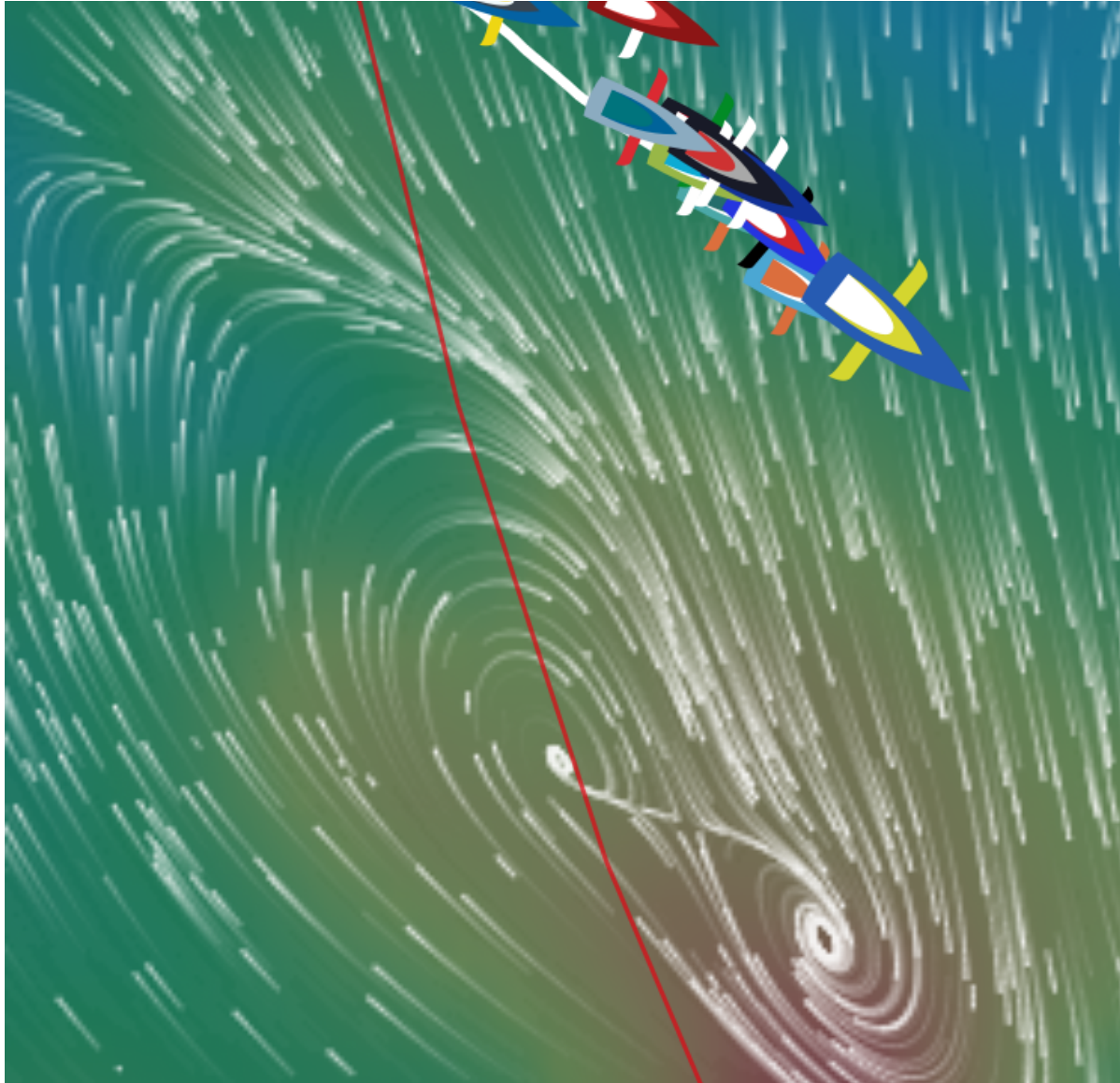




What do you see ?

CHAPTER 6

Entrainment & synchronisation of oscillators

Entrainment of phase oscillators

- Continuous sine coupling
- Pulsed sine coupling (sine map)

Kuramoto model

- Collective synchronization in a population of oscillators

Let's talk about entrainment

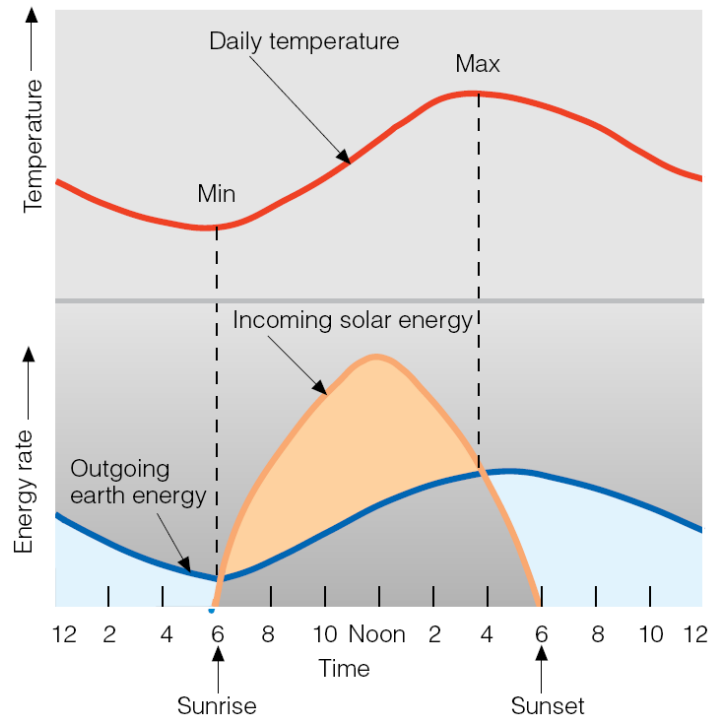


BRITISH
PATHÉ

TACOMA BRIDGE COLLAPSE

PATHE GAZETTE

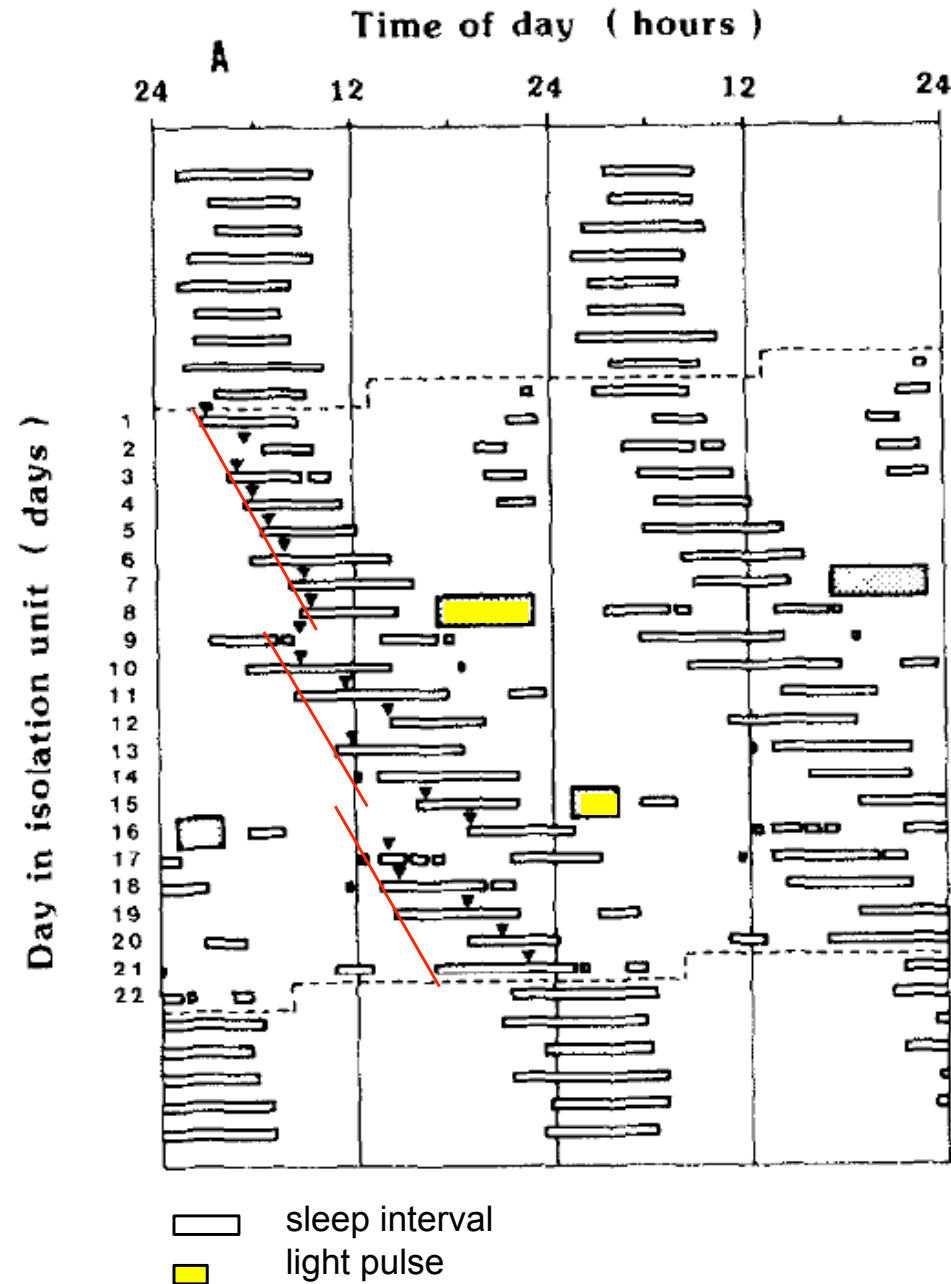
Humans are resonating too



Humans resonate to the light-dark cycle

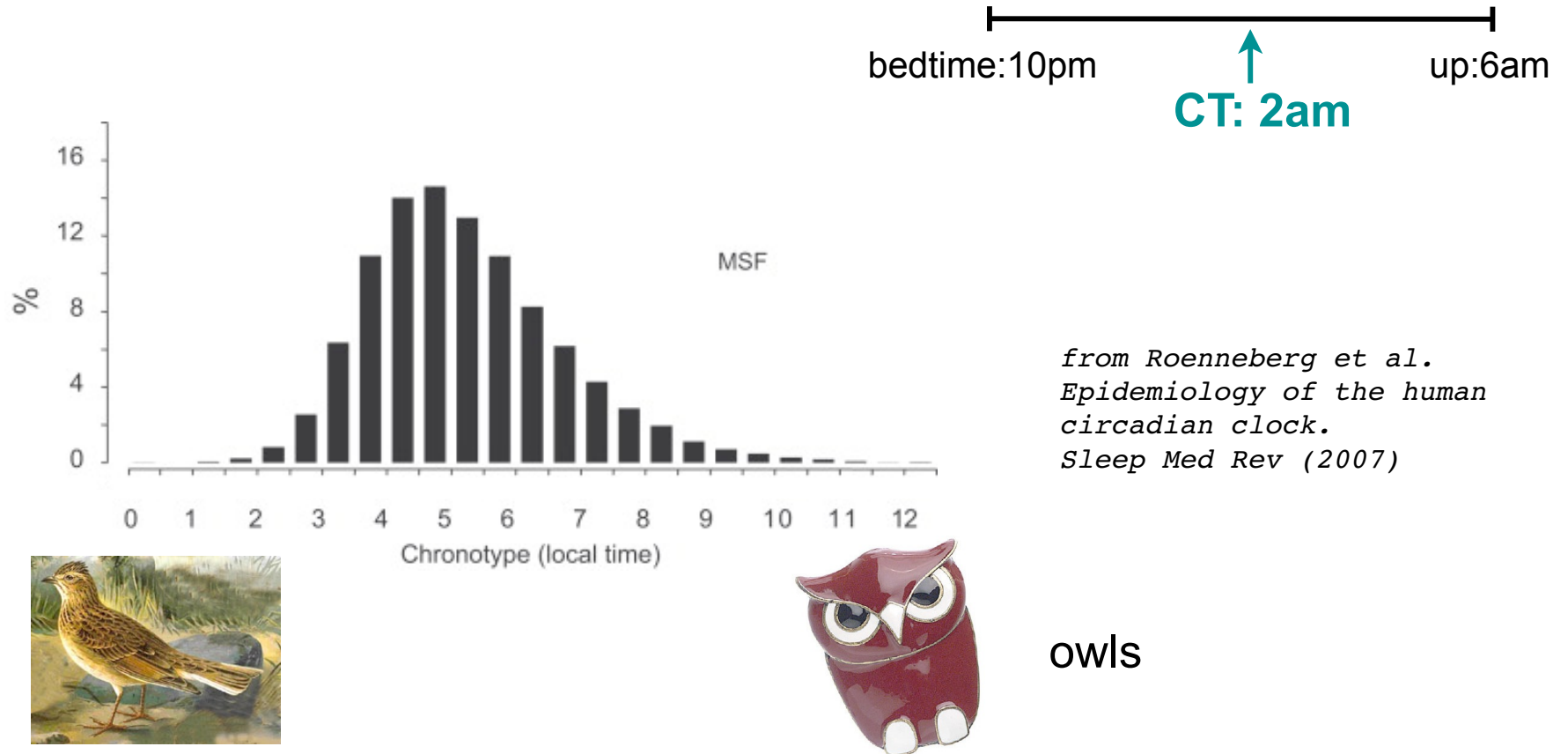
Phase-dependent shift of free-running human circadian rhythms in response to a single bright light pulse

K. Honma, S. Honma and T. Wada* *Experientia* 43 (1987), Birkhäuser Verlag, CH-4010 Basel/Switzerland



Chronobiology, larks and owls

ChronoType (CT): time corresponding to mid-point in sleep

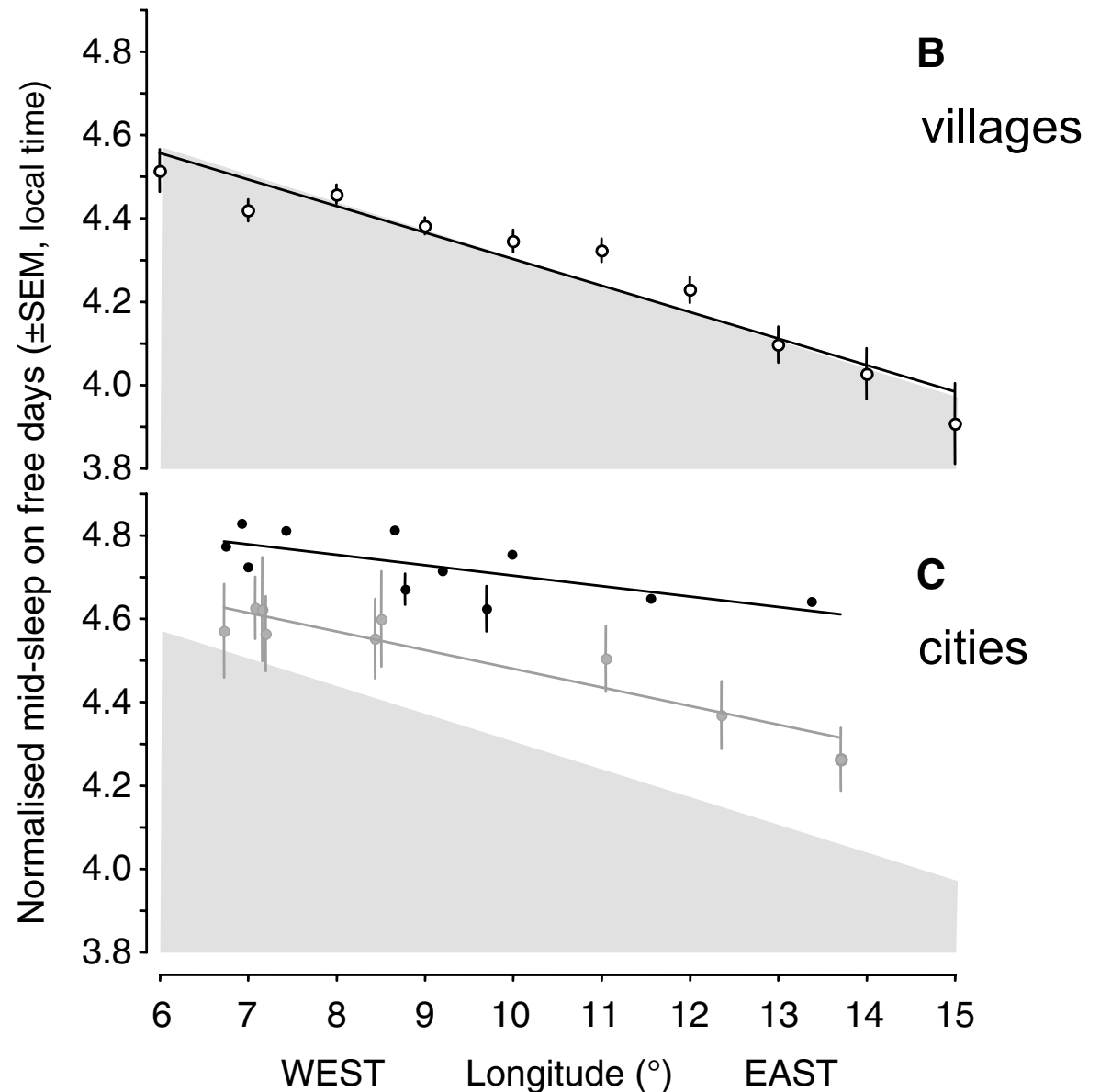
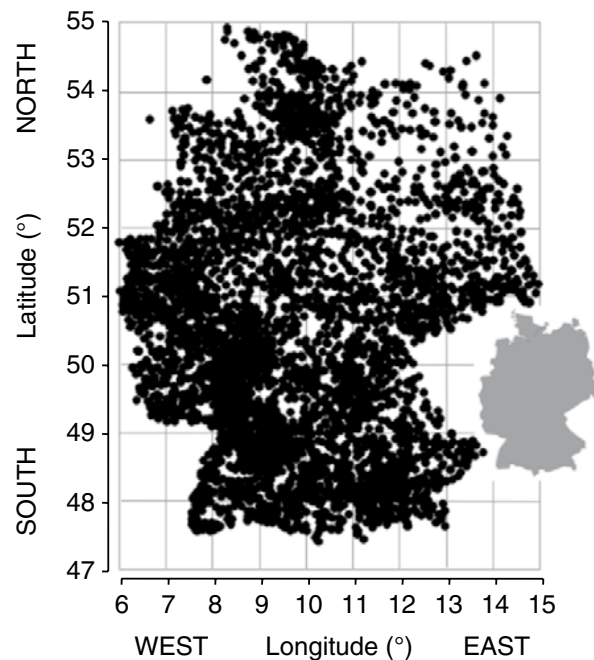


Interpretation: Chronotype as a fixed point φ^* (see 6.1)

Humans (mostly) resonate with solar time, not social time

The human circadian clock entrains to sun time

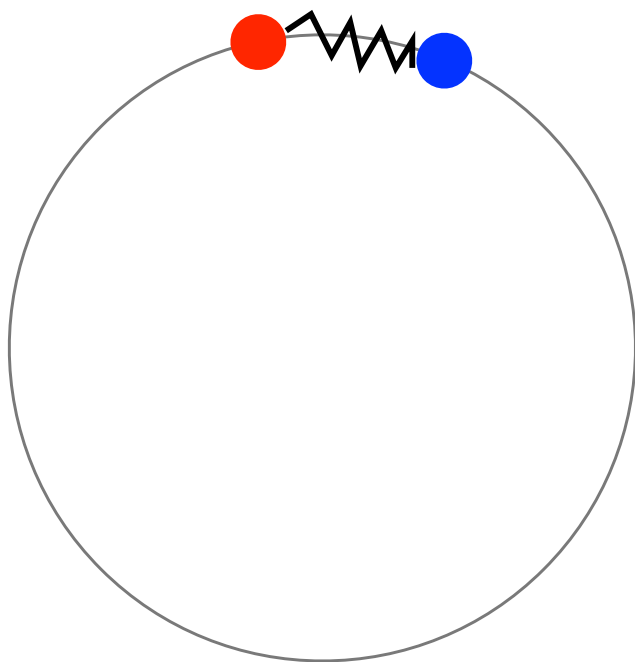
Till Roenneberg¹,
C. Jairaj Kumar² and
Martha Merrow³



Two model of coupling: continuous and pulsed

Model I (6.1)

- $\dot{\alpha} = \Omega$
- $\dot{\theta} = \omega + K \sin(\alpha - \theta)$



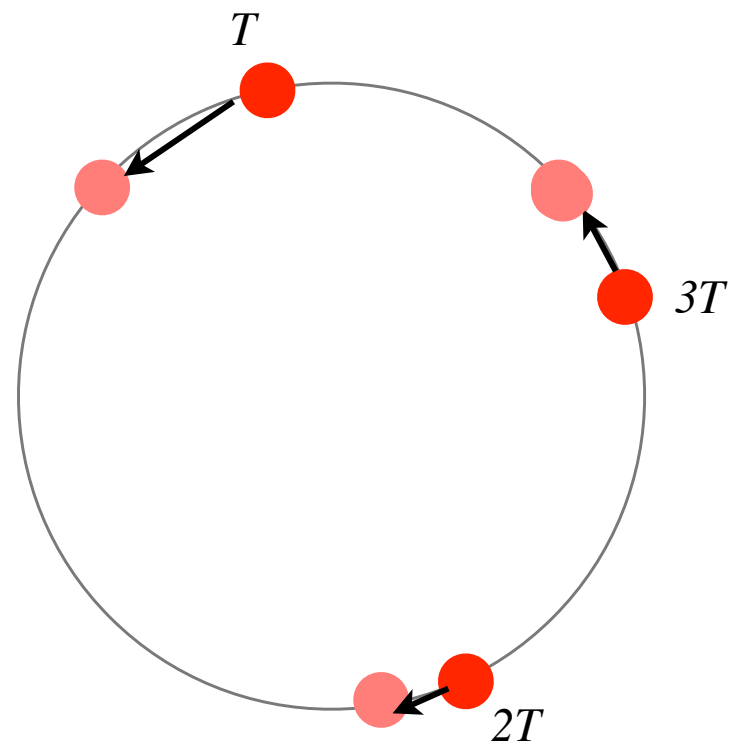
'Like a spring'

Model II (6.2)

$$\dot{\theta} = \omega + \sum_n \delta(t - nT) g(\theta(t))$$

$$\theta_n = \theta_{n-1} + \omega T + g(\theta_{n-1})$$

$$g(\theta) = e \sin(\theta)$$



instantaneous kicks