

Structural Analysis

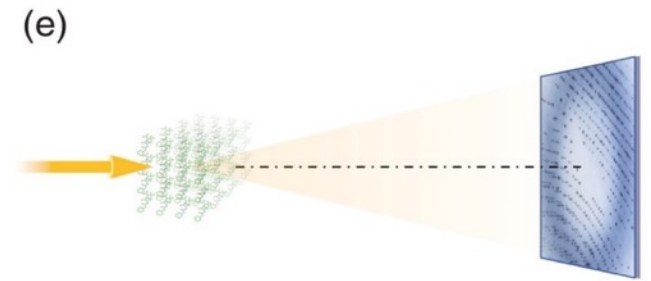
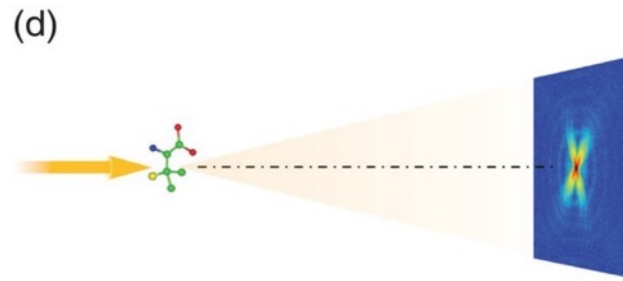
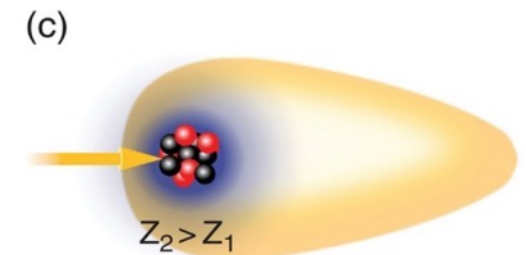
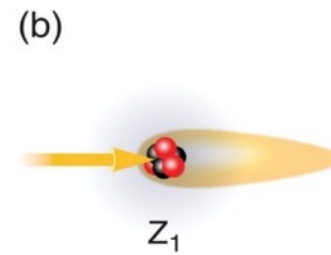
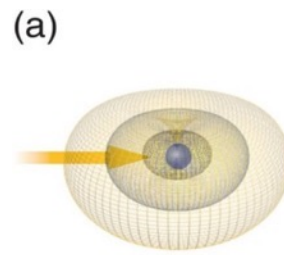
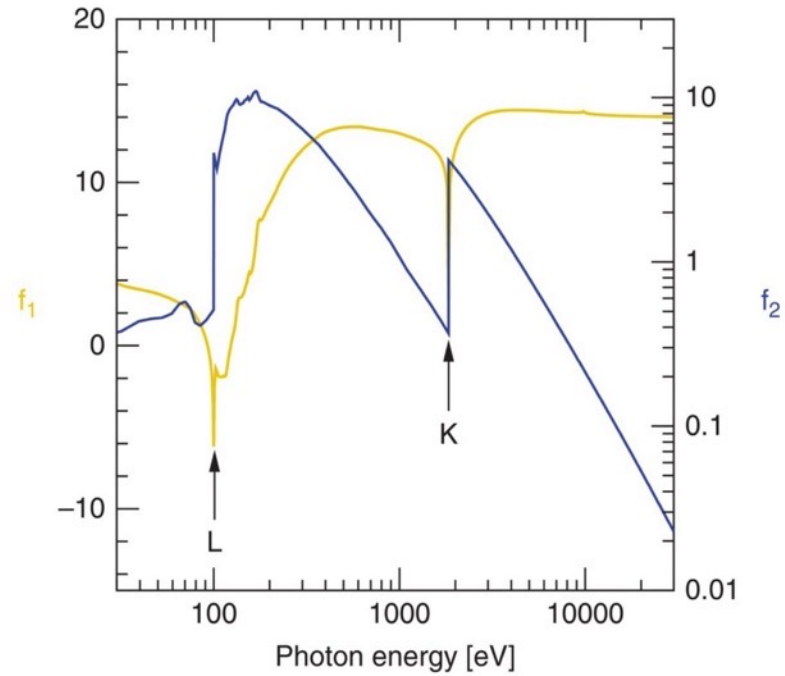
Part III - X-ray tools

Session 4:

X-ray diffraction applications
X-ray spectroscopy

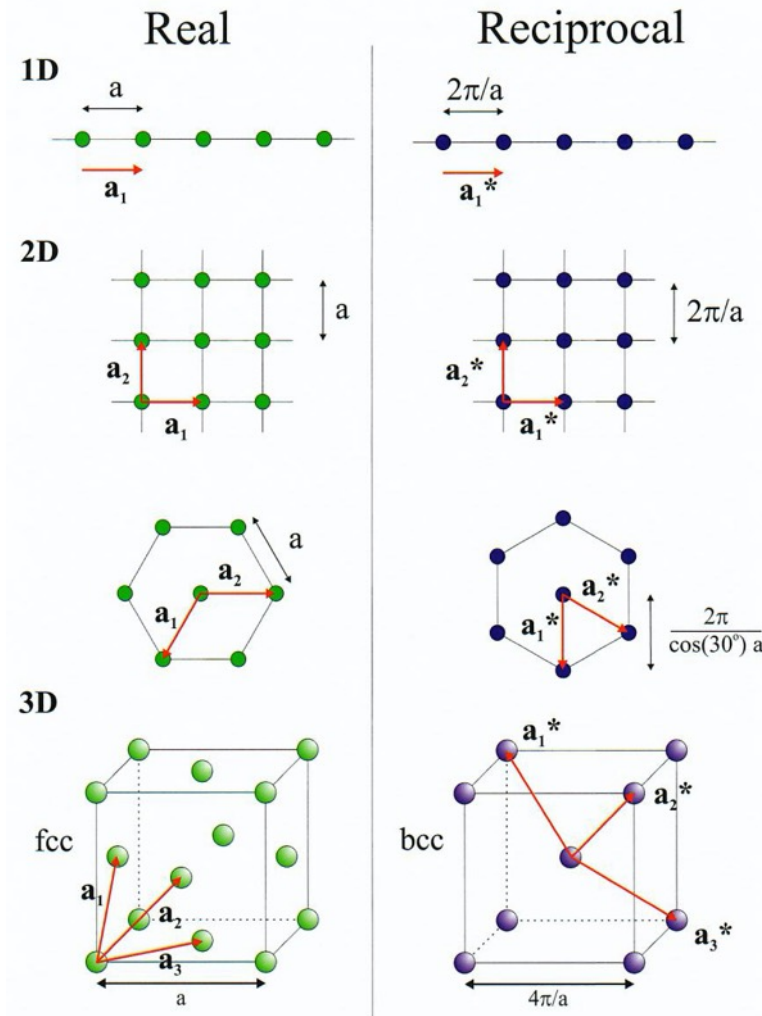
Reminder about previous weeks

Atomic scattering factors again



$$f(Q, h\nu) = \underbrace{f^0(Q)}_{\text{"scattering"}} + \underbrace{f'(h\nu)}_{\text{absorption}} + i f''(h\nu)$$

For each lattice a reciprocal lattice can be defined



→ For each lattice there exists a so called reciprocal lattice

→ The reciprocal lattice is the Fourier Transform of the direct lattice

→ Reciprocal lattice is defined by

$$\vec{G} = h\vec{a}_1^* + k\vec{a}_2^* + l\vec{a}_3^*$$

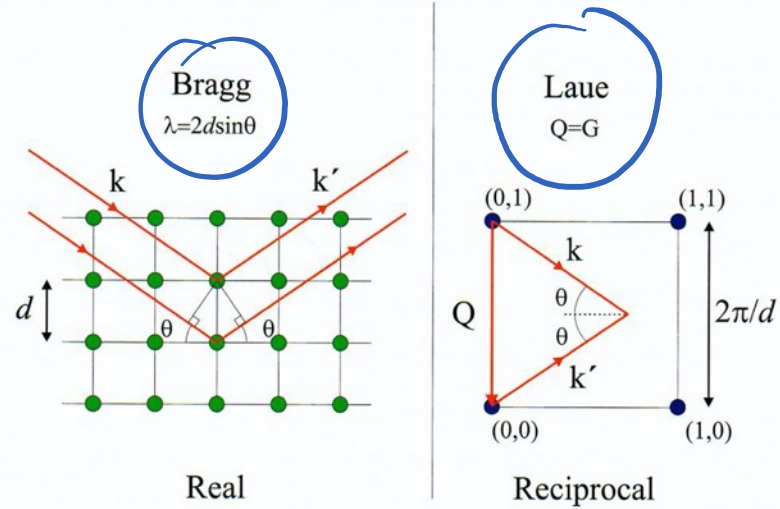
$$|\vec{G}| = \frac{2\pi}{d_{hkl}}$$

$\vec{G}$ perpendicular to planes
 $hkl \rightarrow$ Miller indices

Bragg and Laue conditions

Real

(a) Equivalence of Bragg and Laue



(b) Miller indices and reciprocal lattice vectors

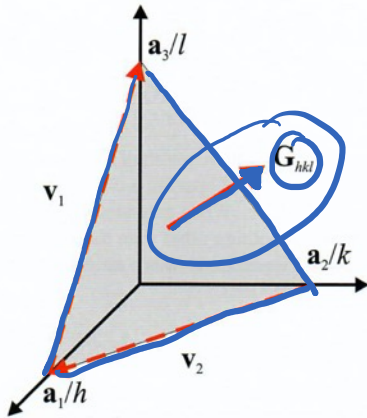


Photo from the Nobel Foundation archive.
Max von Laue
Prize share: 1/1

In reciprocal space
one can show that
constructive interference is obtained for

$$\vec{Q} = \vec{G}$$

$\vec{G} \rightarrow$ perpendicular to the planes
with Miller indices h, k, l

$$|\vec{G}| = \frac{2\pi}{d_{hkl}} \Rightarrow \text{Lattice spacing of } hkl \text{ planes}$$

The Ewald Sphere

• Elegant geometric construction of relationships

$$\vec{Q} = \vec{P} - \vec{P}' \rightarrow \text{wave vector } \vec{P}$$

$\rightarrow$ diffraction angle

$\rightarrow$ in reciprocal lattice

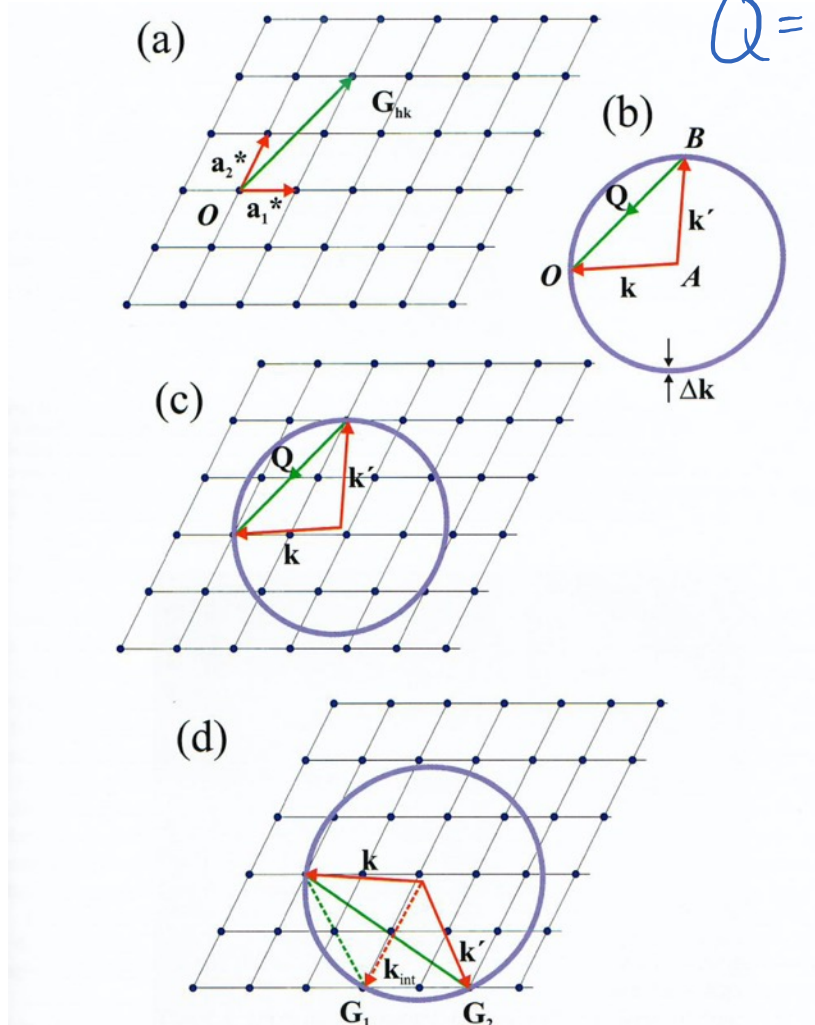
• Laue condition

$$\vec{Q} = \vec{G}_{hkl}$$

• Create sphere with radius λ (circle in 2D)

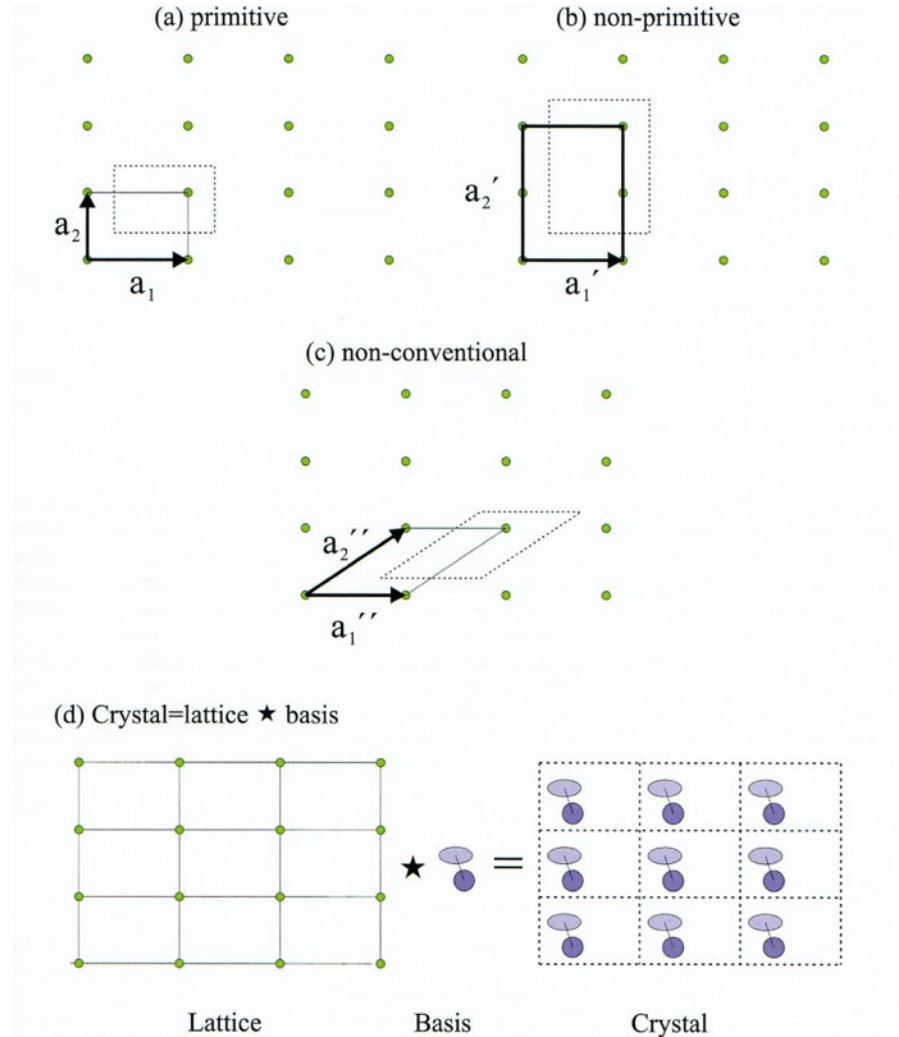
• Move sphere on origin O

• Non-chromatic light can be scattered constructively ("signal") whenever sphere overlaps with reciprocal lattice point as here $\vec{Q} = \vec{G}$

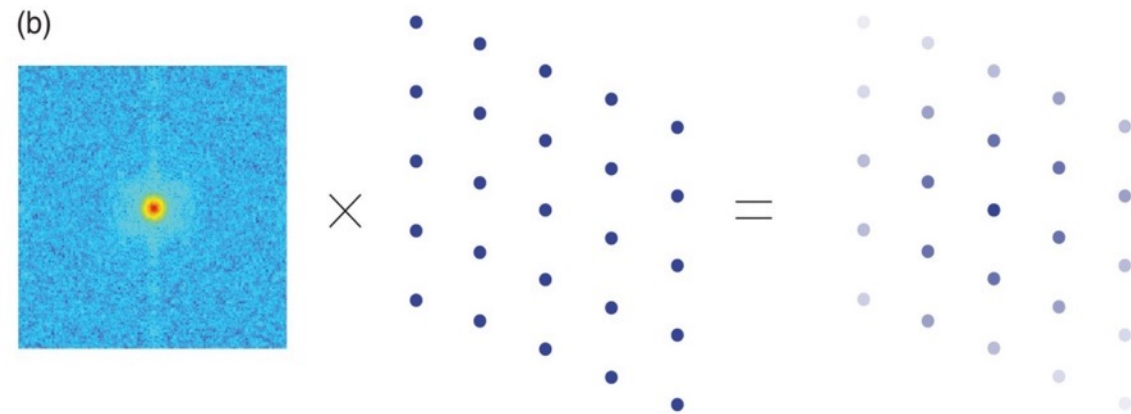
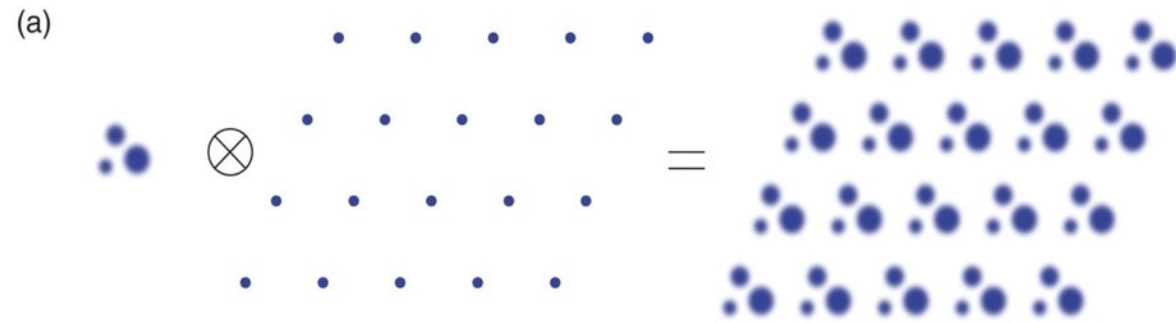


More on Bragg peaks

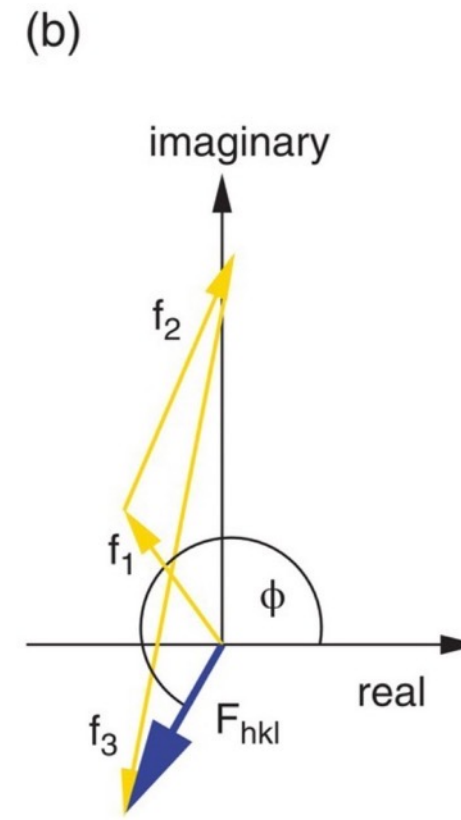
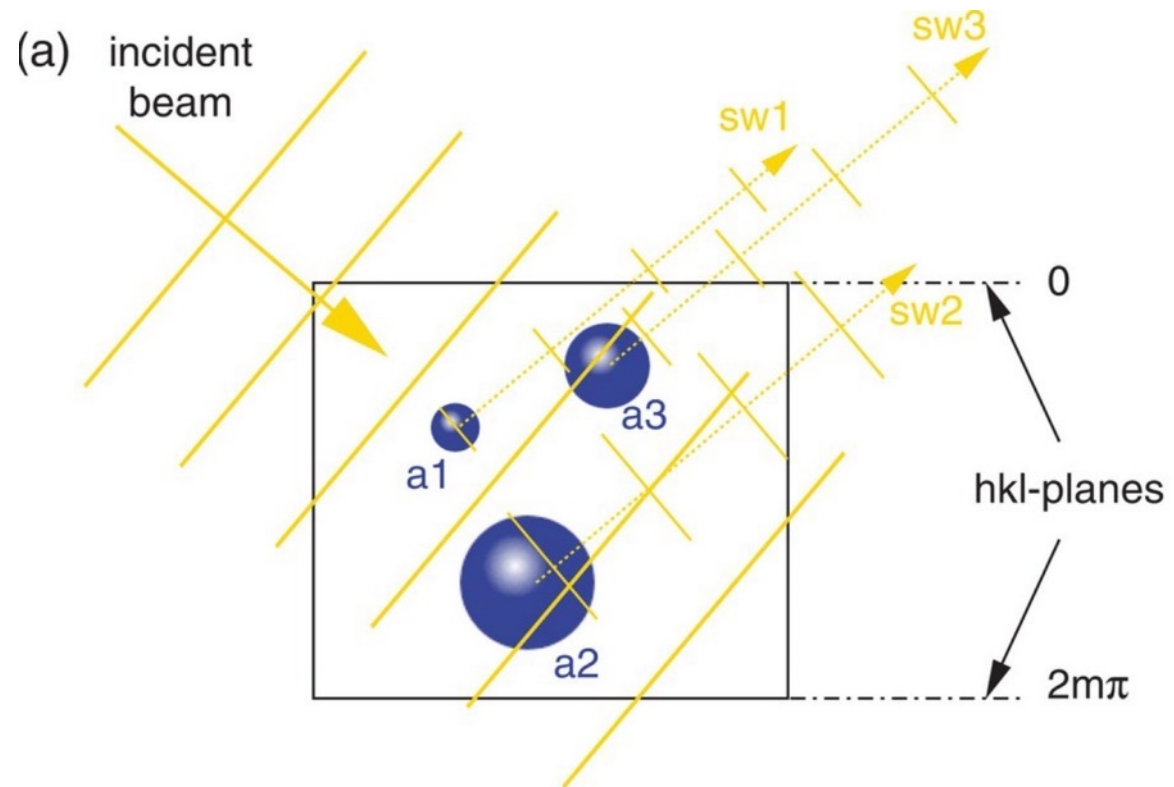
A crystal is defined by its lattice and basis



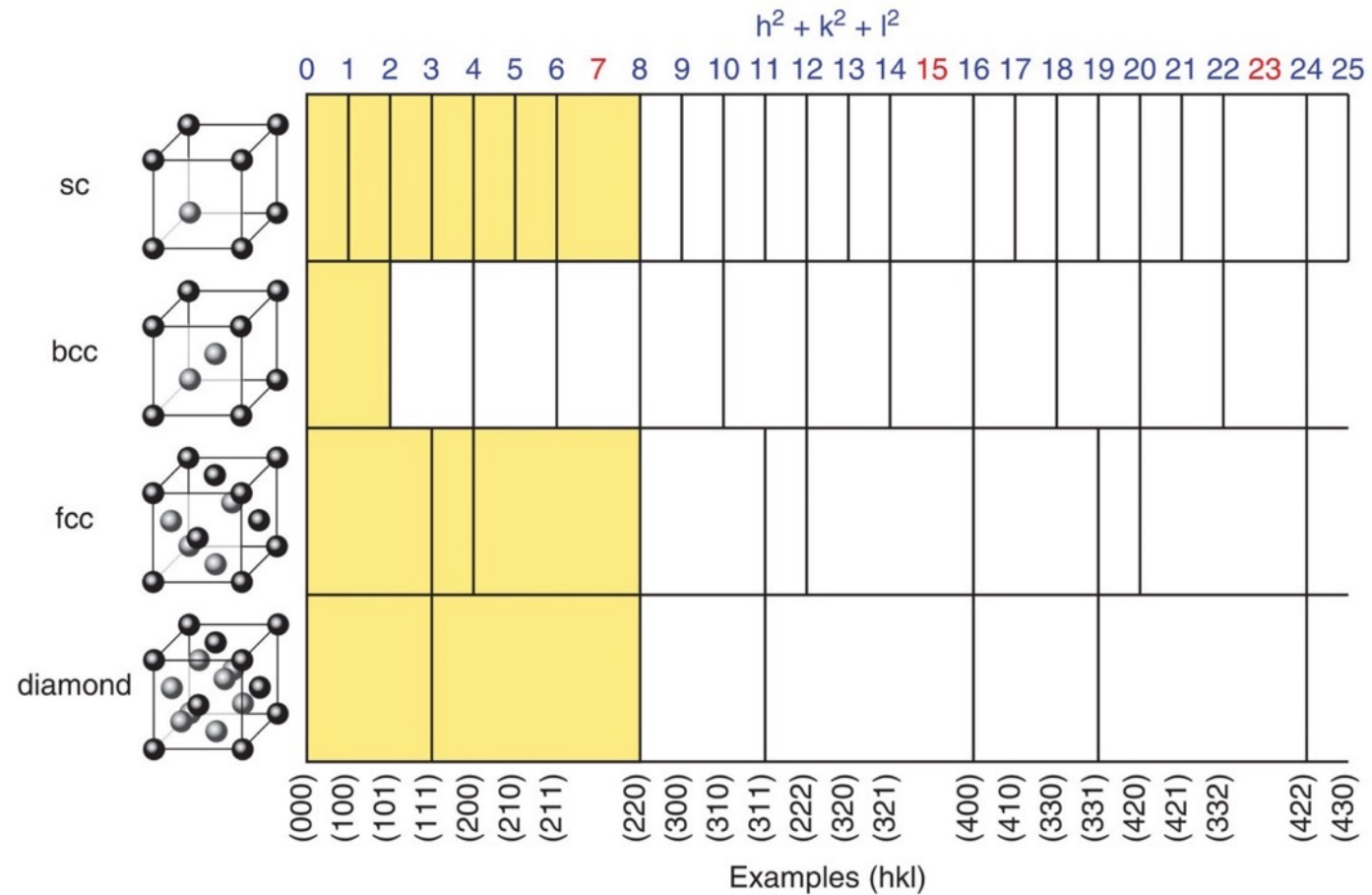
The structure factor



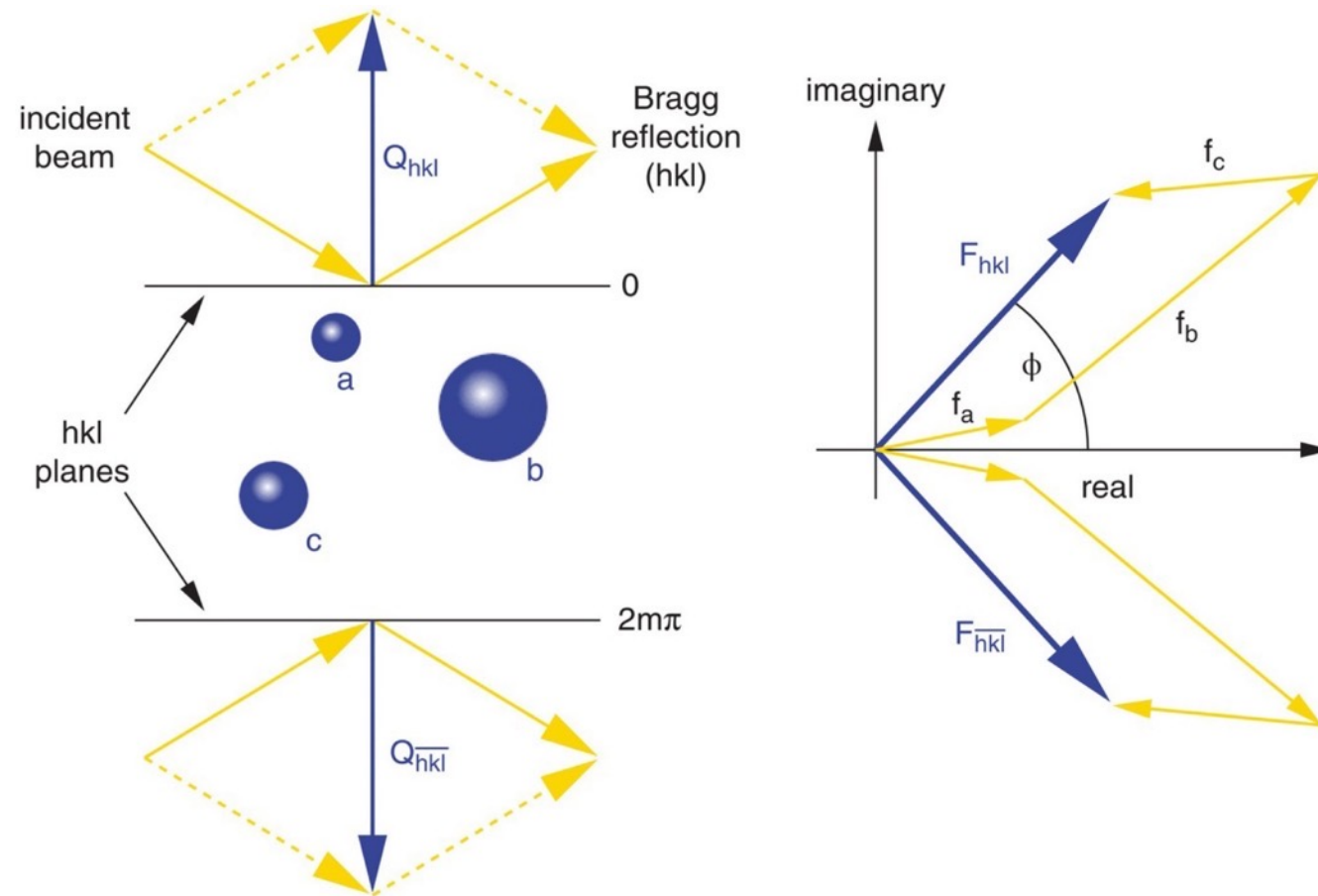
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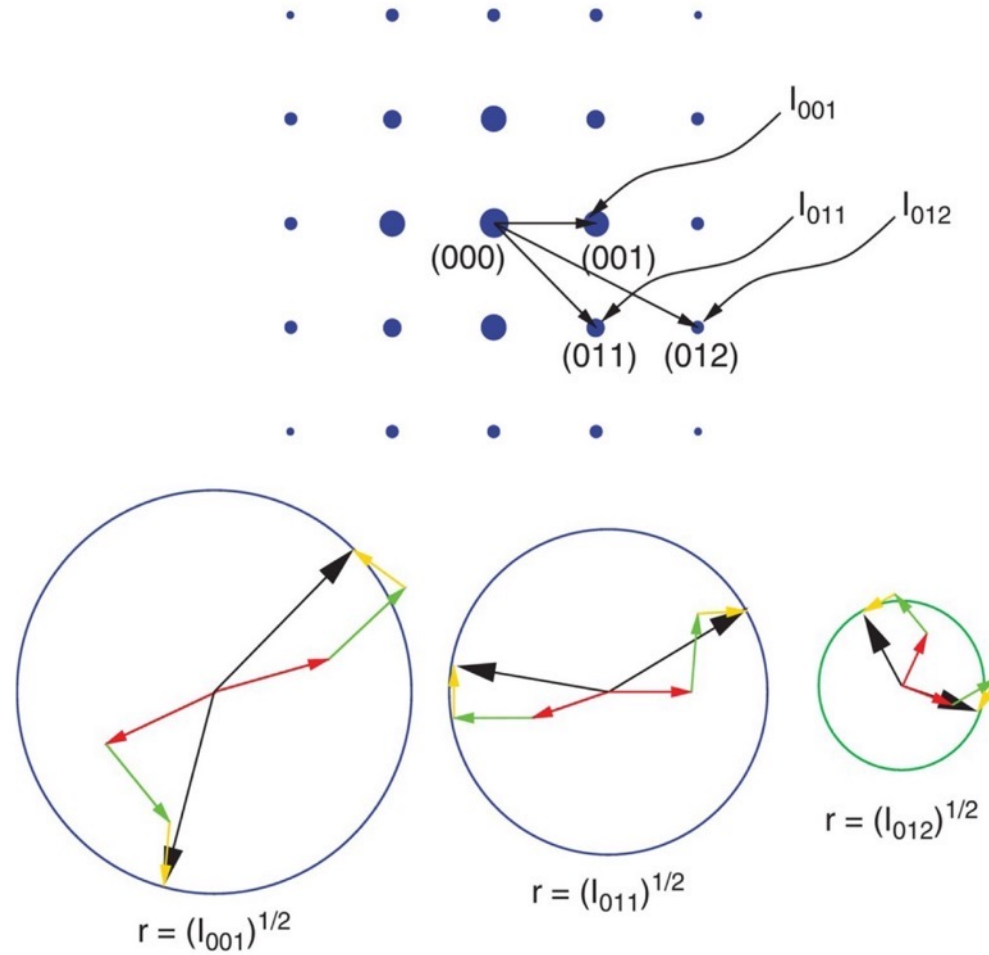
Allowed and forbidden reflections



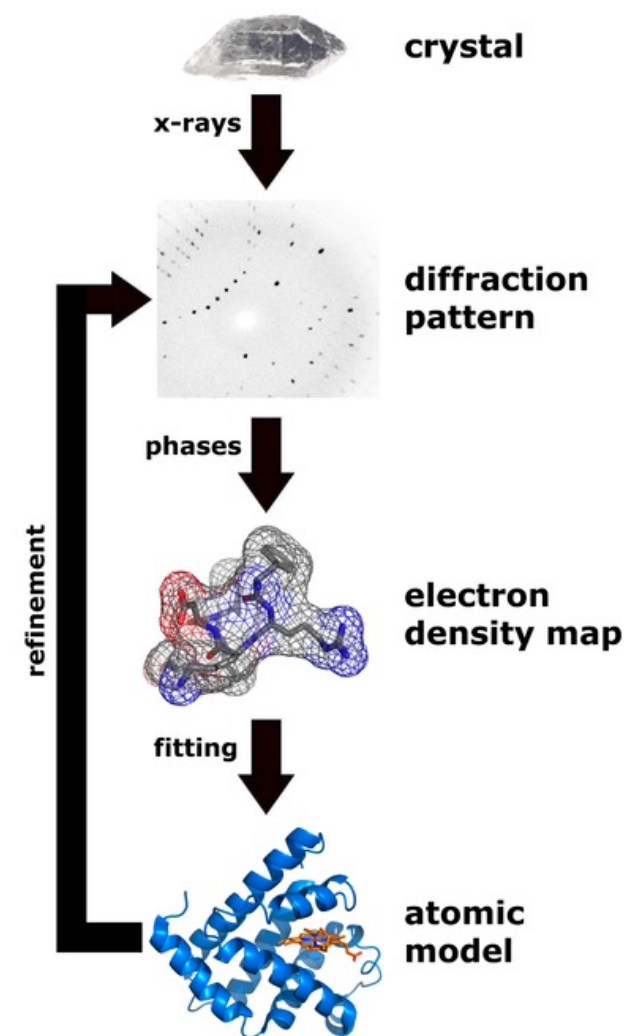
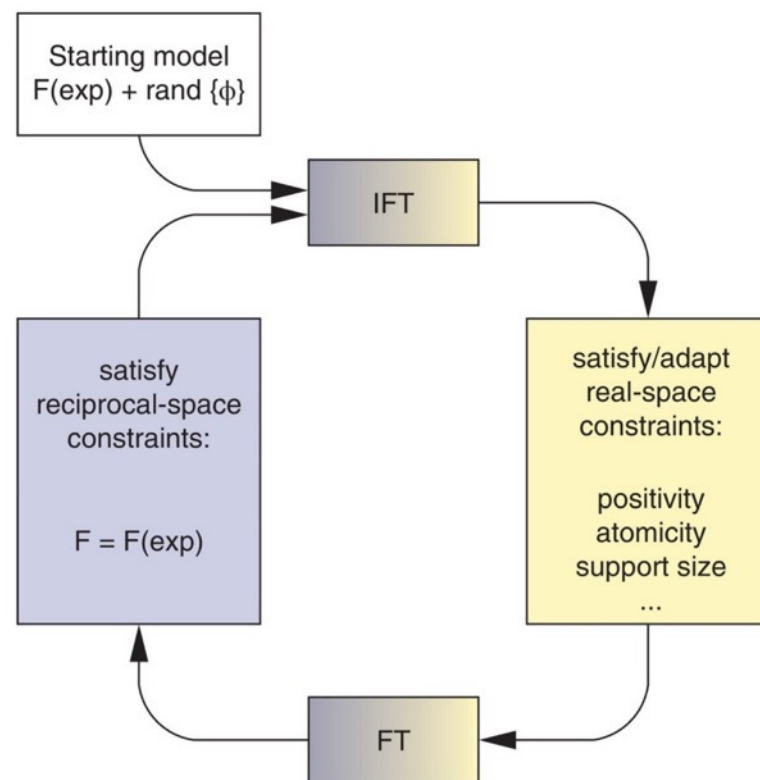
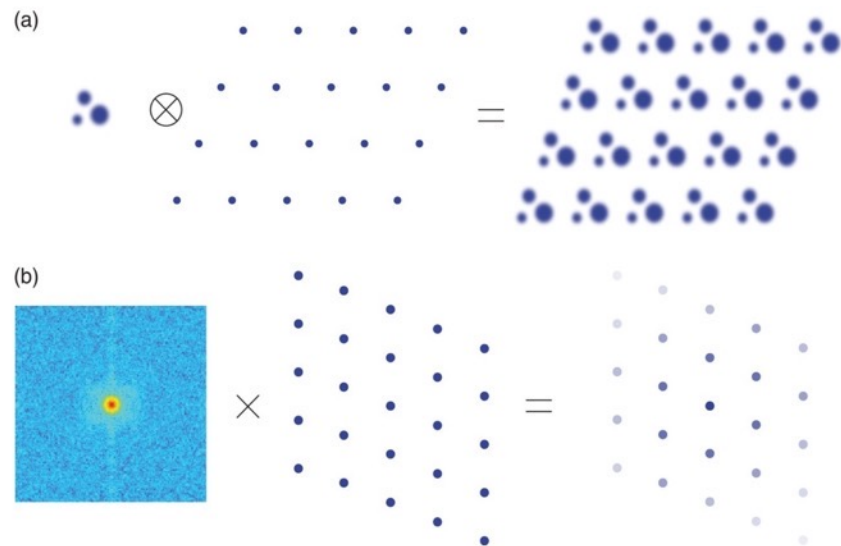
Friedel's law



The phase problem



Solving a crystal structure

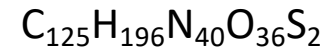


A few examples and case studies

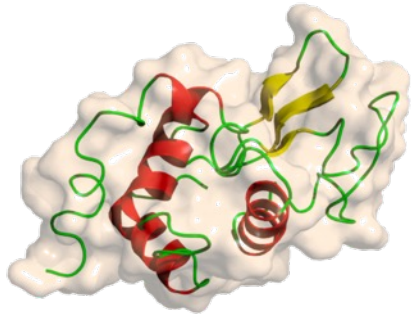
Remember last week example for diffraction of lysozyme crystal

Lysozym (Protein, Immunsystem)

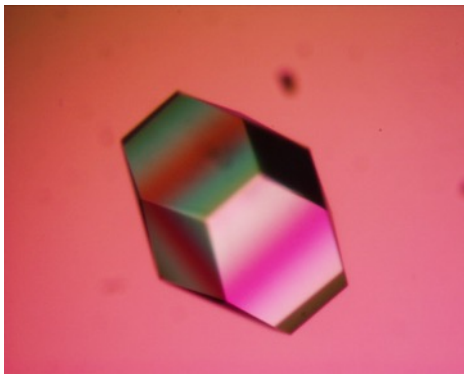
Stoichiometric formula



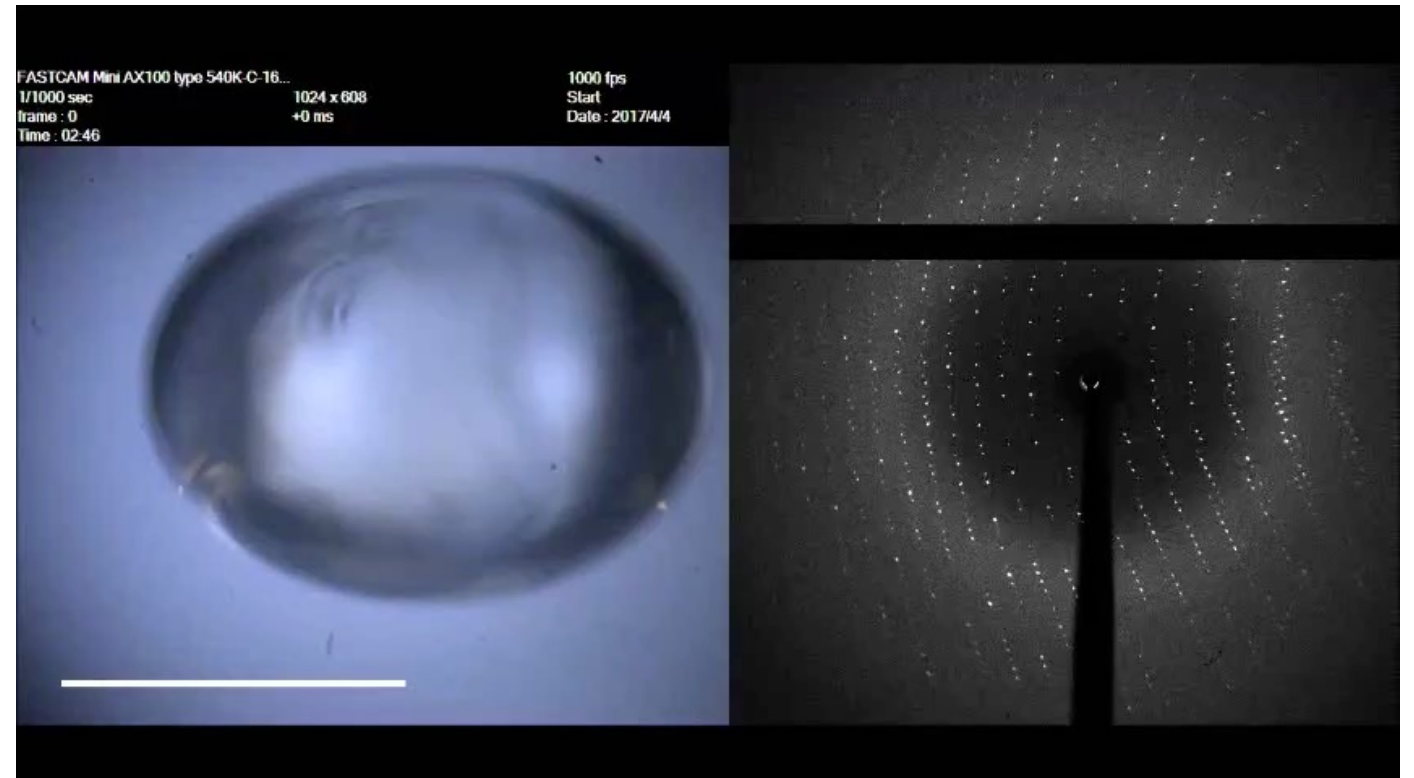
Structure



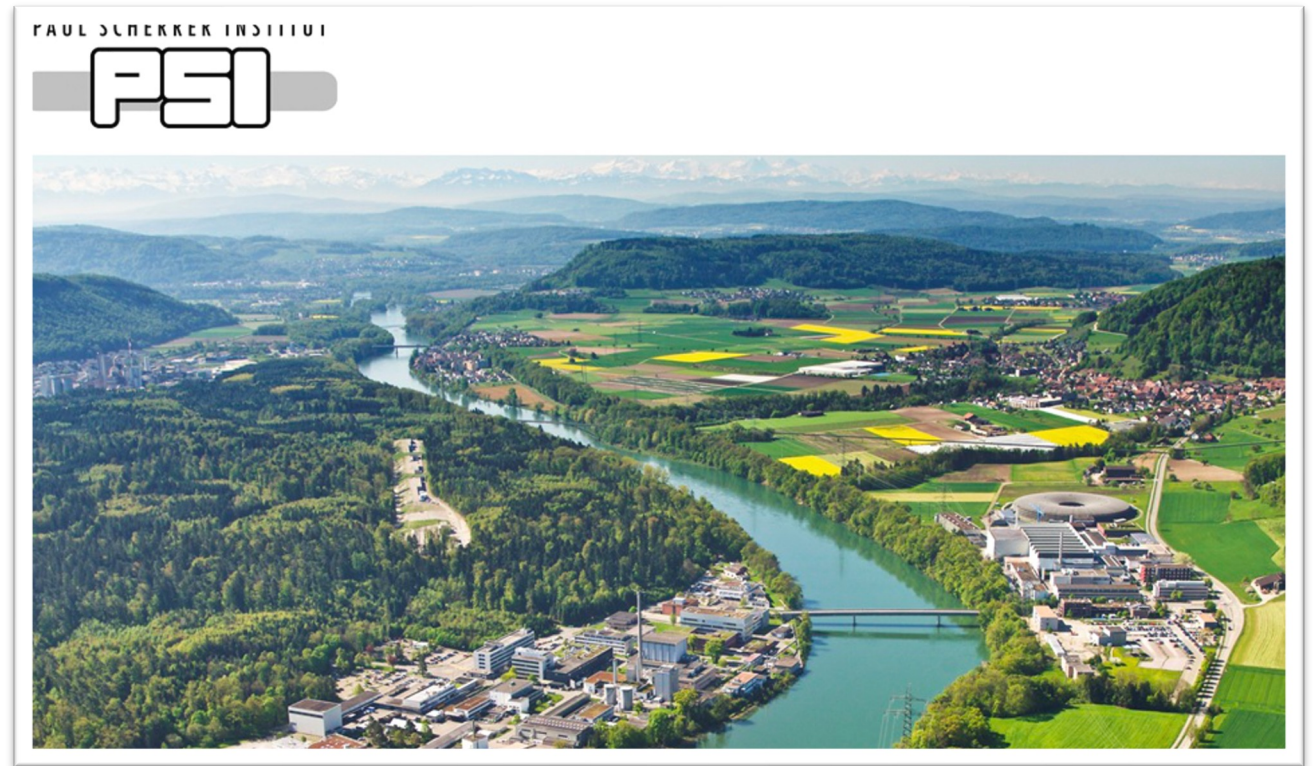
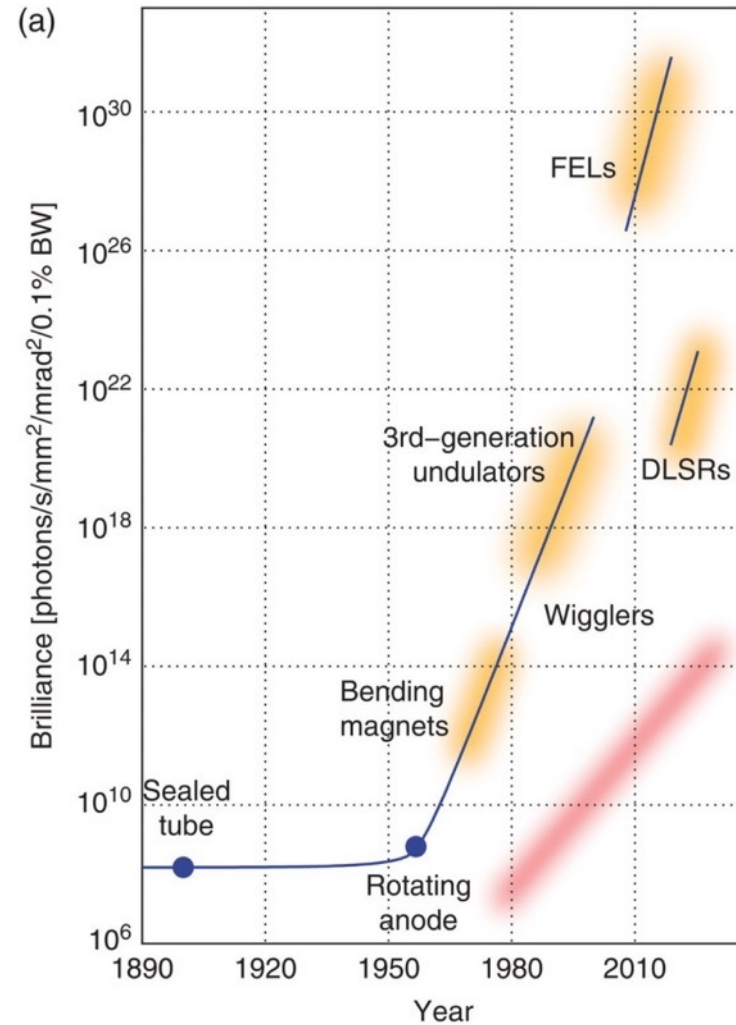
Crystal



Experiment at the Swiss Light Source

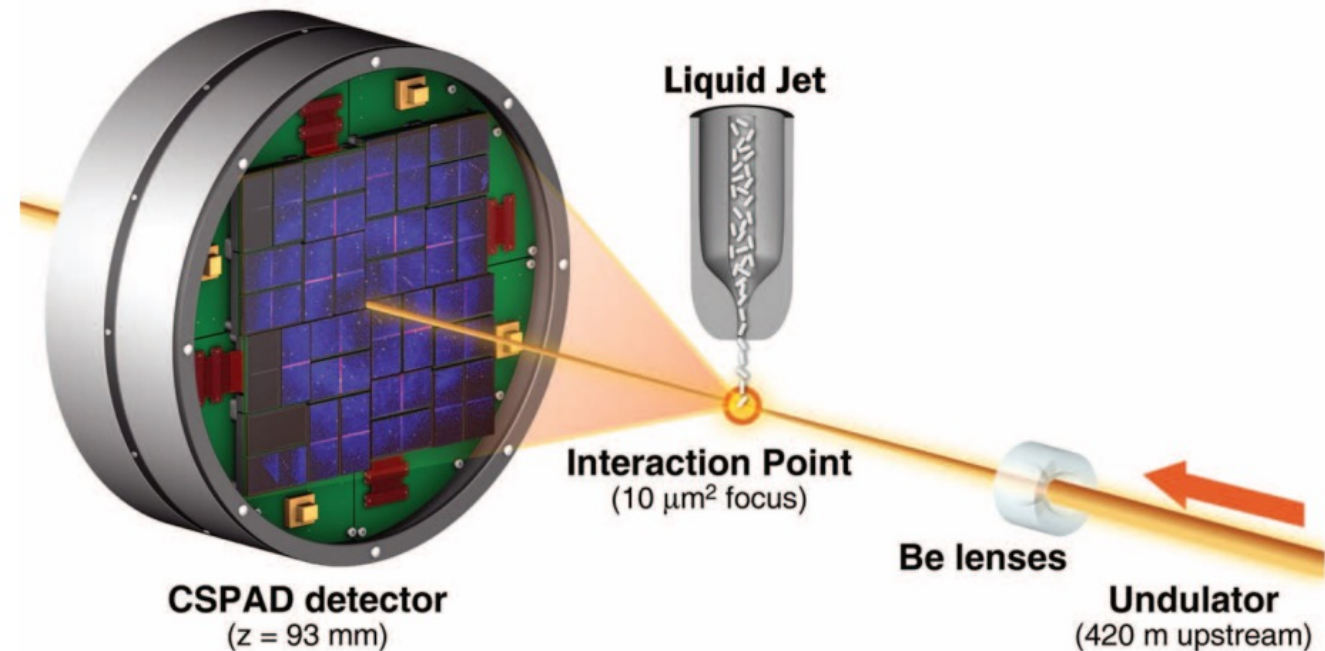


Each X-ray source allows characteristic experiments. „Output“ varies by >20 orders of magnitude

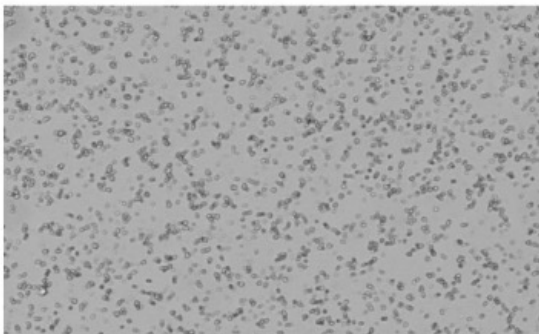


High-Resolution Protein Structure Determination by Serial Femtosecond Crystallography

Sébastien Boutet,^{1*} Lukas Lomb,^{2,3} Garth J. Williams,¹ Thomas R. M. Barends,^{2,3} Andrew Aquila,⁴ R. Bruce Doak,⁵ Uwe Weierstall,⁵ Daniel P. DePonte,⁴ Jan Steinbrener,^{2,3} Robert L. Shoeman,^{2,3} Marc Messerschmidt,¹ Anton Barty,⁴ Thomas A. White,⁴ Stephan Kassemeyer,^{2,3} Richard A. Kirian,⁵ M. Marvin Seibert,¹ Paul A. Montanez,¹ Chris Kenney,⁶ Ryan Herbst,⁶ Philip Hart,⁶ Jack Pines,⁶ Gunther Haller,⁶ Sol M. Gruner,^{7,8} Hugh T. Philipp,⁷ Mark W. Tate,⁷ Marianne Hromalik,⁹ Lucas J. Koerner,¹⁰ Niels van Bakel,¹¹ John Morse,¹² Wilfred Ghonsalves,¹ David Arnlund,¹³ Michael J. Bogan,¹⁴ Carl Caleman,⁴ Raimund Fromme,¹⁵ Christina Y. Hampton,¹⁴ Mark S. Hunter,¹⁵ Linda C. Johansson,¹³ Gergely Katona,¹³ Christopher Kupitz,¹⁵ Mengning Liang,⁴ Andrew V. Martin,⁴ Karol Nass,¹⁶ Lars Redecke,^{17,18} Francesco Stellato,⁴ Nicusor Timneanu,¹⁹ Dingjie Wang,⁵ Nadia A. Zatsepin,⁵ Donald Schafer,¹ James Deфеver,¹ Richard Neutze,¹³ Petra Fromme,¹⁵ John C. H. Spence,⁵ Henry N. Chapman,^{4,16} Ilme Schlichting^{2,3}



B



C



Time-resolved x-ray diffraction

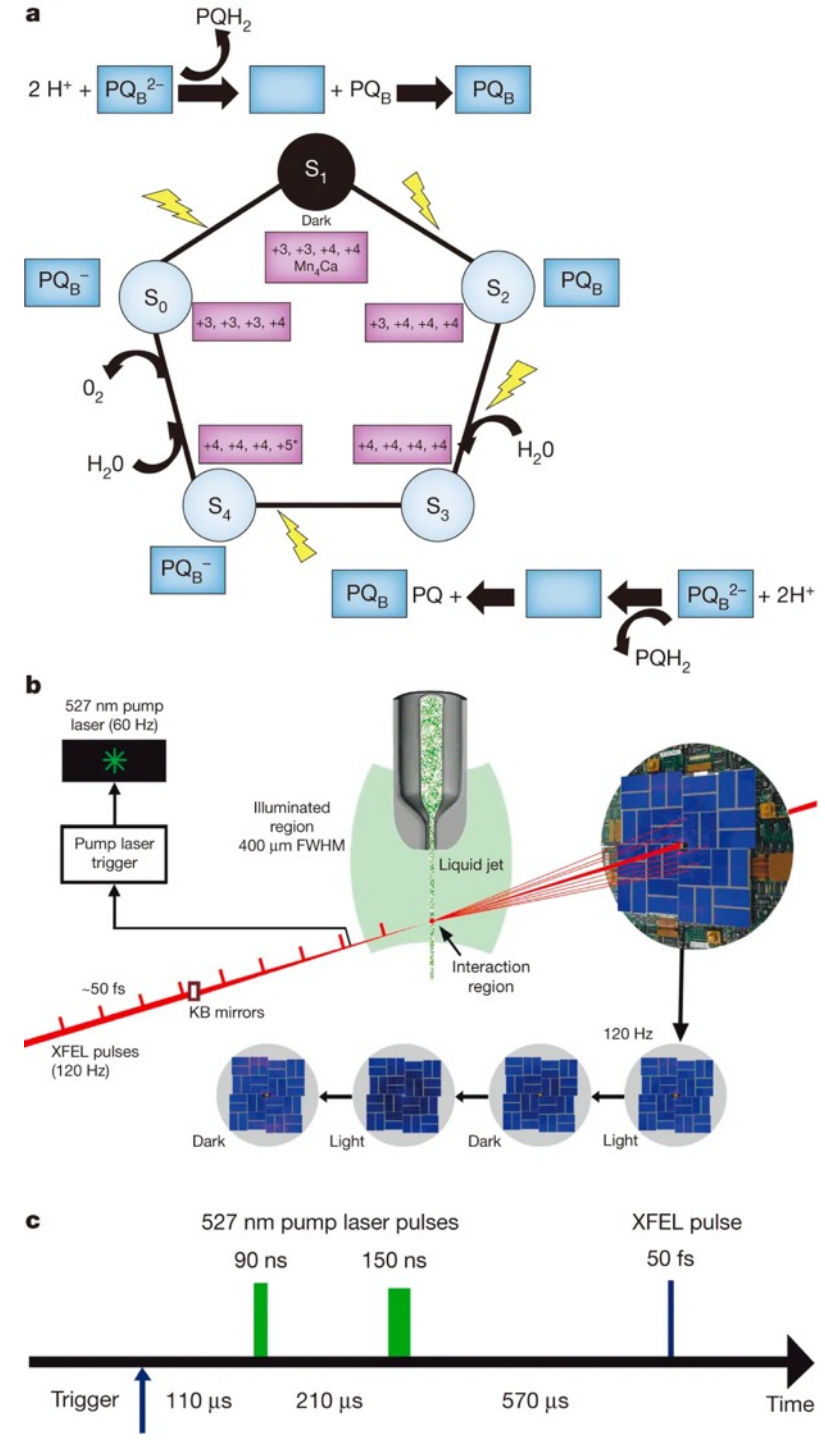
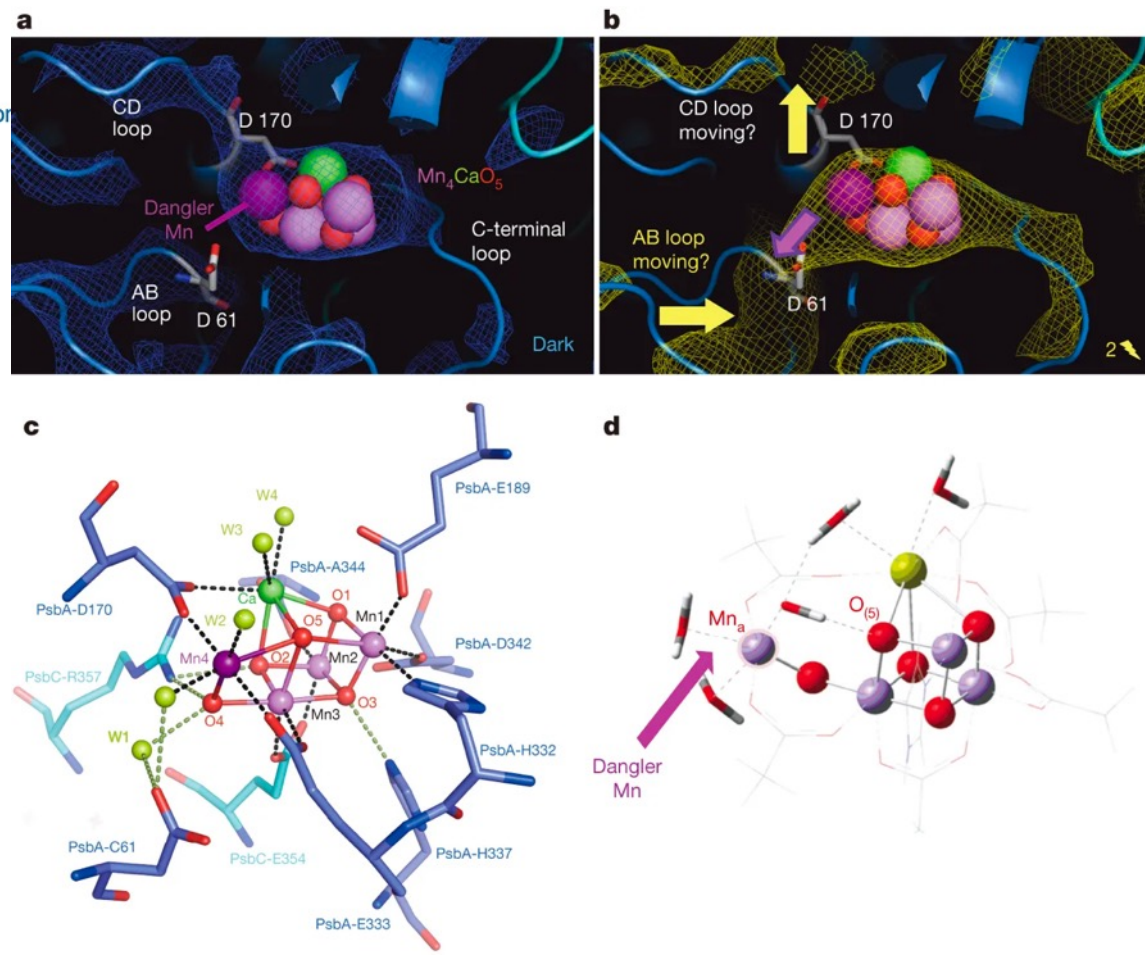
nature

Letter | Published: 09 July 2014

Serial time-resolved crystallography of photosystem II using a femtosecond X-ray laser

Christopher Kupitz, Shibom Basu, [...] Petra Fromme

Nature 513, 261–265(2014) | Cite this article



Recent results from SwissFEL

Article

Femtosecond-to-millisecond structural changes in a light-driven sodium pump

<https://doi.org/10.1038/s41586-020-2307-8>

Received: 29 November 2019

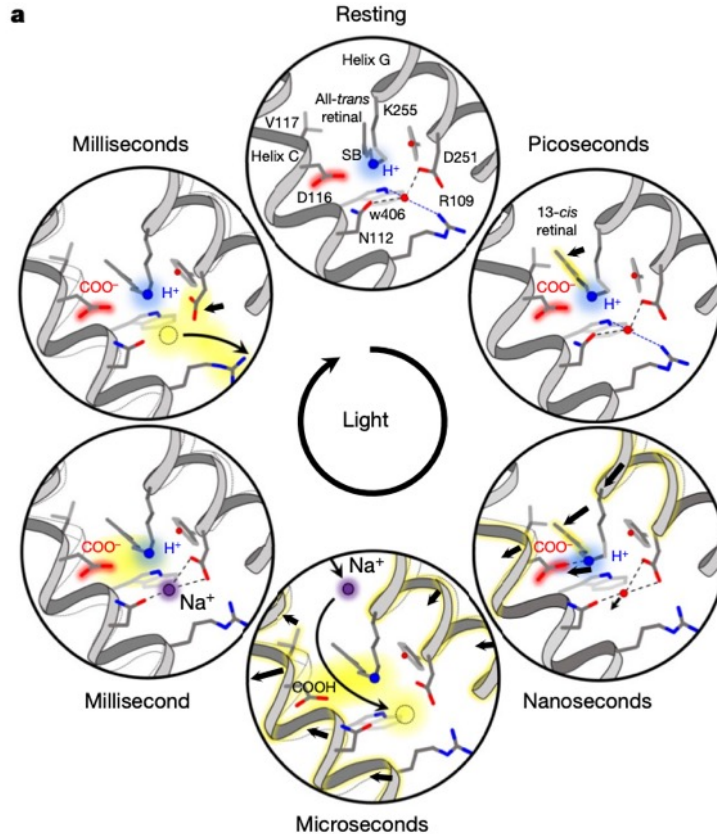
Accepted: 16 April 2020

Published online: 20 May 2020

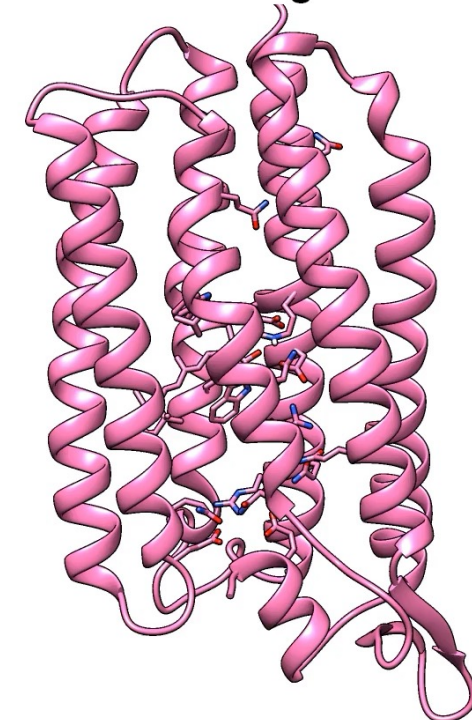
Check for updates

Petr Skopintsev¹, David Ehrenberg^{2,3}, Tobias Weinert^{1,3}, Daniel James¹, Rajiv K. Kar³, Philip J. M. Johnson⁴, Dmitry Ozerov⁵, Antonia Furrer¹, Isabelle Martiel⁶, Florian Dworkowski⁶, Karol Nass^{6,7}, Gregor Knopp⁷, Claudio Cirelli⁷, Christopher Arrell⁸, Dardan Gashi^{1,7}, Sandra Mous⁹, Maximilian Wranik¹, Thomas Gruhl¹, Demet Kekilli⁷, Steffen Brünle¹, Xavier Deupi^{1,10}, Gebhard F. X. Schertler^{1,11}, Roger M. Benoit^{1,12}, Valerie Panneels¹, Przemysław Nogly⁹, Igor Schapiro³, Christopher Milne⁷, Joachim Heberle² & Jörg Standfuss^{1,13}

Light-driven sodium pumps actively transport small cations across cellular membranes¹. These pumps are used by microorganisms to convert light into membrane potential and have become useful optogenetic tools with applications in neuroscience. Although the resting state structures of the prototypical sodium pump *Krokinobacter eikastus* rhodopsin 2 (KR2) have been solved^{2,3}, it is unclear how structural alterations over time allow sodium to be translocated against a concentration gradient. Here, using the Swiss X-ray Free Electron Laser⁴, we have collected serial crystallographic data at ten pump–probe delays from femtoseconds to milliseconds. High-resolution structural snapshots throughout the KR2 photocycle show how retinal isomerization is completed on the femtosecond timescale and changes the local structure of the binding pocket in the early nanoseconds. Subsequent rearrangements and deprotonation of the retinal Schiff base open an electrostatic gate in microseconds. Structural and spectroscopic data, in combination with quantum chemical calculations, indicate that a sodium ion binds transiently close to the retinal within one millisecond. In the last structural intermediate, at 20 milliseconds after activation, we identified a potential second sodium-binding site close to the extracellular exit. These results provide direct molecular insight into the dynamics of active cation transport across biological membranes.



KR2 resting state



Some notes on X-ray Spectroscopy

Remember: interaction of x-rays with matter

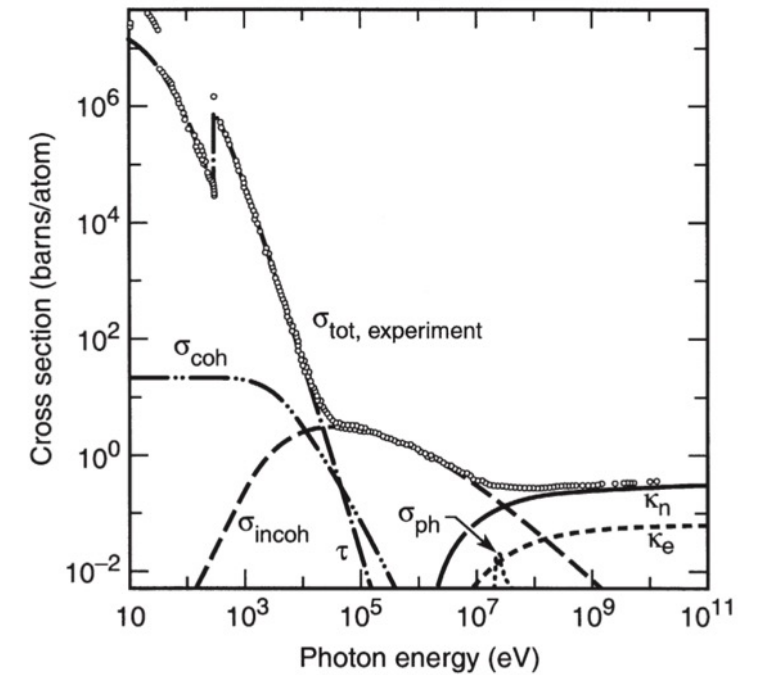
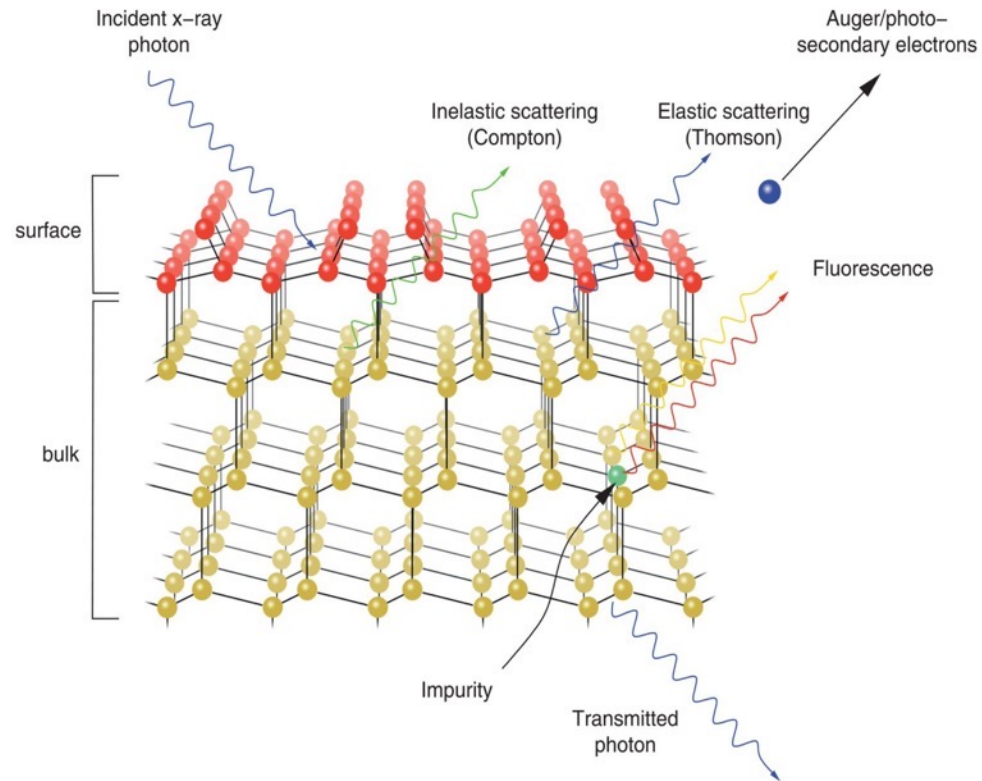
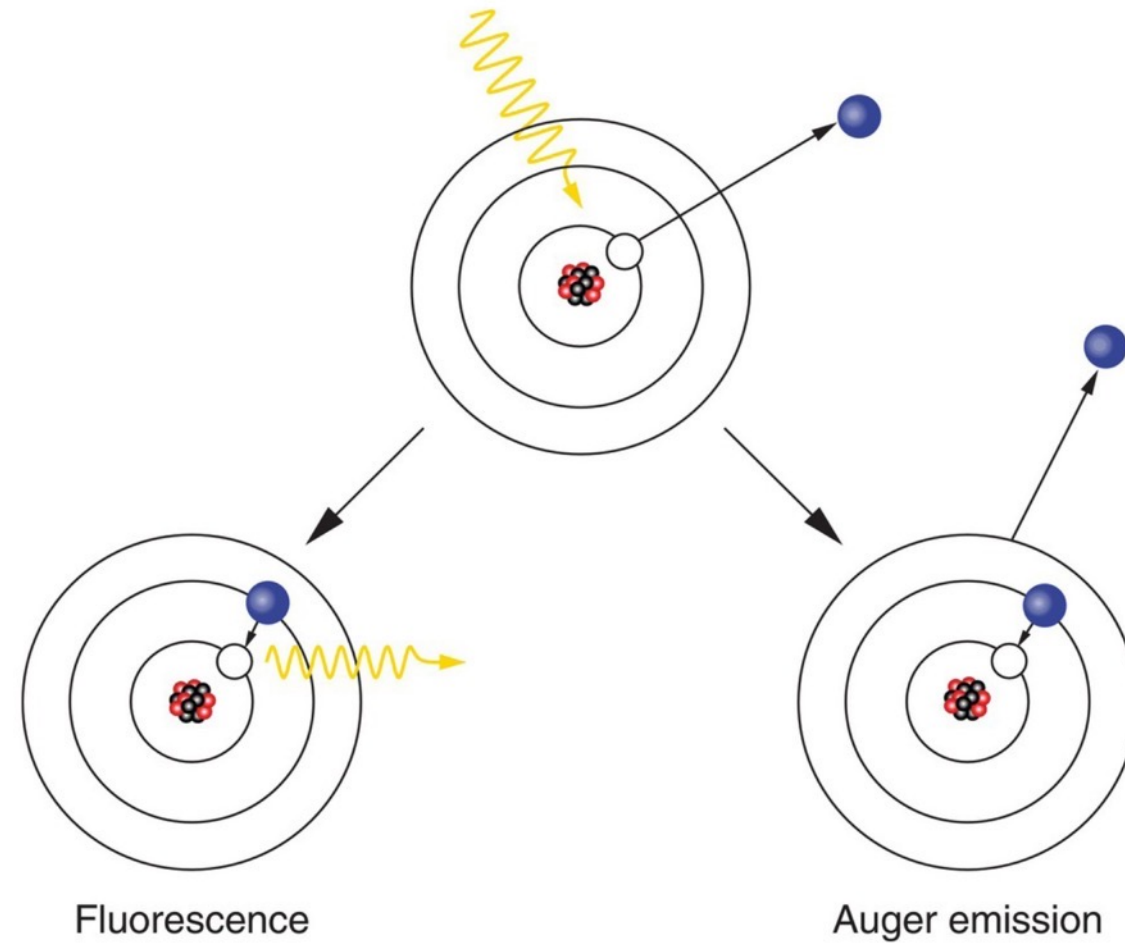
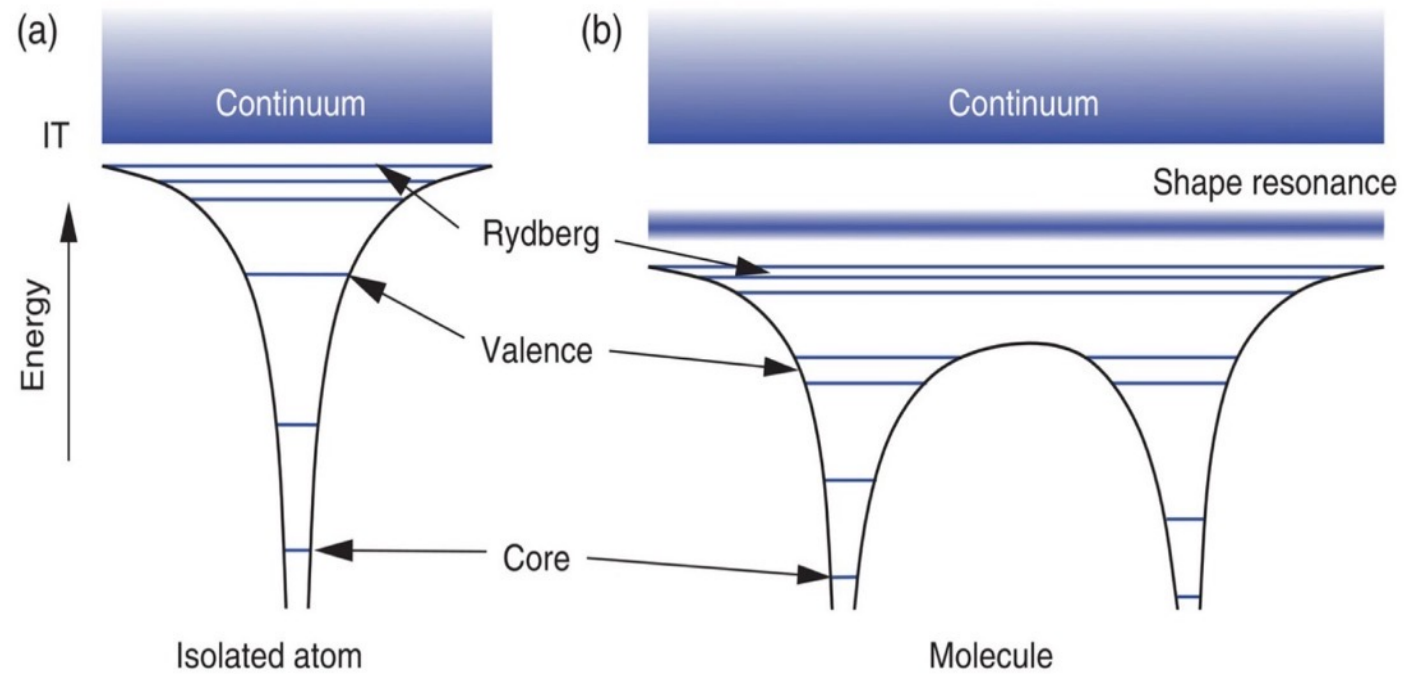


Fig. 3-1. Total photon cross section σ_{tot} in carbon, as a

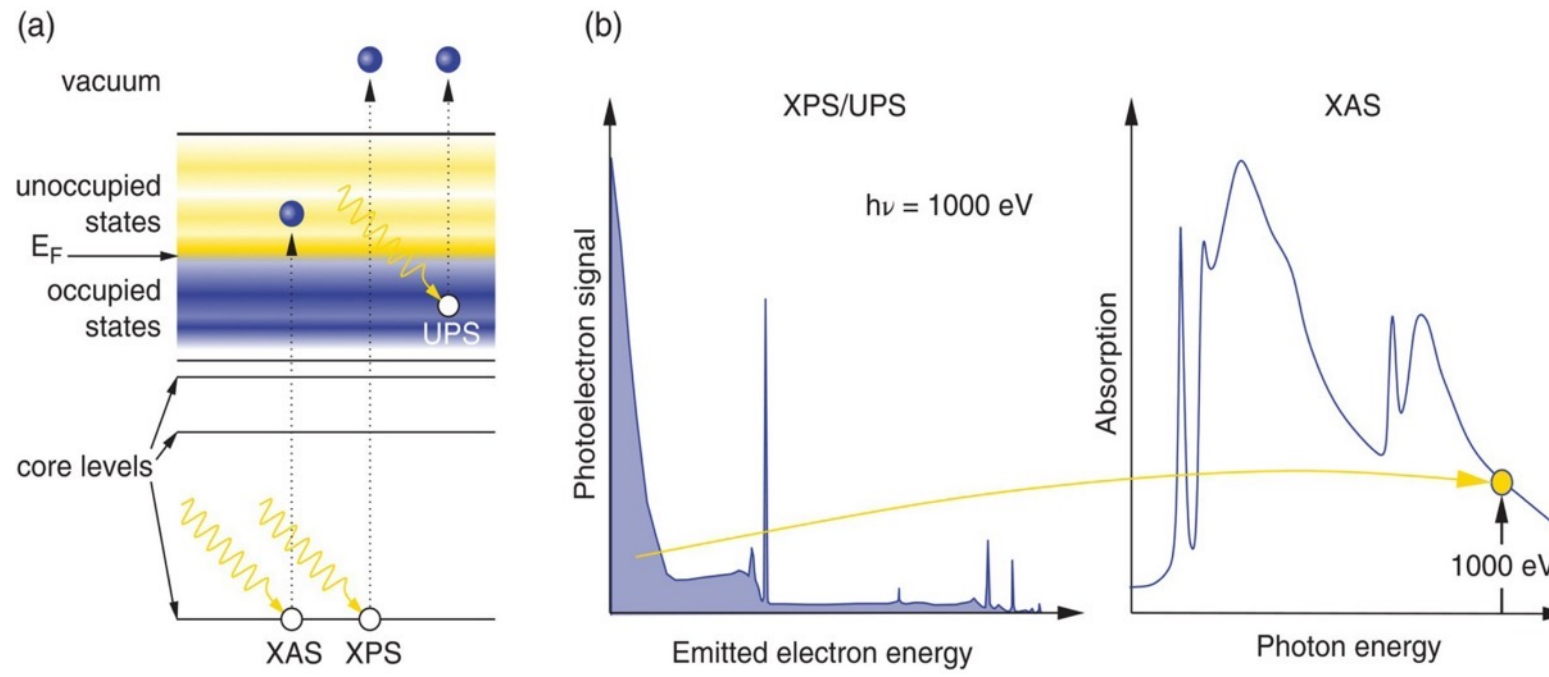
Photoionization / absorption



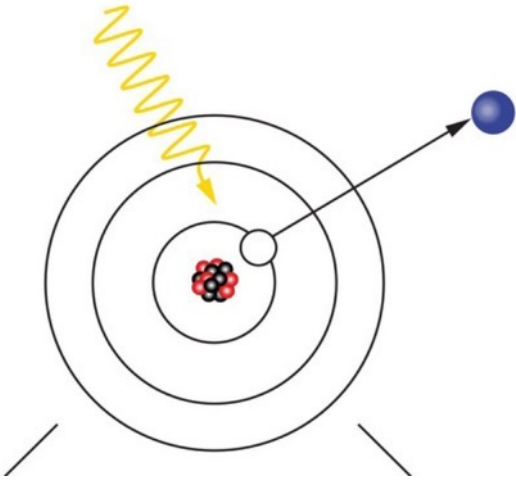
Atoms vs molecules



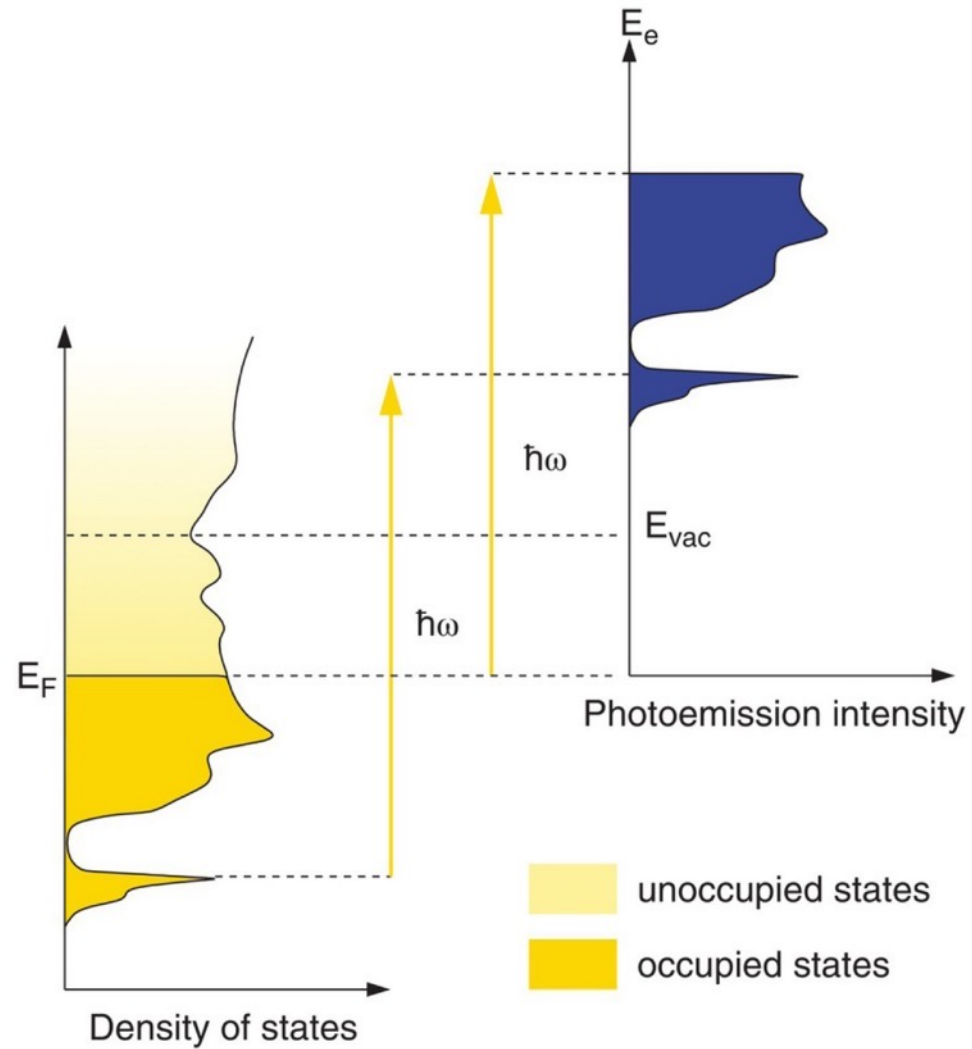
Absorption vs Photoemission



Photoemission:



Photoelectrons reflect occupied density of states



Ionization energies of elements

Table 1-1. Electron binding energies, in electron volts, for the elements in their natural forms.

Element	K 1s	L ₁ 2s	L ₂ 2p _{1/2}	L ₃ 2p _{3/2}	M ₁ 3s	M ₂ 3p _{1/2}	M ₃ 3p _{3/2}	M ₄ 3d _{3/2}	M ₅ 3d _{5/2}	N ₁ 4s	N ₂ 4p _{1/2}
1 H	13.6										
2 He	24.6*										
3 Li	54.7*										
4 Be	111.5*										
5 B	188*										
6 C	284.2*										
7 N	409.9*	37.3*									
8 O	543.1*	41.6*									
9 F	696.7*										
10 Ne	870.2*	48.5*	21.7*	21.6*							
11 Na	1070.8†	63.5†	30.65	30.81							
12 Mg	1303.0†	88.7	49.78	49.50							
13 Al	1559.6	117.8	72.95	72.55							
14 Si	1839	149.7*b	99.82	99.42							
15 P	2145.5	189*	136*	135*							
16 S	2472	230.9	163.6*	162.5*							
17 Cl	2822.4	270*	202*	200*							
18 Ar	3205.9*	326.3*	250.6†	248.4*	29.3*	15.9*	15.7*				
19 K	3608.4*	378.6*	297.3*	294.6*	34.8*	18.3*	18.3*				
20 Ca	4038.5*	438.4†	349.7†	346.2†	44.3 †	25.4†	25.4†				
21 Sc	4492	498.0*	403.6*	398.7*	51.1*	28.3*	28.3*				
22 Ti	4966	560.9†	460.2†	453.8†	58.7†	32.6†	32.6†				

Chemical shifts

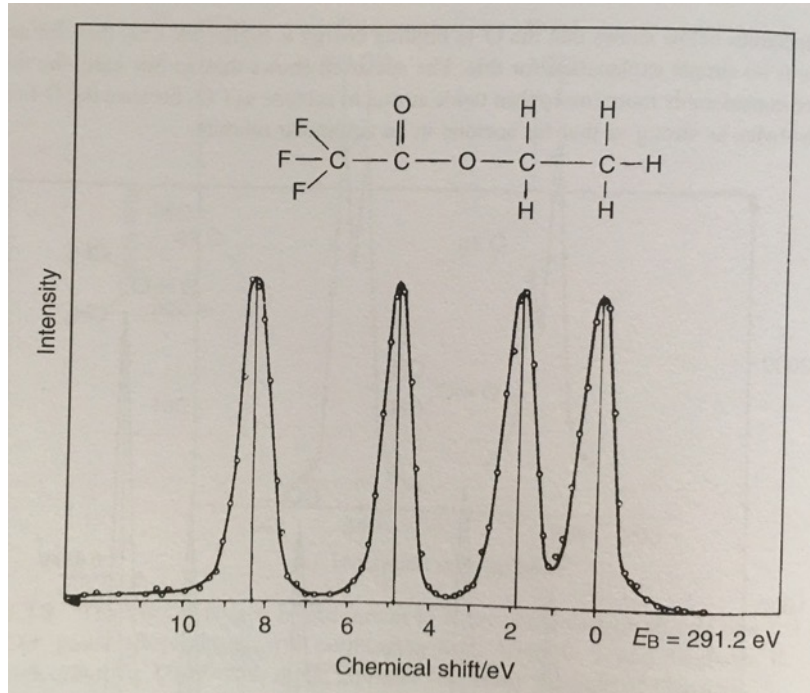
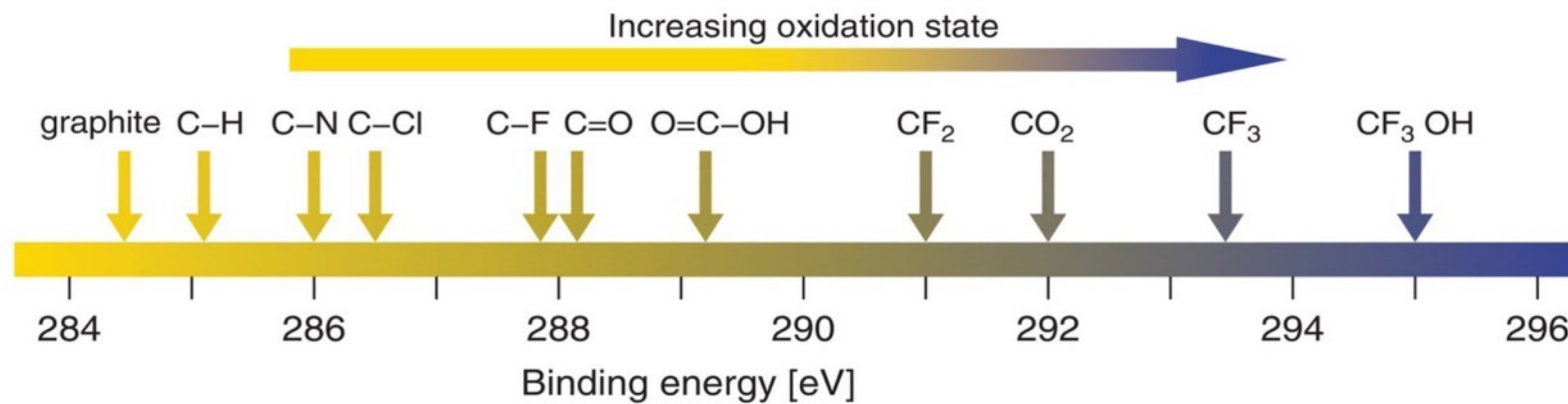


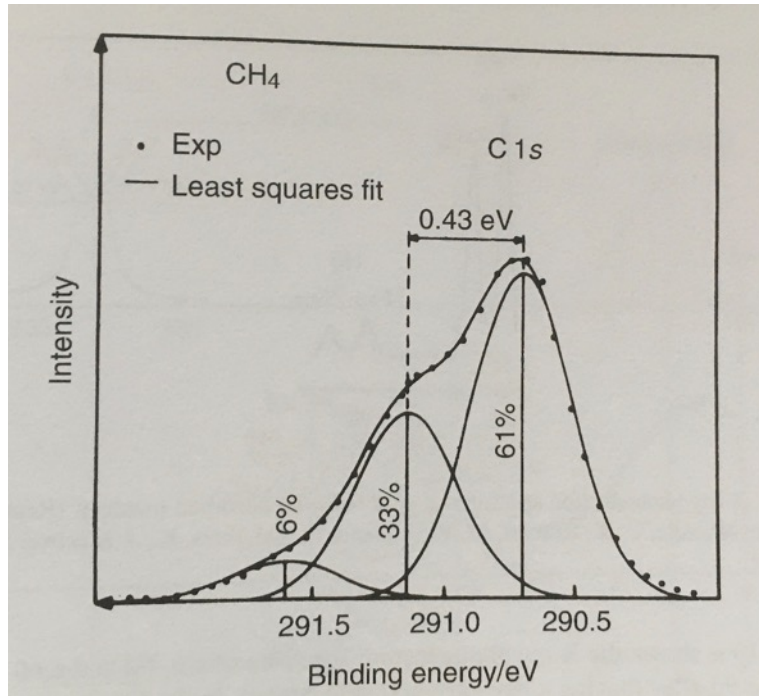
Photo from the Nobel Foundation archive.

Kai M. Siegbahn

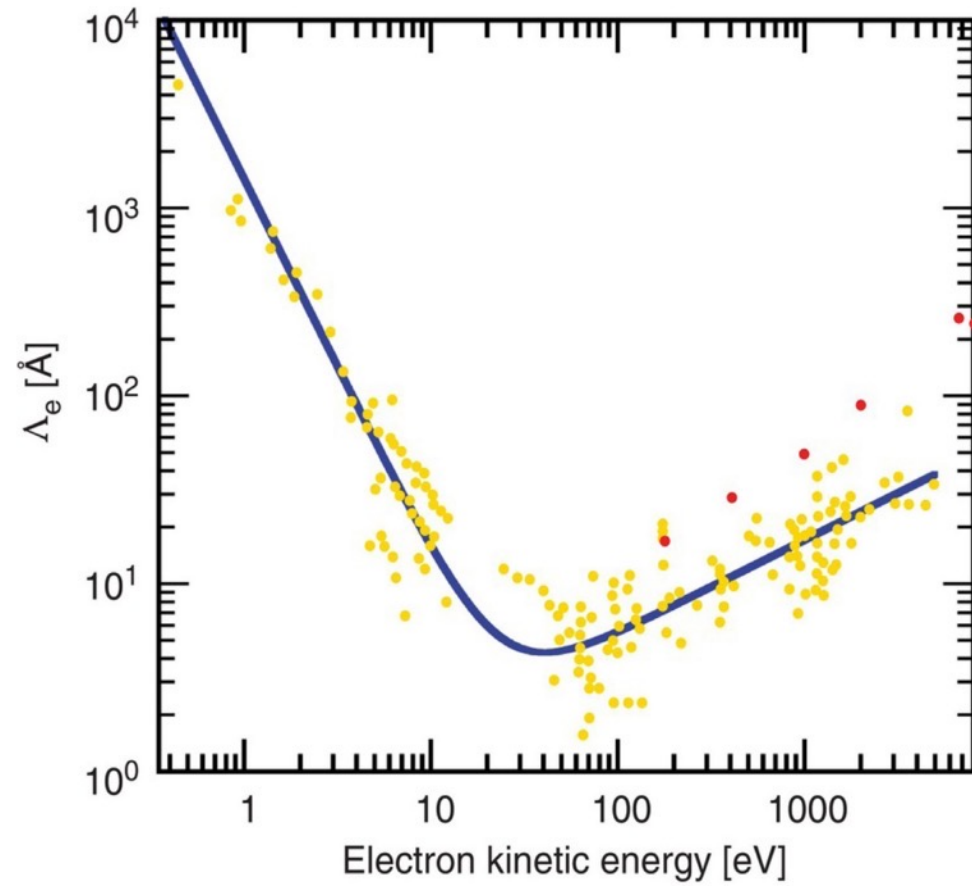
Prize share: 1/2



Vibrational information in photoelectron spectroscopy



The „universal curve of photoemission“



X-ray absorption XAS

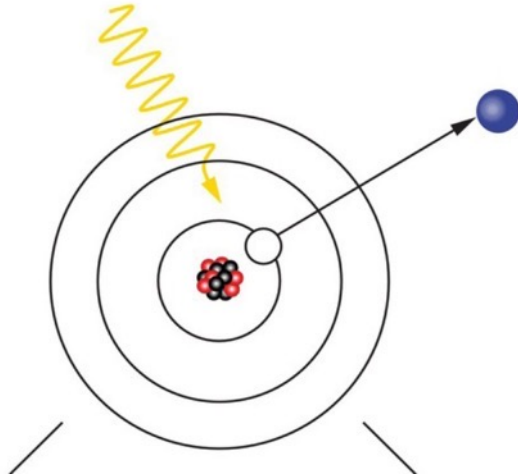
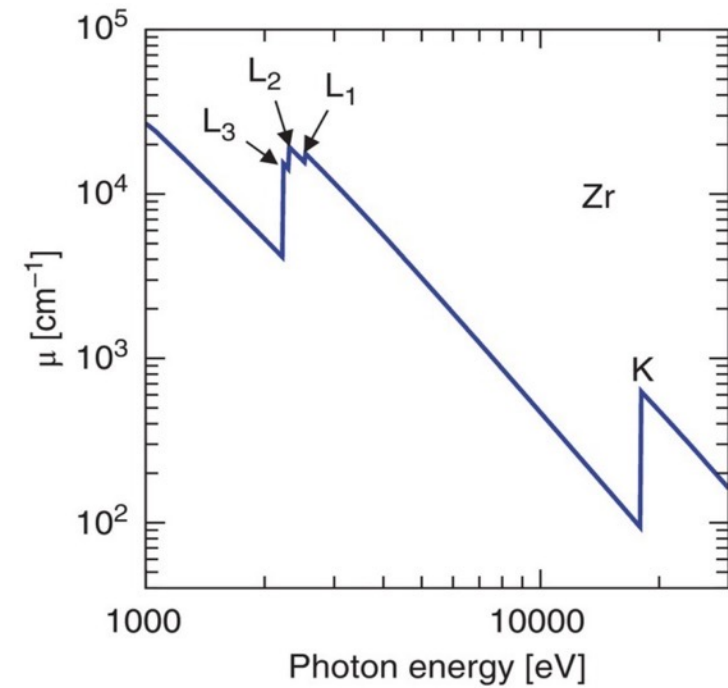
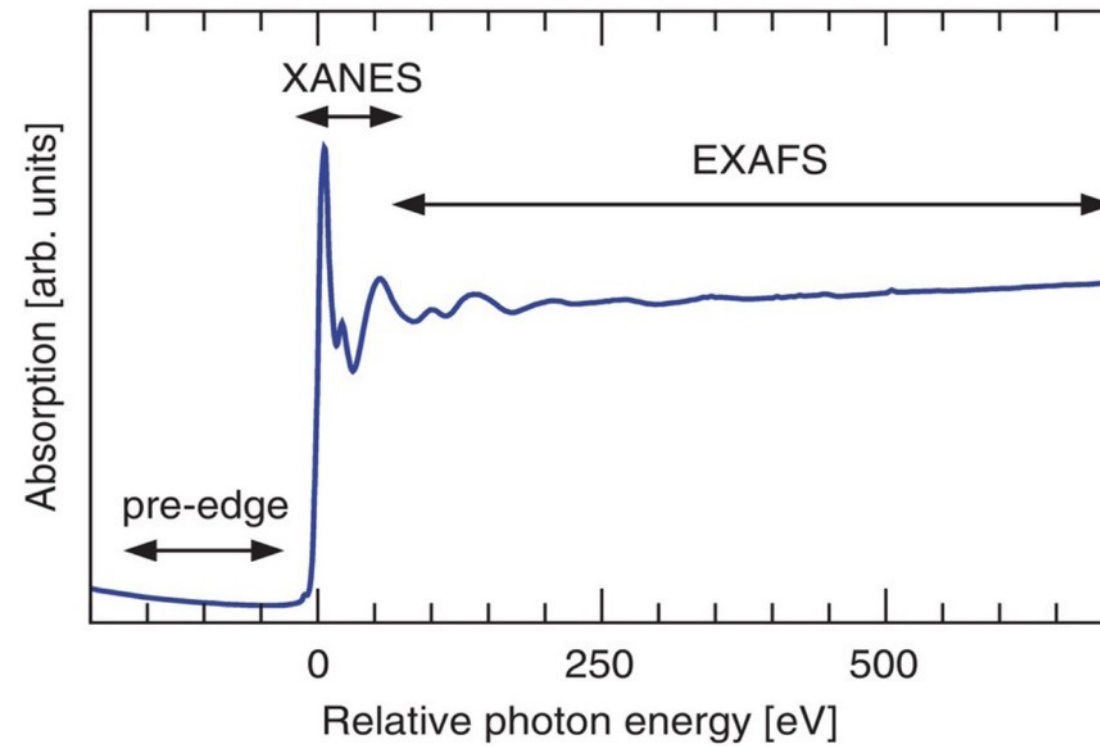


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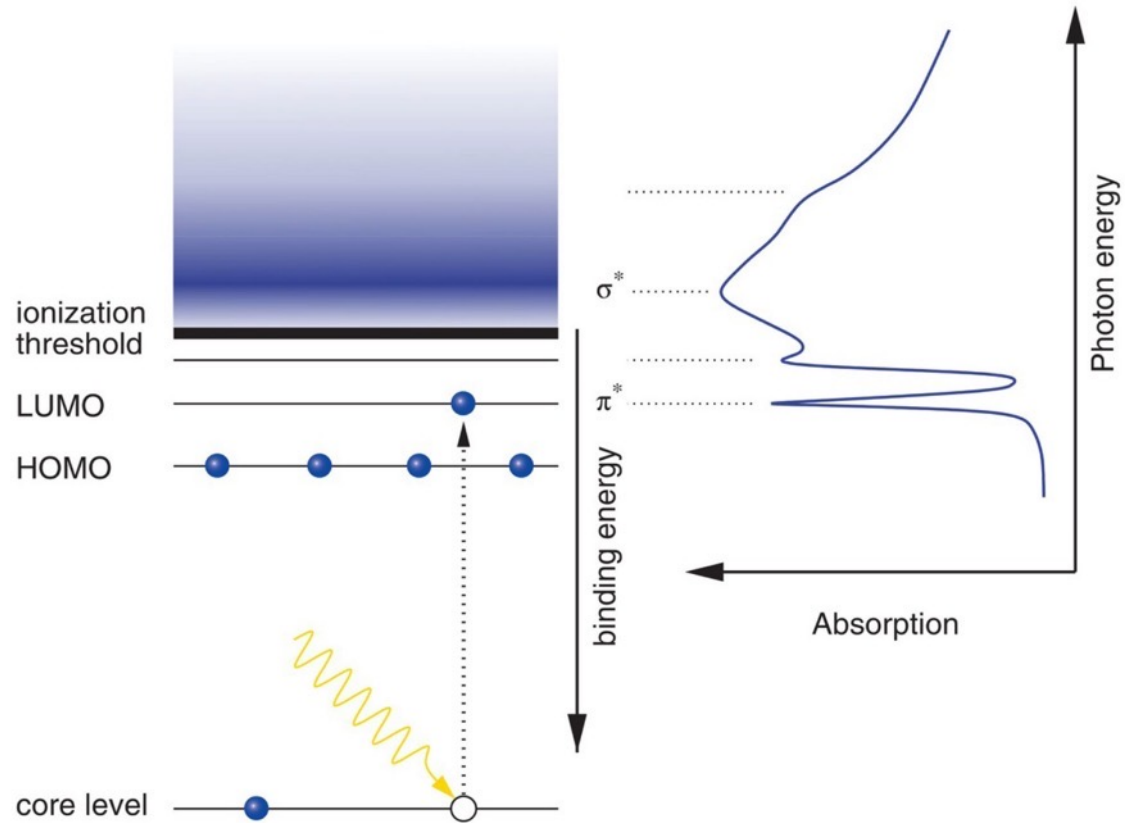
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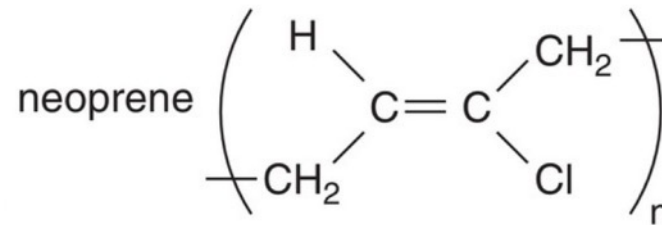
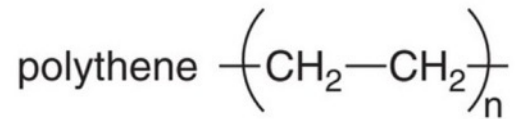
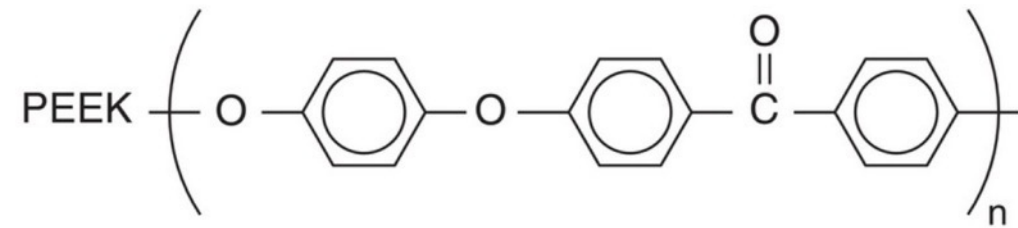
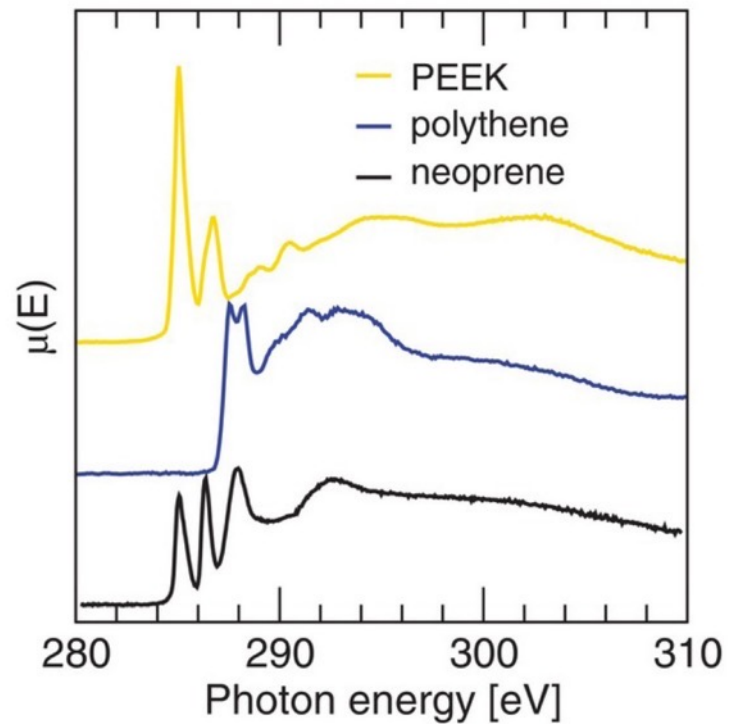
Distinct regions of X-ray absorption



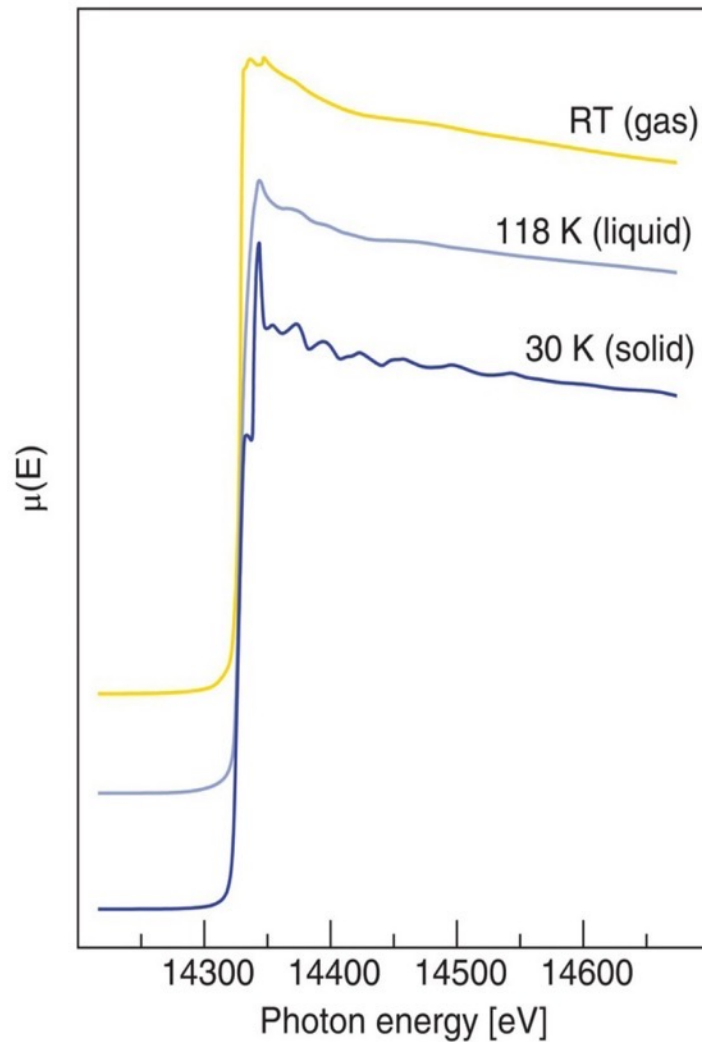
X-ray Absorption Near Edge Structure (XANES)



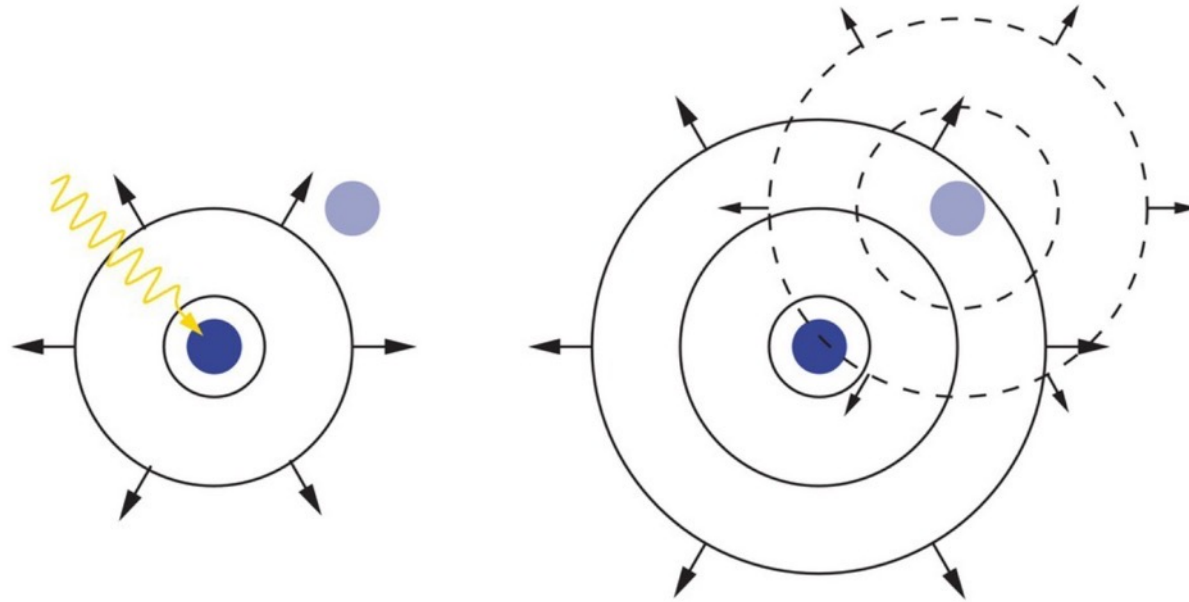
XANES spectra yield detailed information about bonding structure



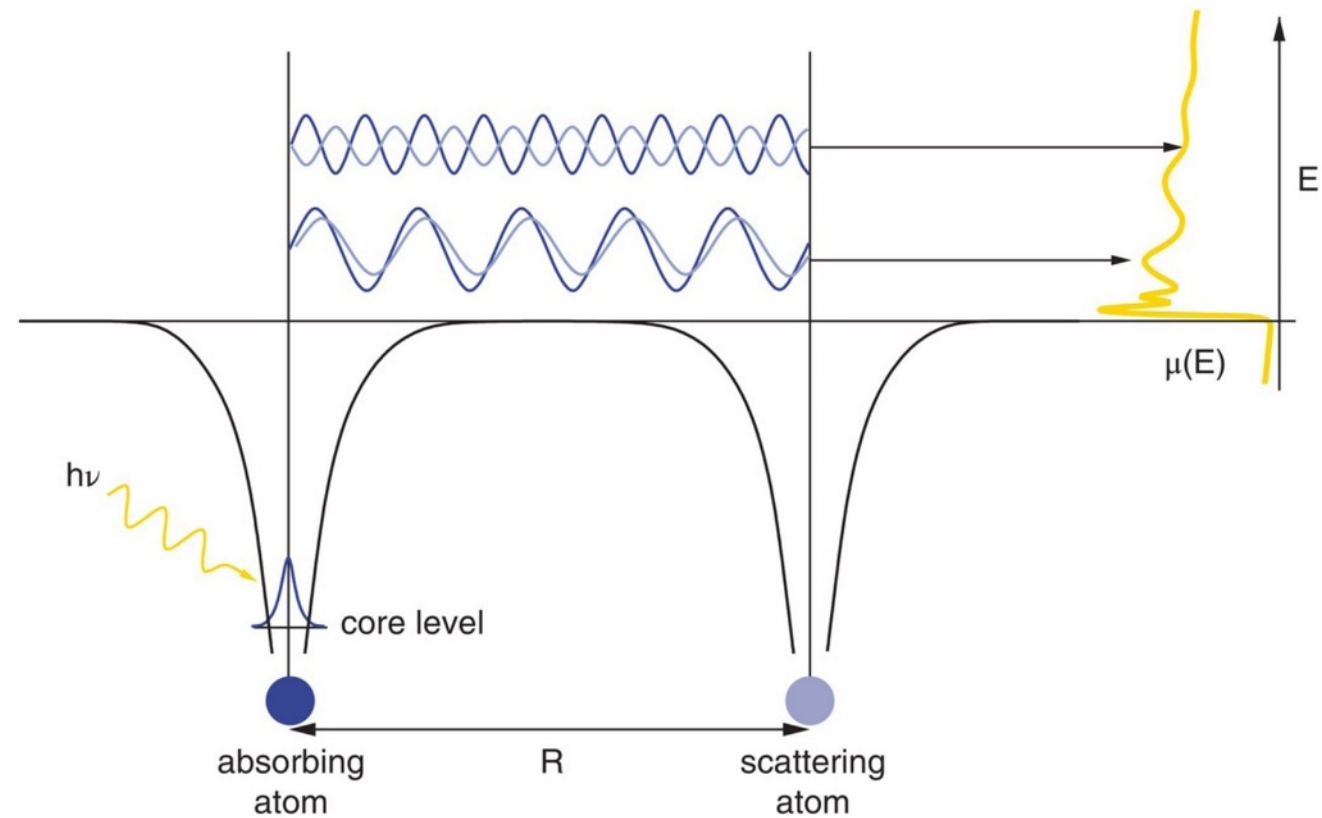
Extended X-ray Absorption Fine Structure (EXAFS) contains information about nearest neighbors



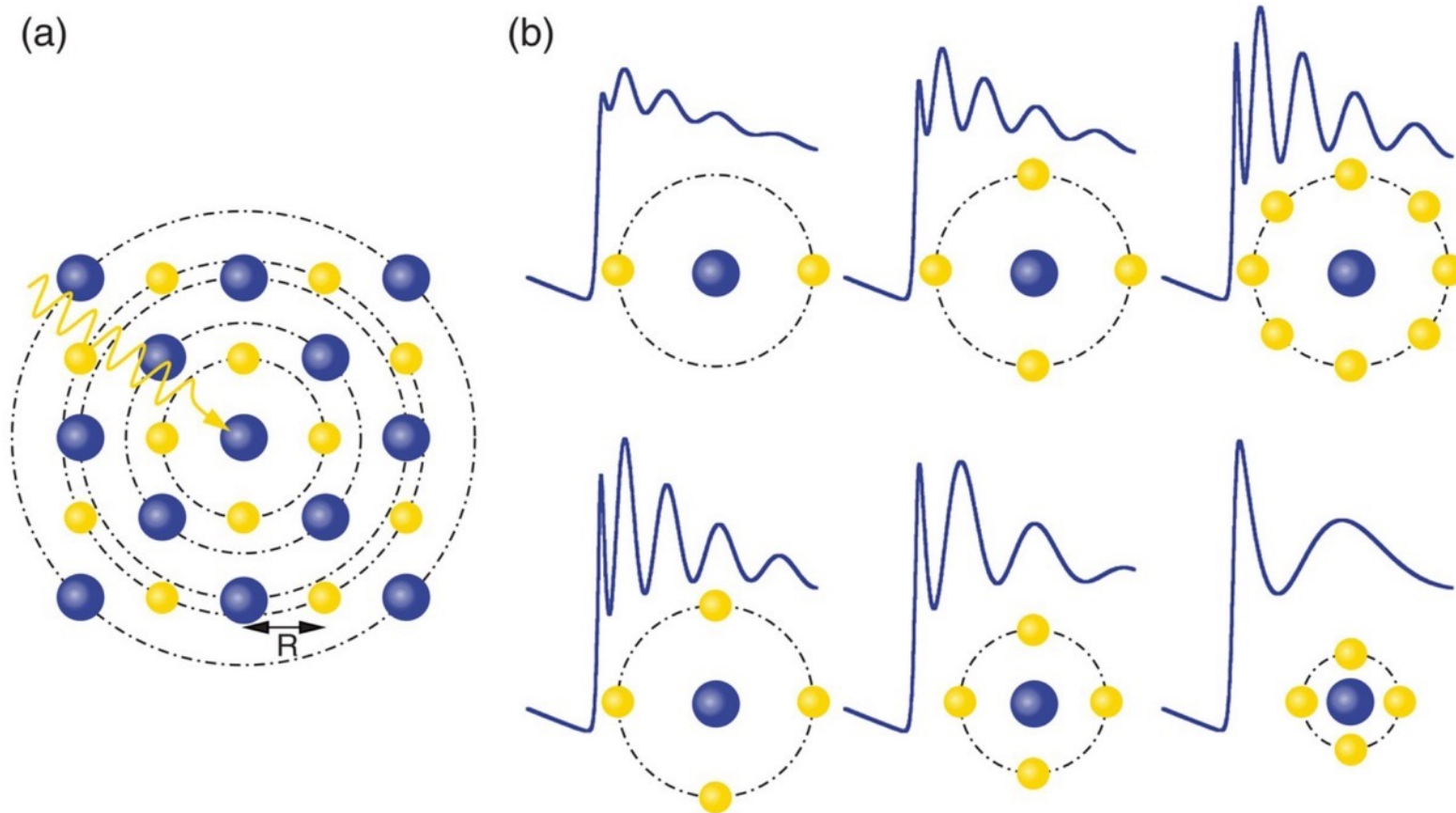
EXAFS and nearest neighbors



EXAFS interference examples



Characteristic features in EXAFS



The end