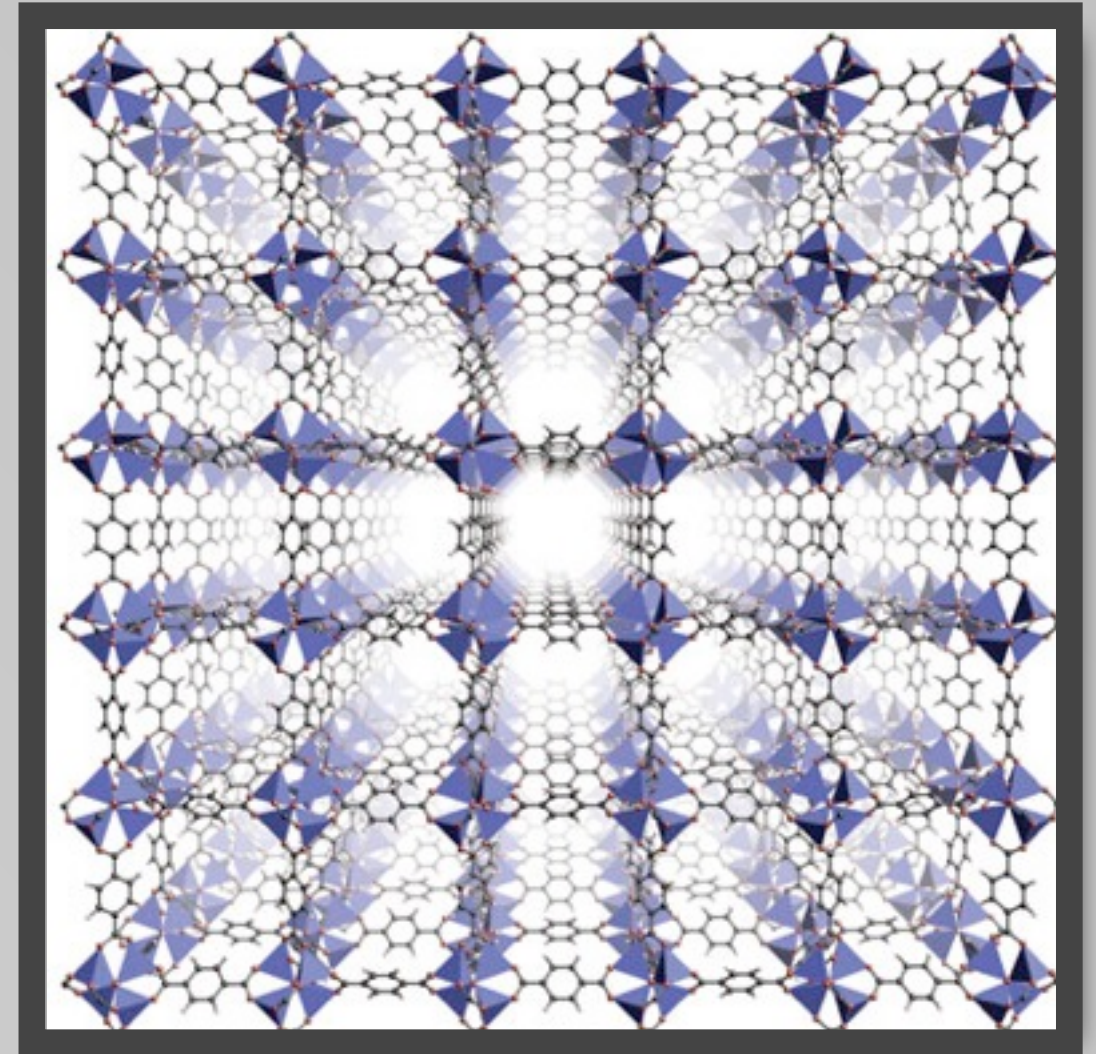


Pressure in a solid

Let us assume that in the pressure range of the isotherm the solid does not deform

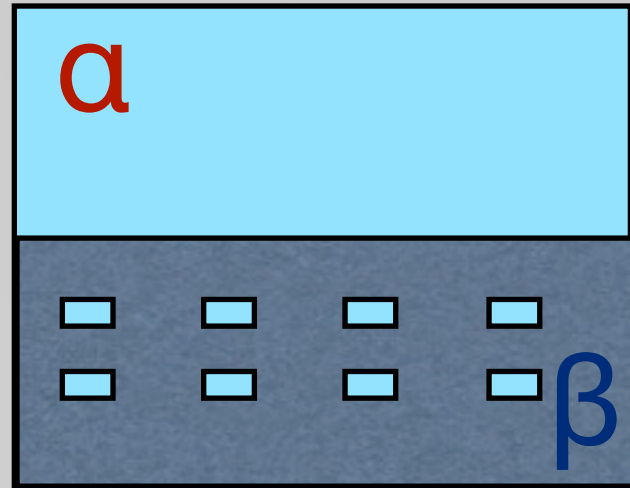
Hence,

$$\left(\frac{\partial F}{\partial V} \right)_{T,N} = \infty$$



We cannot change the **volume** of our solid;
hence **pressure is not defined** inside the solid.

For these adsorption studies the pressure of the gas phase is not the preferred thermodynamic variable!



Equilibrium

A solid phase β and a large reservoir which is the fluid phase α

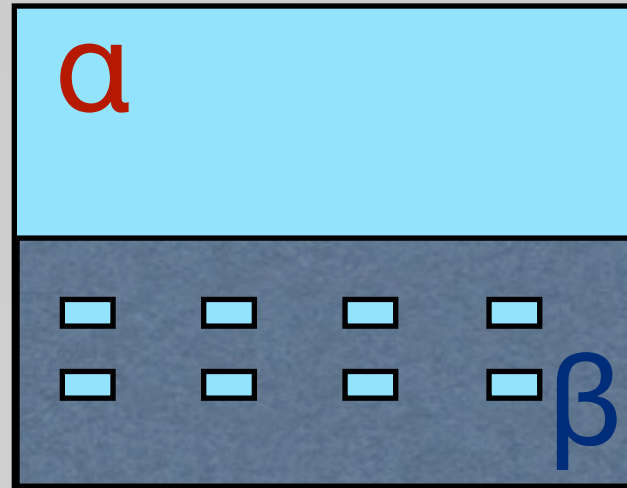
Question: When are these two systems in equilibrium?

Equilibrium: 2nd Law of Thermodynamics

For a system at constant energy U , number of particles N , and volume V : entropy is maximal

Total system NVU : **$dS \geq 0$**

$$dS = dS_{\alpha} + dS_{\beta} \geq 0$$



Total system NVU: $dS \geq 0$

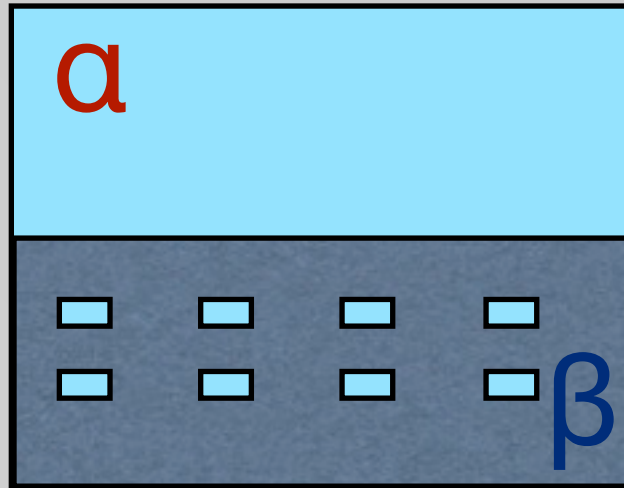
$$dS = dS_{\alpha} + dS_{\beta} \geq 0$$

Chemical potential of component i

1st Law of Thermodynamics:

$$dU = TdS - pdV + \sum_i \mu_i dN_i$$

the change in internal energy if we add a particle while keeping the entropy and volume constant



Total system NVU: $dS \geq 0$

$$dS = dS_{\alpha} + dS_{\beta} \geq 0$$

$$dS_{\beta} = \frac{1}{T_{\beta}} dU_{\beta} + \cancel{\frac{p}{T_{\beta}} dV_{\beta}} - \sum_i \frac{\mu_i^{\beta}}{T_{\beta}} dN_i^{\beta}$$

As the total system is at constant U and N :

$$dU_{\alpha} + dU_{\beta} = 0$$

$$dN_{\alpha} + dN_{\beta} = 0$$

$$dS_{\alpha} + dS_{\beta} = \left(\frac{1}{T_{\alpha}} - \frac{1}{T_{\beta}} \right) dU_{\alpha} - \sum_i \left(\frac{\mu_i^{\alpha}}{T_{\alpha}} - \frac{\mu_i^{\beta}}{T_{\beta}} \right) dN_i^{\alpha}$$

Equilibrium:

$$T_{\alpha} = T_{\beta} \quad \wedge \quad \mu_i^{\alpha} = \mu_i^{\beta}$$

Equilibrium: the adsorbed gas has an equal temperature and chemical potential as the reservoir

Capillary Forces



What is the pressure difference between the inside and the outside of the bubble?

$$-\Delta p \delta V + \gamma \delta A = 0$$

$$A = 4\pi R^2$$

$$V = \frac{4}{3}\pi R^3$$

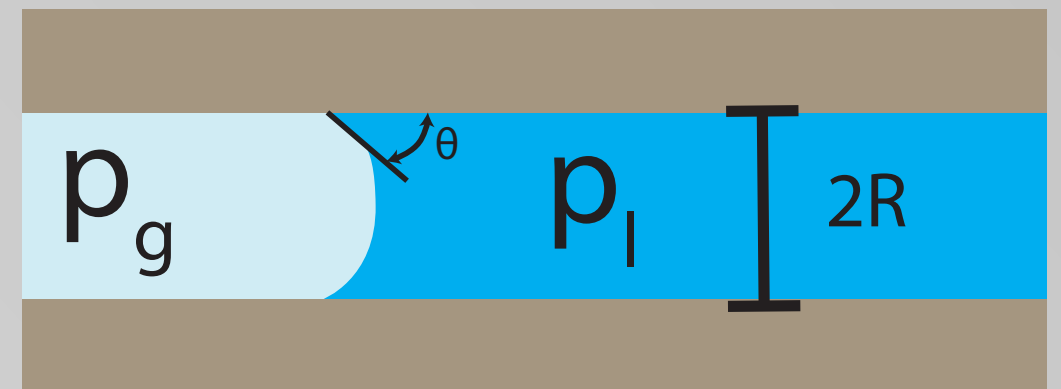
$$\frac{dA}{dV} = \frac{2}{R}$$

Hence,

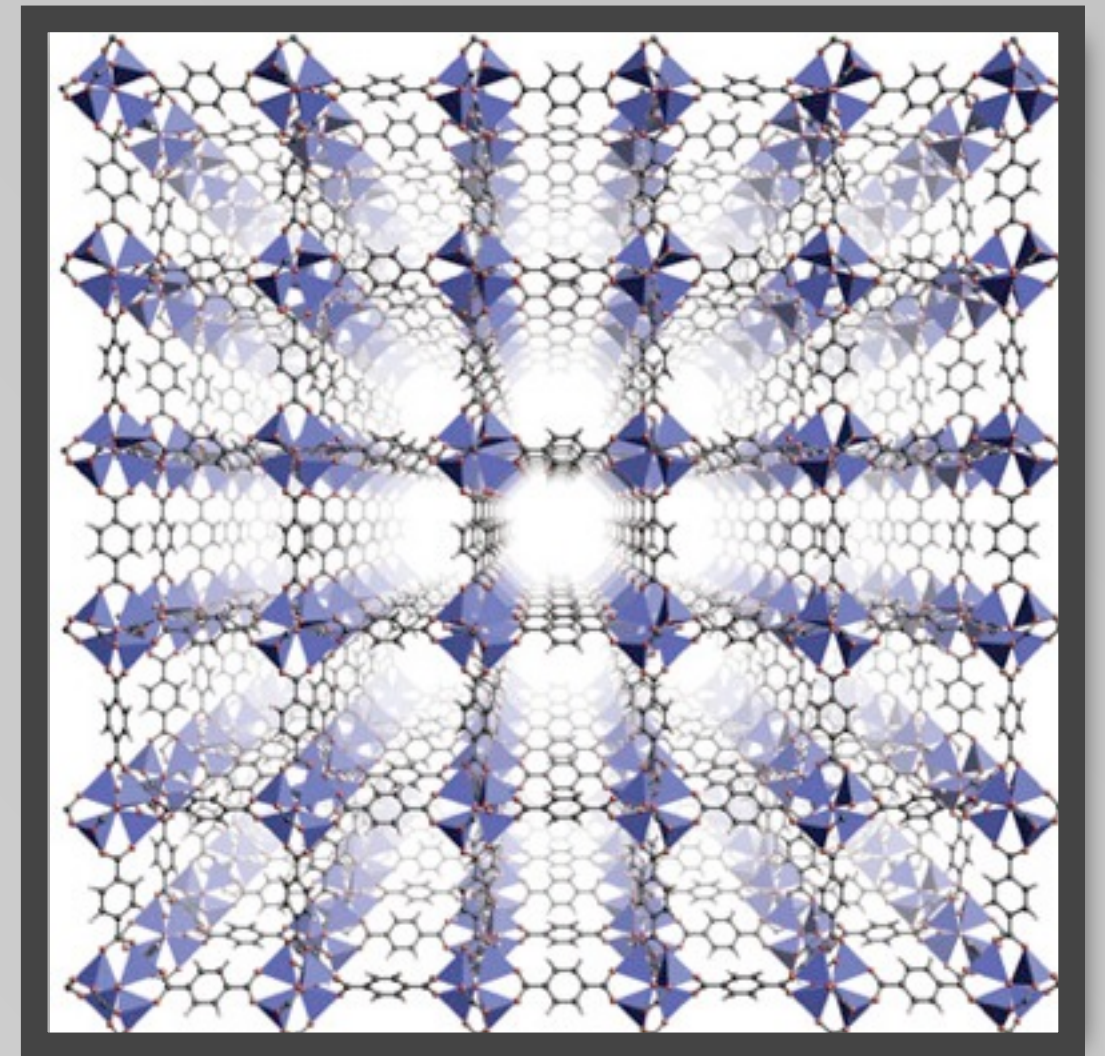
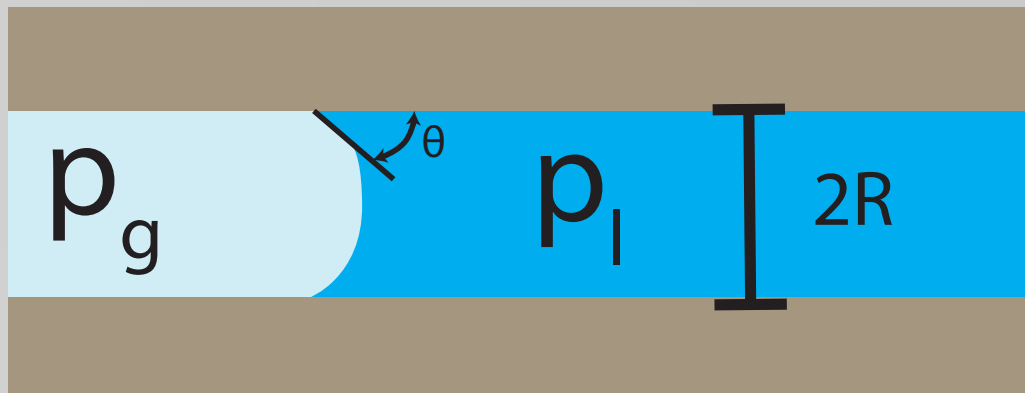
$$\Delta p = \frac{2\gamma}{R}$$

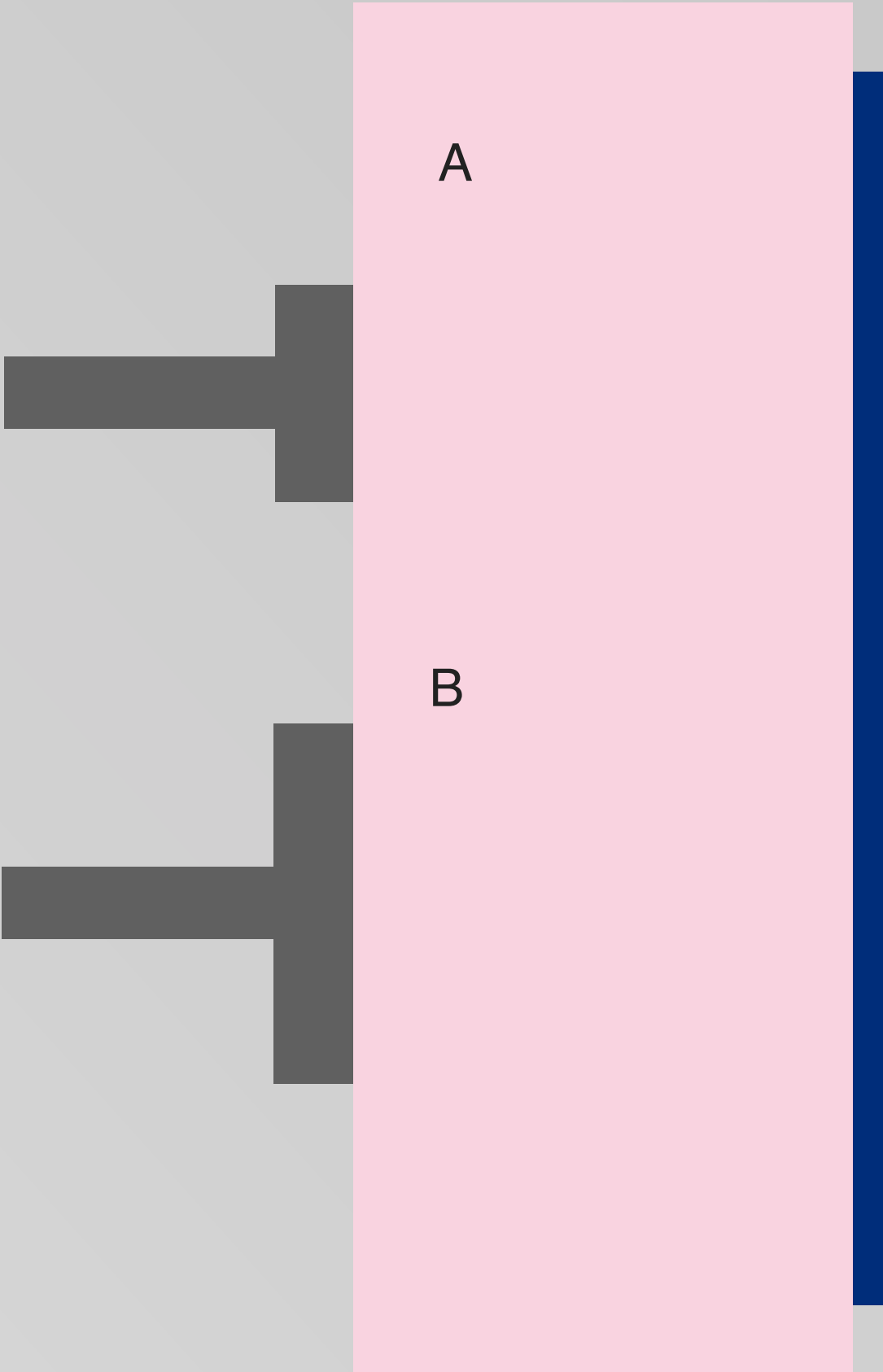
More general shape:

$$\Delta p = \gamma \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$$

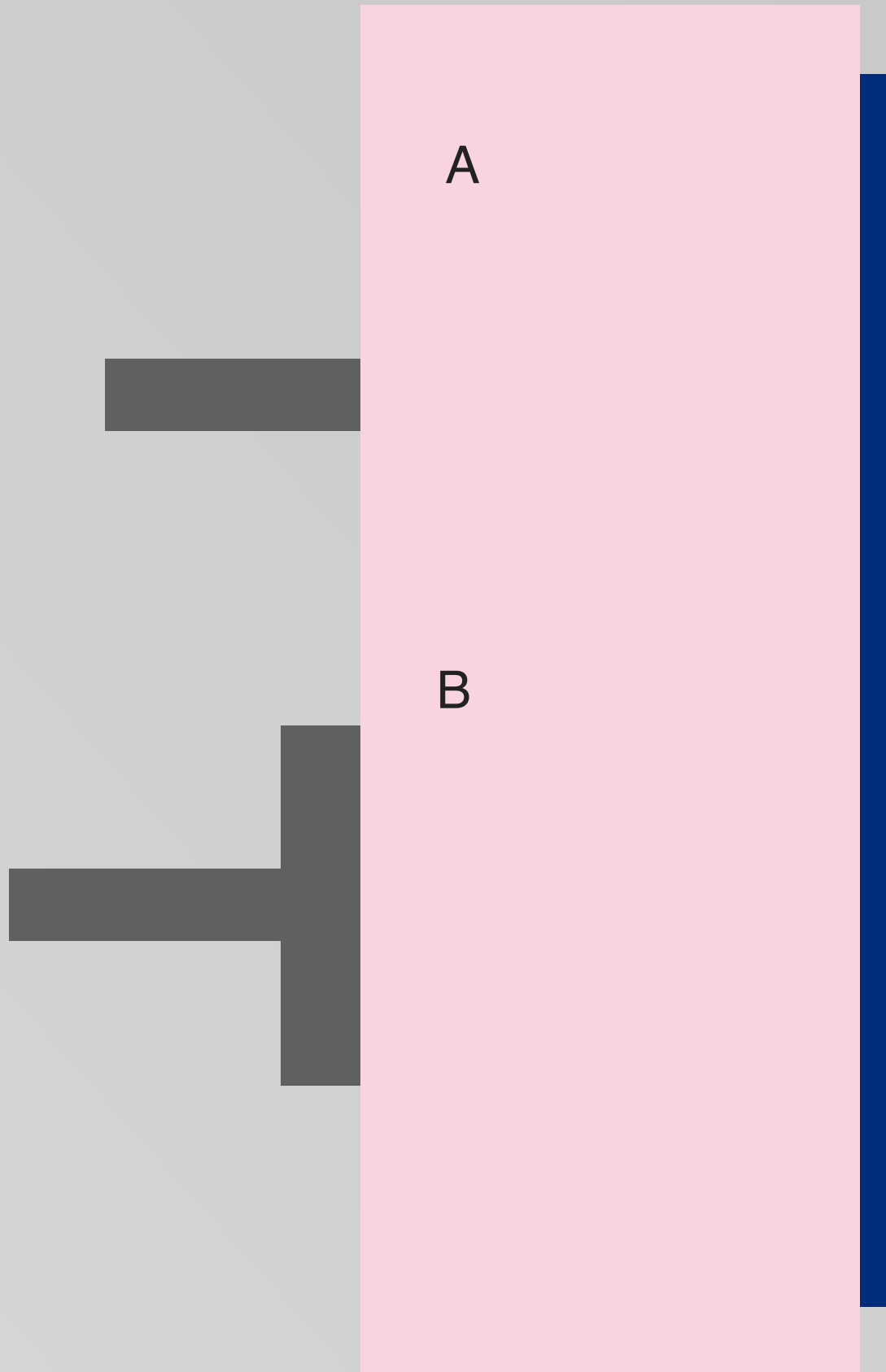


Pressure or no pressure





Pressure: we need to make a measurement in which we can change the volume



Pressure: we need to make a measurement in which we can change the volume

Experiment A: our piston is sufficiently small that we can the pore volume $\Rightarrow$ we can measure pressure in the pore

Experiment B: our piston is too large, we cannot change the volume $\Rightarrow$ we cannot measure the pressure in the pore

Summary

We discussed how to describe adsorption equilibria from a thermodynamic point of view