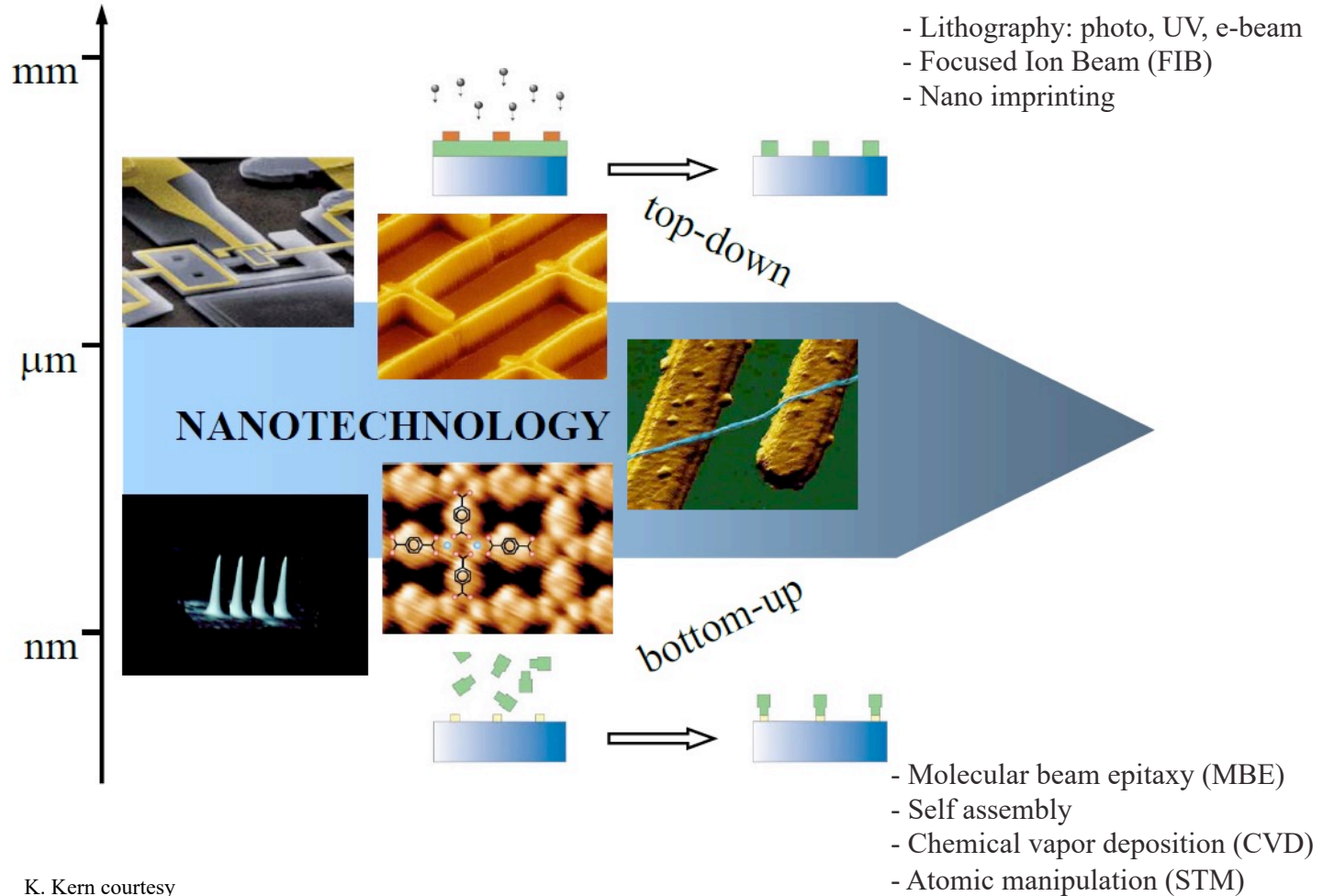
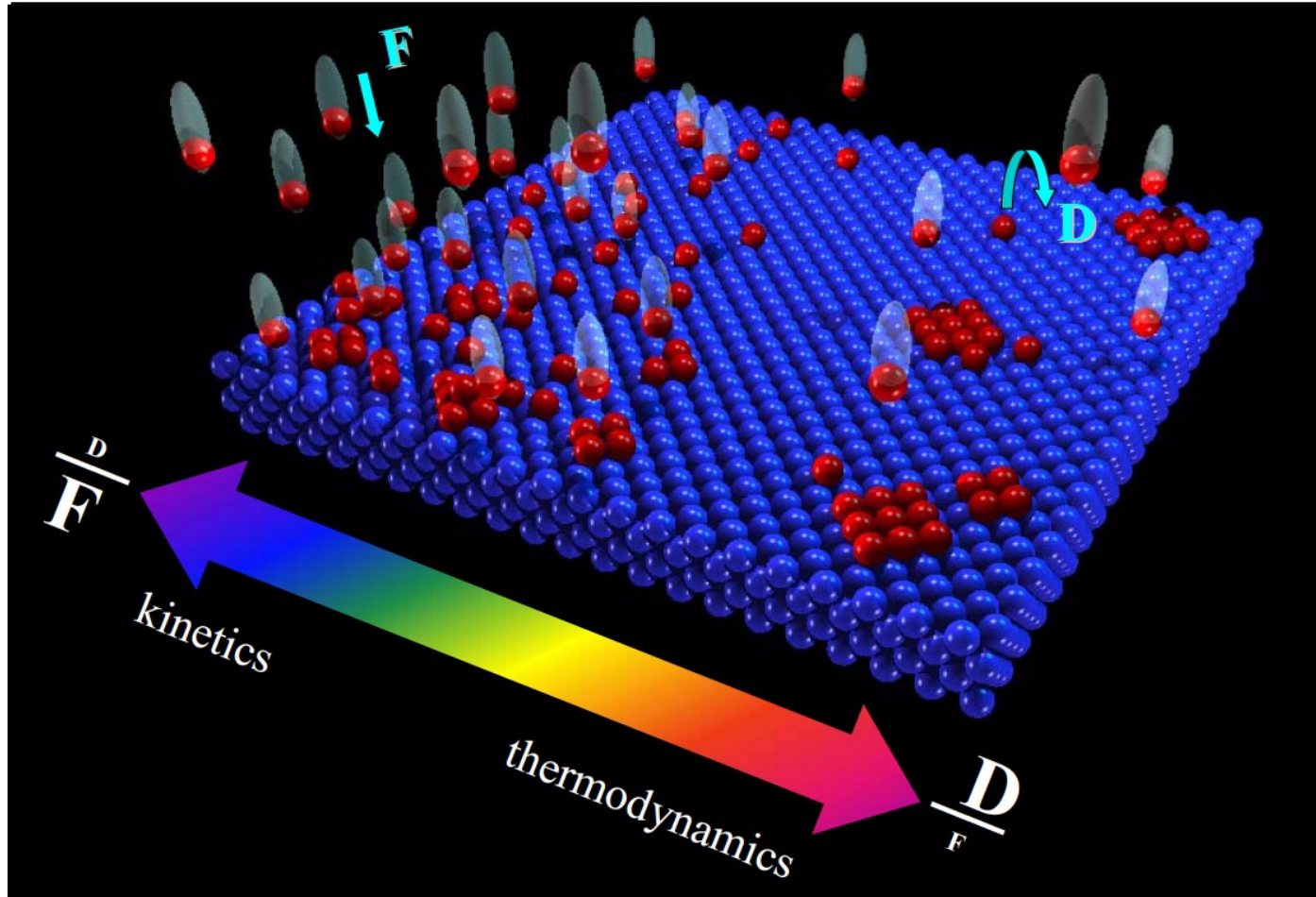


How to make the nanostructures: two approaches



Thin film growth / Nanostructure growth



Surface tension, surface energy and equilibrium surfaces

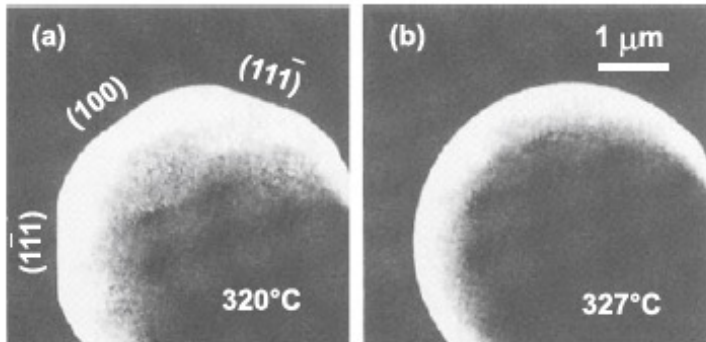
from bulk, creation of a surface (atoms that are not fully coordinated, i.e. broken bonds) → additional energy term γ : surface energy per unit surface (surface tension)

$\gamma > 0$ and energy = γA , with A the area of the additional surface, at constant volume

shape of a solid at equilibrium minimizes the surface energy

in liquids γ is isotropic → spherical shape (smallest surface area)

in solids γ is different for the different surface orientations of a crystal: $\gamma(\vec{n})$



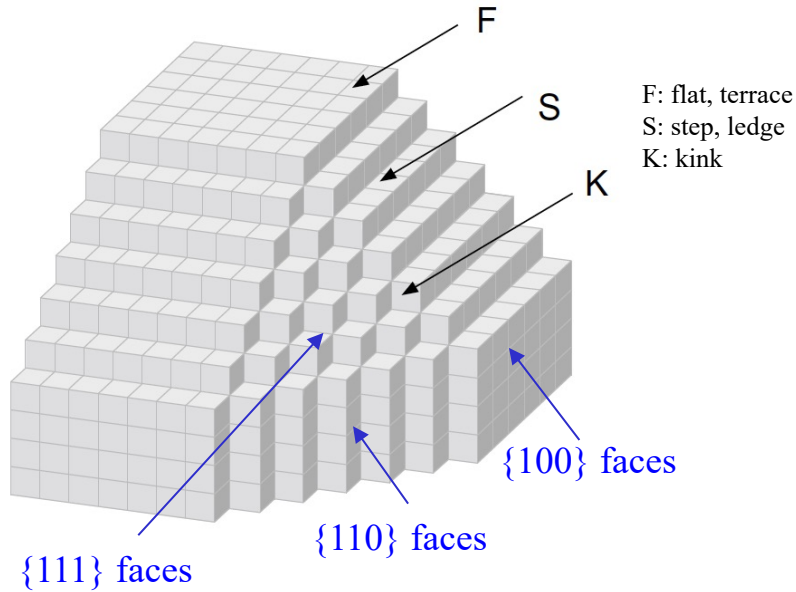
SEM photographs of the equilibrium shape of Pb crystals in the [011] azimuth; in b) Pb is liquid
J.J. Métois & J.C. Heyraud, **31**, 73 (1989)

Kossel crystal – TLK model

different crystal orientation → different surface energy

simplest model: Kossel crystal (simple cubic - sc)

evaluate the number of broken bonds per unit surface depending on the surface orientation



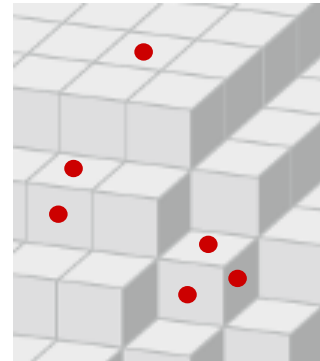
considering only the nearest neighbors (NN)

bulk: 6 NN → 6 bonds per atom

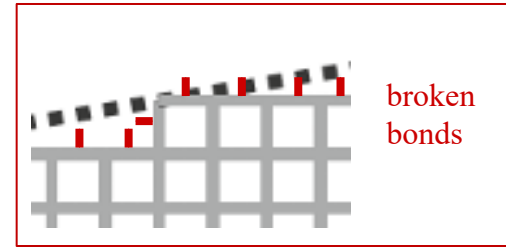
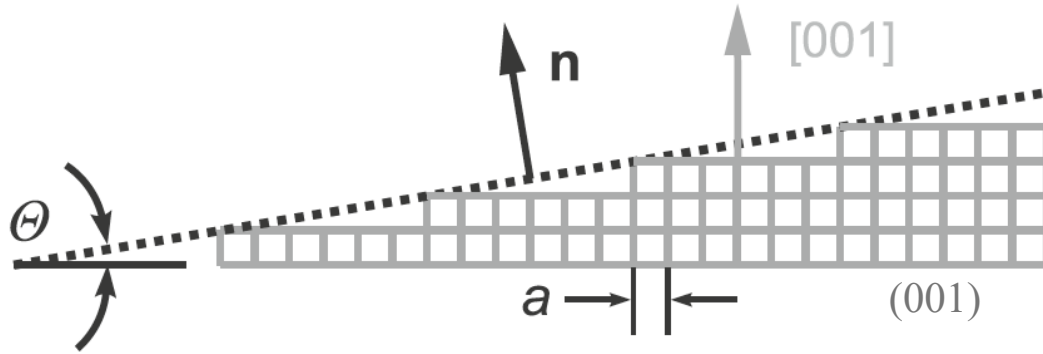
terrace: 5 NN → 5 bonds per atom, 1 broken bond

step: 4 NN → 4 bonds per atom, 2 broken bonds

kink: 3 NN → 3 bonds per atom, 3 broken bonds
(half-crystal site)



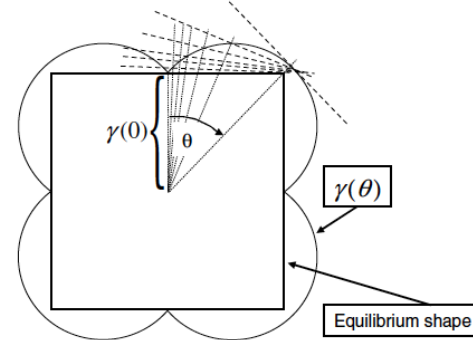
Vicinal surfaces (stepped)



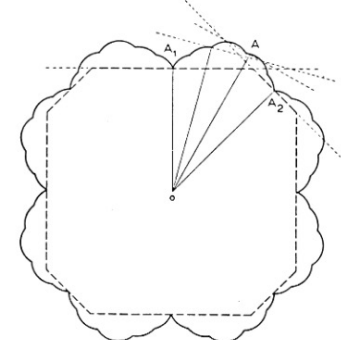
Wulff construction / γ plot

- The surface energy of a vicinal surface always exceeds that of the corresponding singular surface
- From $\gamma(\theta) \rightarrow$ equilibrium crystal shape
- Experimentally: from crystal shape \rightarrow surface energy

simplest example:



more realistic:



Surface tension for cubic crystals

considering the number of broken bonds per unit surface, for singular (low-Miller index) surfaces:

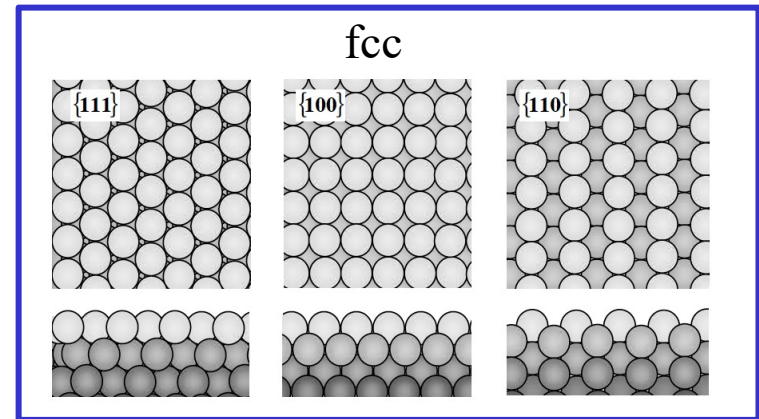
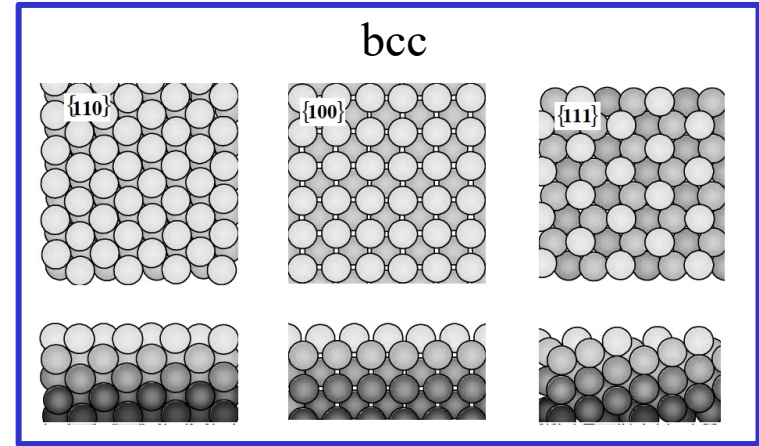
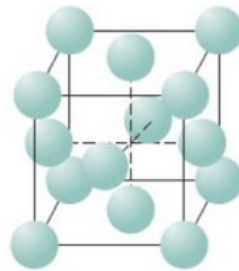
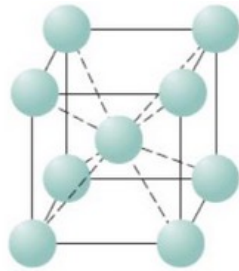
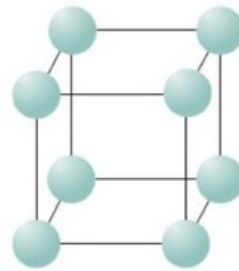
sc: $\gamma_{100} < \gamma_{110} < \gamma_{111}$

bcc: $\gamma_{110} < \gamma_{100} < \gamma_{111}$

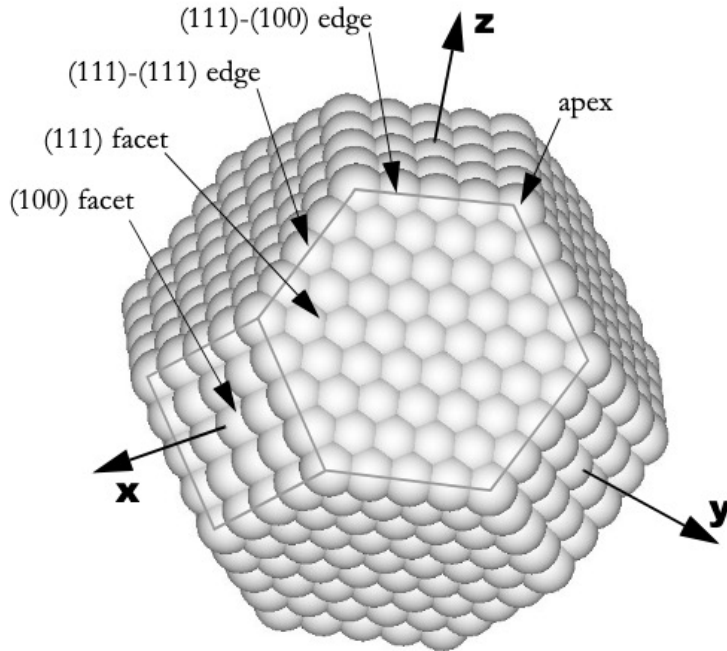
fcc: $\gamma_{111} < \gamma_{100} < \gamma_{110}$

in general, the more compact the surface, the lower the energy

conventional unit cell



Equilibrium crystal shape



1289 atoms, truncated octahedron
surface:volume ratio = 482:807

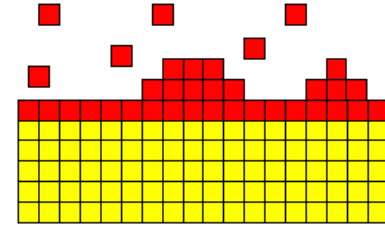
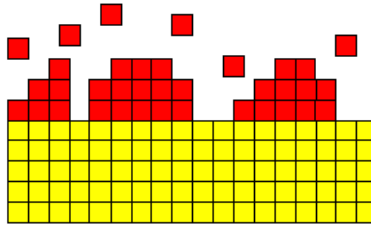
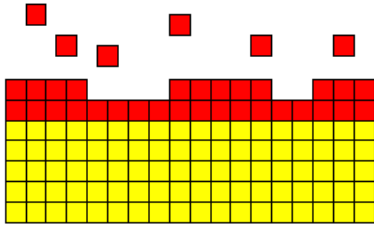
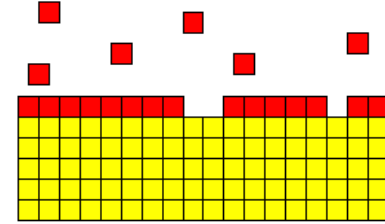
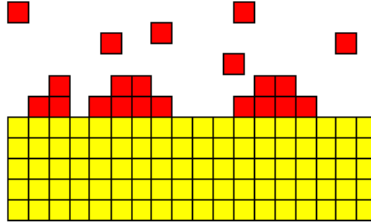
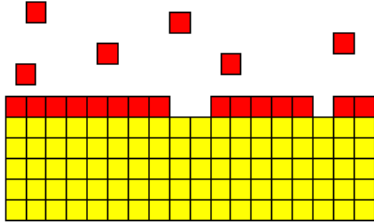
Facts and Figures:

- 482 surface atoms
- 8 (111)-facets
- 6 (100)-facets
- 24 apex positions
- 54 atoms on a (100)-surface (excluding edges)
- 296 atoms on a (111)-surface (excluding edges)
- 36 atoms form a (111)-(111) edge
- 72 atoms form a (100)-(111) edge

Warning: the broken bond model for surface energy neglects the relaxation in positions of the atoms near the surface of a crystal (discussed later)

Growth modes (at thermodynamic equilibrium)

Growth of B on A



layer - by - layer growth
(Frank - van der Merve)

island growth
(Volmer - Weber)

layer - by - layer
+ island growth
(Stranski - Krastanov)
surface energy & strain

surface energy

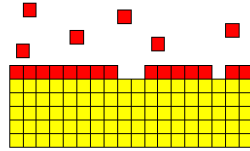
Growth modes (at thermodynamic equilibrium)

Growth of B on A

γ_A : surface energy of A
(interface with vacuum)

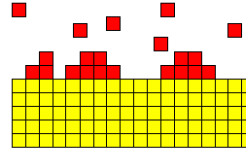
γ_B : surface energy of B
(interface with vacuum)

γ_{AB} :
A-B interface energy
(hybridization,
lattice mismatch,...)



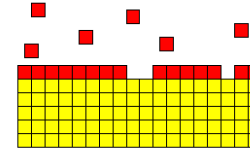
layer - by - layer growth
(Frank - van der Merve)

$$\gamma_B + \gamma_{AB} \leq \gamma_A$$



island growth
(Volmer - Weber)

$$\gamma_A < \gamma_B + \gamma_{AB}$$



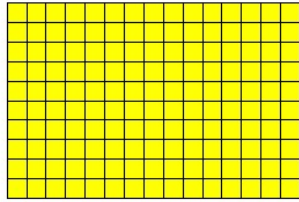
layer - by - layer
+ island growth
(Stranski - Krastanov)

$\gamma_B + \gamma_{AB} < \gamma_A$ at the beginning, but γ_{AB} increases with coverage (typically due to strain) \rightarrow change from 2D to 3D

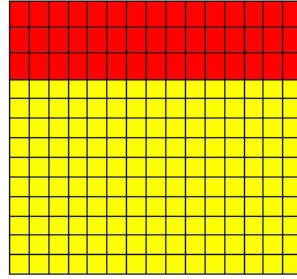
Stranki-Krastanov growth of semiconductor quantum dots

lattice parameters
don't match

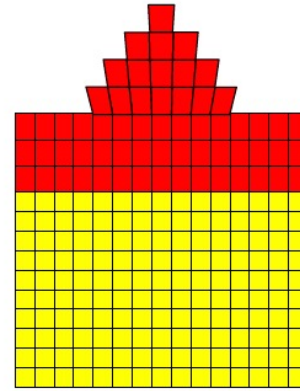
$$a_B > a_A$$



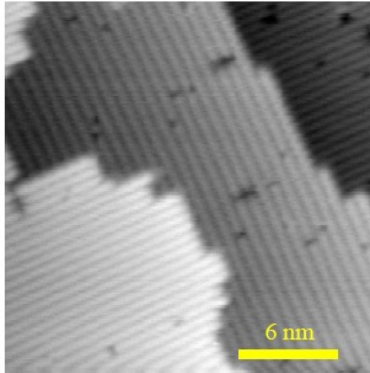
substrate



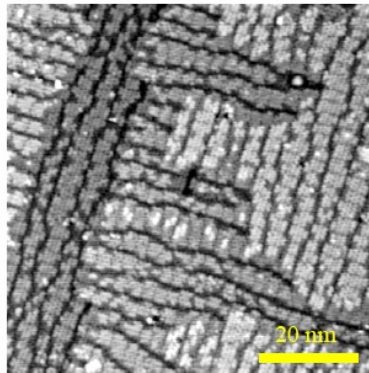
wetting layer



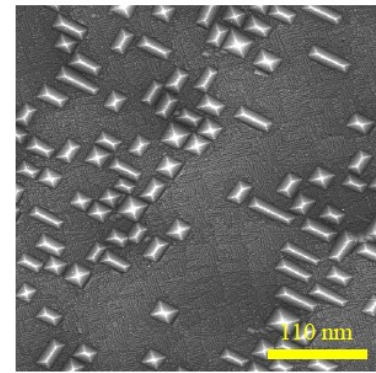
islands



Si(001)



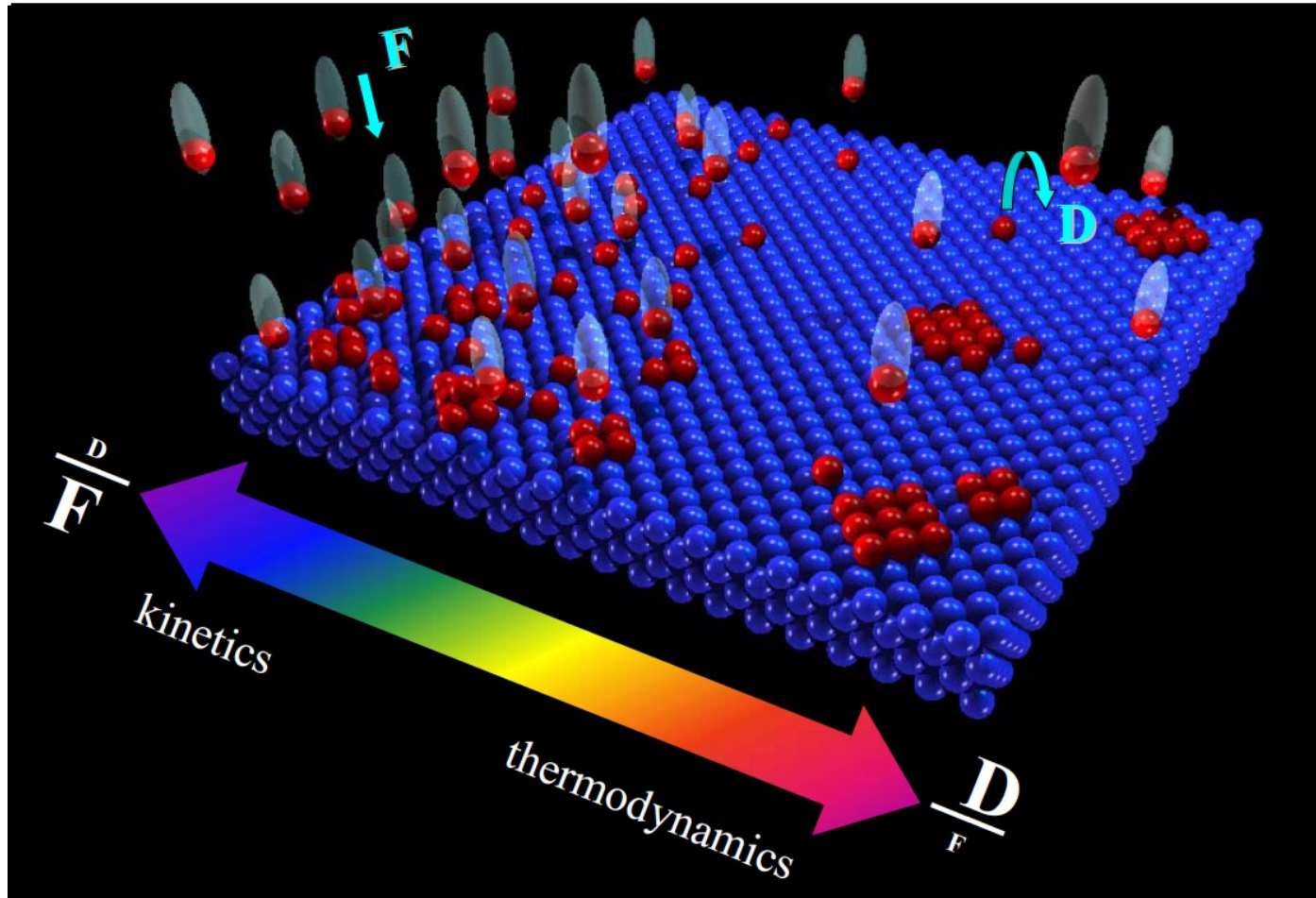
3ML Ge on Si(001)



6ML Ge on Si(001)

exact shape:
balance between
surface energy,
strain energy, and
volume

Thin film growth / Nanostructure growth

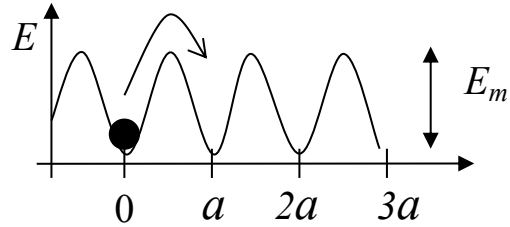


Growth as a non-equilibrium process: kinetics

single crystal surfaces: a 2D laboratory

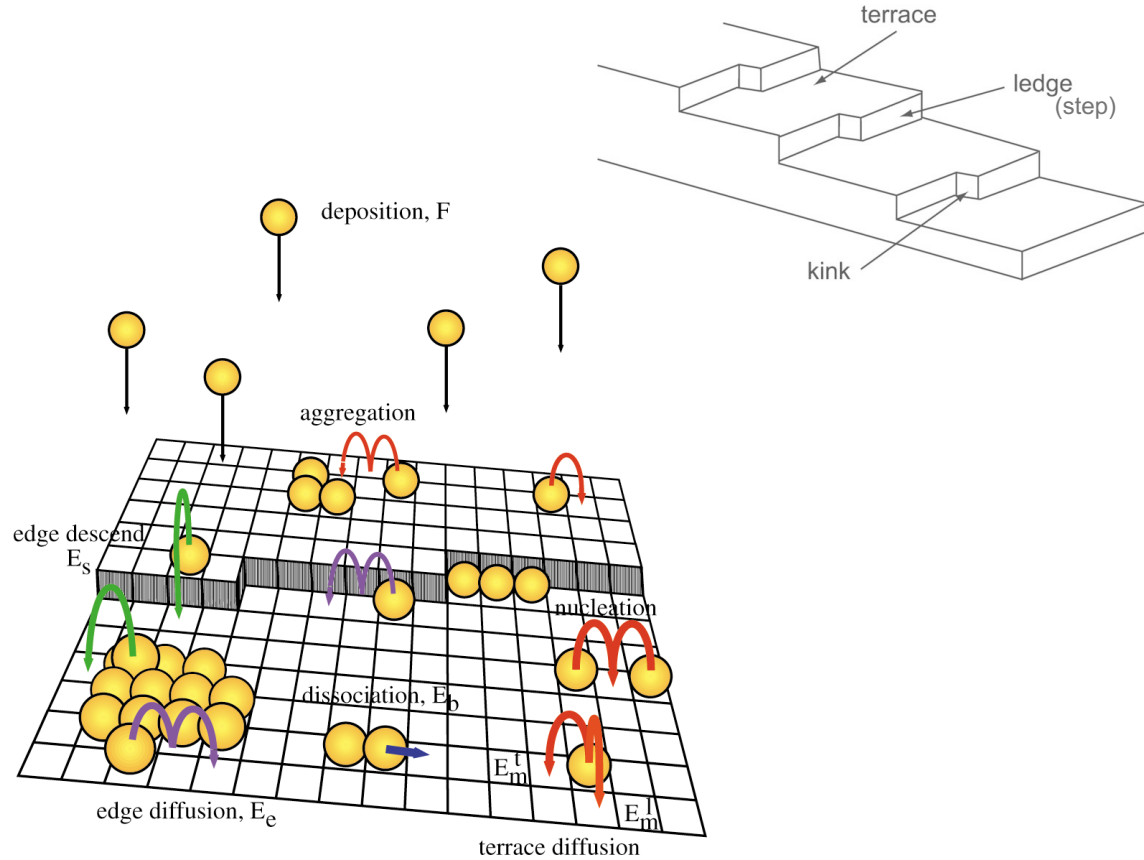
each process i has
an energy barrier E_i and a rate ν

$$\nu = \nu_0 \exp(-E_i/k_B T)$$



diffusion process, random walk
 a lattice constant, t time
number of jumps = νt
mean squared displacement:

$$\langle \Delta r^2 \rangle = \nu a^2 t$$



Growth as a non equilibrium process

Aim: controlling

- mean size (size distribution)
- density
- shape
- composition

Control parameters:

- substrate temperature T
- deposition flux F
- surface coverage Θ
- substrate/overlayer material (strain, mixing, etc.)
- substrate symmetry or patterning

Statistical growth: $T \rightarrow 0$ K

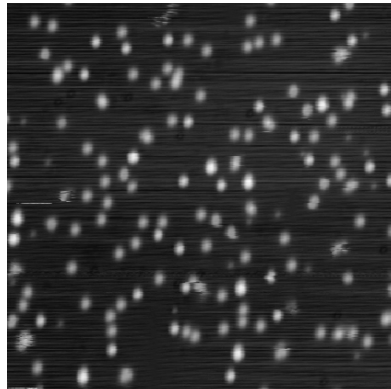
- thermally-activated diffusion is frozen

$$v = v_0 \exp(-E_1/k_B T) \rightarrow 0$$

- coverage determines mean island size n
- broad size distribution

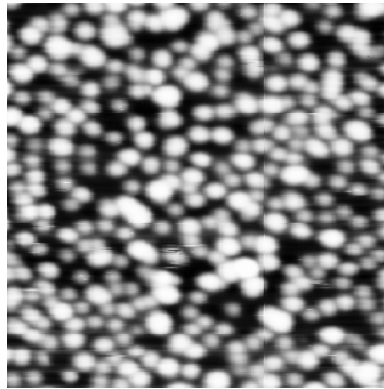
Co/Pt(111)

0.03 ML, $T = 50$ K:
 $n = 1.2$



50 Å

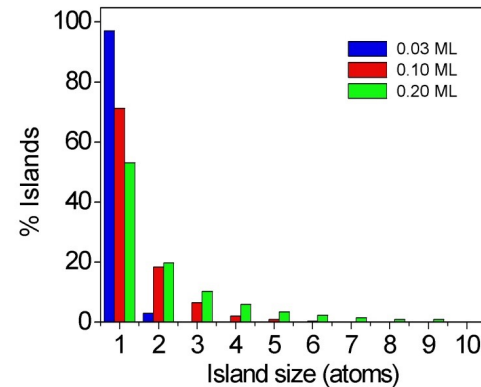
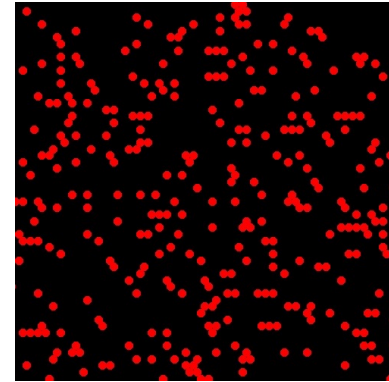
0.10 ML, $T = 50$ K:
 $n = 2.9$



50 Å

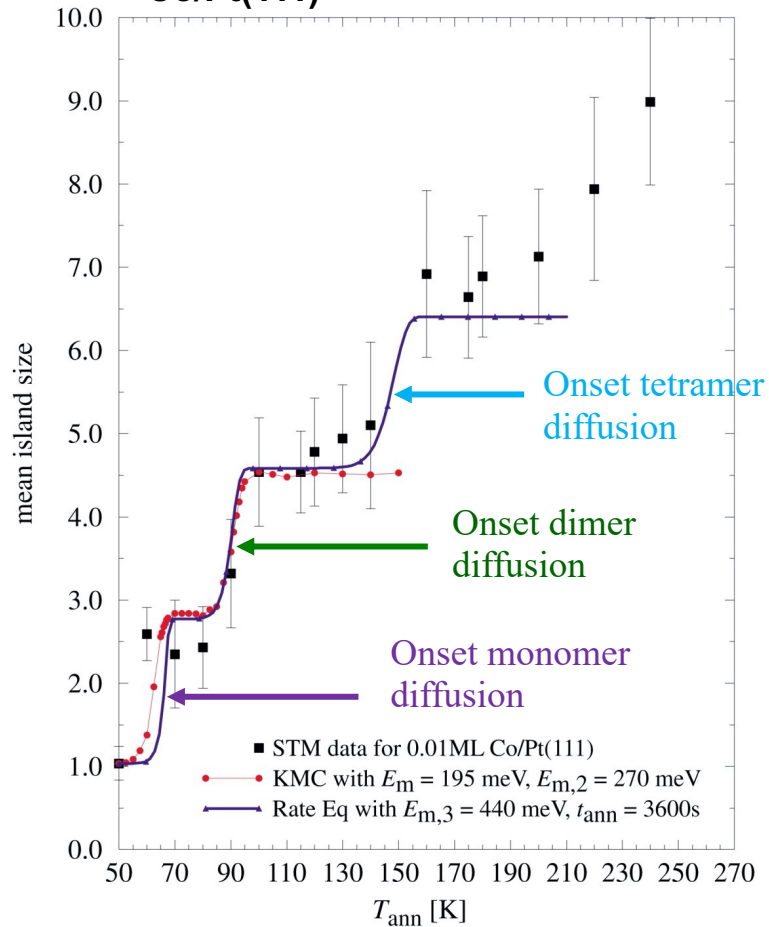
$n = \text{mean island size} = \text{coverage}/\text{island density}$

Kinetic Monte Carlo
simulation

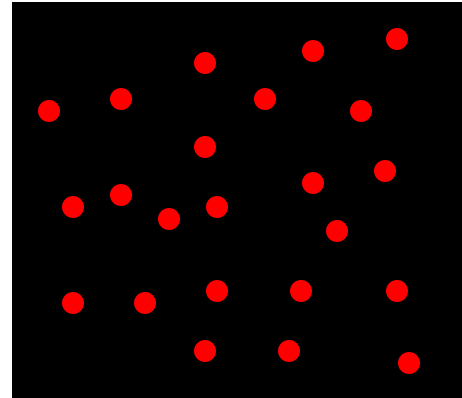


Adatom and cluster diffusion

Ex:
Co/Pt(111)

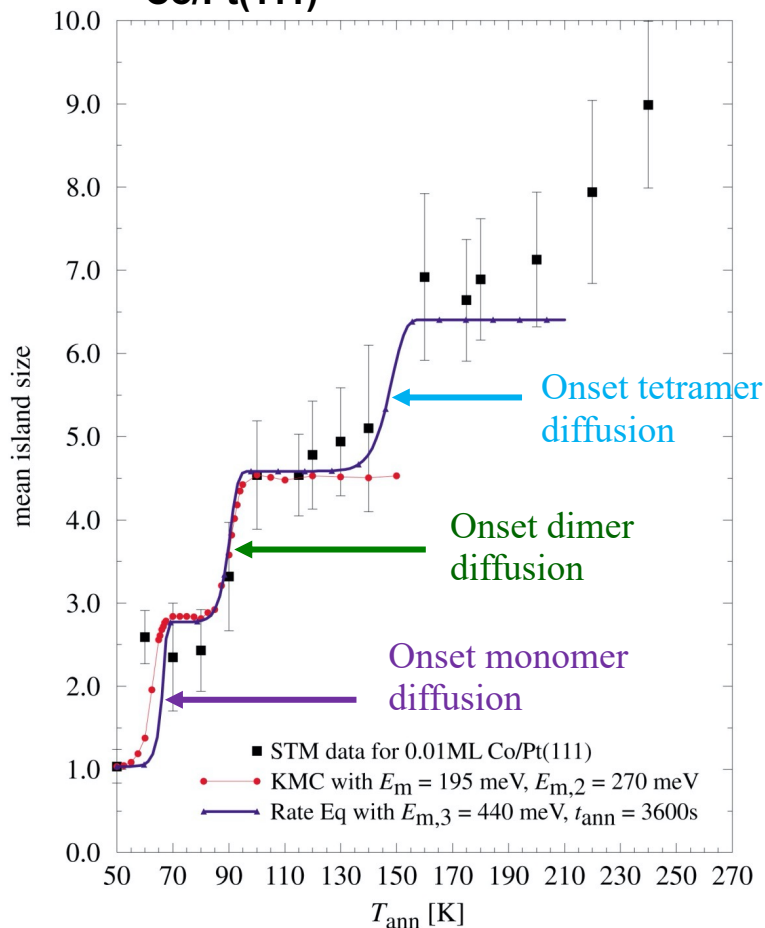


$T < 60$ K: monomers



Adatom and cluster diffusion

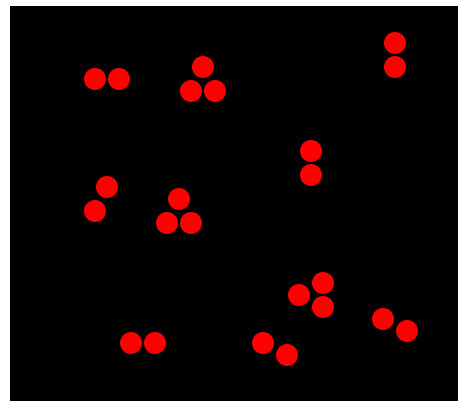
Ex:
Co/Pt(111)



By increasing T , sequential activation of cluster diffusion results in size selection:

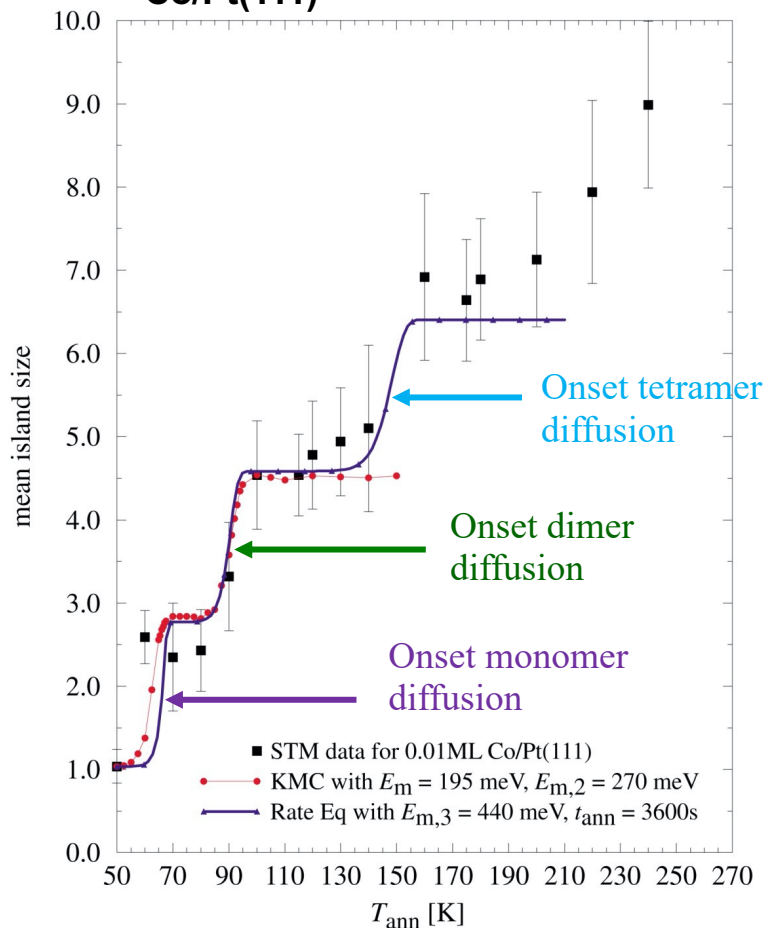
$T < 60$ K: monomers

$60 \text{ K} < T < 90 \text{ K}$: dimers and trimers



Adatom and cluster diffusion

Ex:
Co/Pt(111)

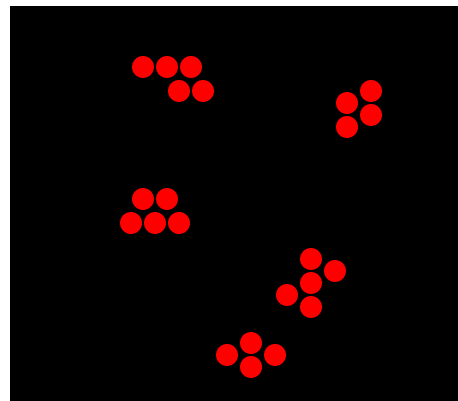


By increasing T , sequential activation of cluster diffusion results in size selection:

$T < 60$ K: monomers

$60 \text{ K} < T < 90 \text{ K}$: dimers and trimers

$100 \text{ K} < T < 130 \text{ K}$: tetramers and pentamers



Rate equations: simple case of $i = 1$

Assumption: adatom can diffuse with a rate D
but

dimer is stable, i.e. when two atoms meet, they cannot detach

Critical size $i=1$

Time evolution of average values of n_1 and n_x

n_1 adatom density

Dimer creation

Growth flux

Adatom-island attachment

$$\frac{dn_1}{dt} = F - 2\sigma_1 D n_1^2 - \sigma_x D n_1 n_x - k_x F (Ft - n_1) - 2k_1 F n_1$$

Direct impinging on an island

Direct impinging on an adatom

$$\frac{dn_x}{dt} = \sigma_1 D n_1^2 + k_1 F n_1$$

$$D = D_0 \exp(-E_1/k_B T)$$

σ_1 and σ_x capture rates

E_1 is the diffusion energy barrier of a monomer ($i=1$)

Rate equations give the formation rate for adatoms and stable islands

Island density

$$n_x = \eta(\theta, i) \left(\frac{D}{F}\right)^{-\chi} \exp\left(\frac{E_i^c}{(i+2)k_B T}\right)$$

$$D = D_0 \exp\left(-\frac{E_1}{k_B T}\right)$$

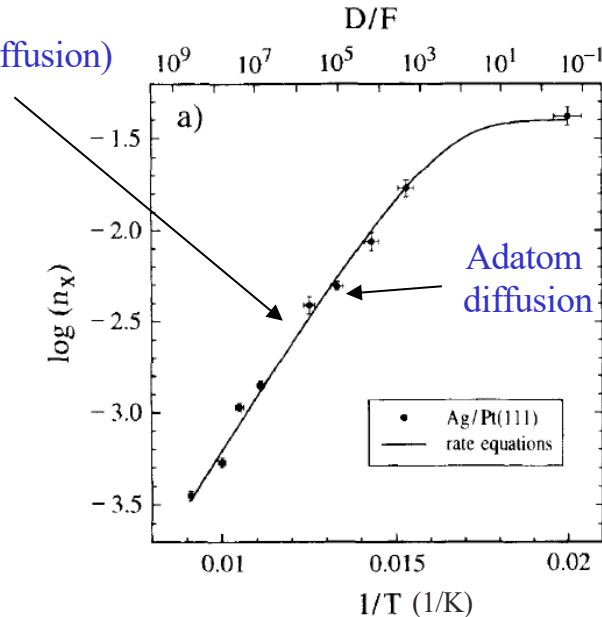
$$\chi = \frac{i}{i+2}$$

E_i^c is the dissociation energy of the island with critical size = i

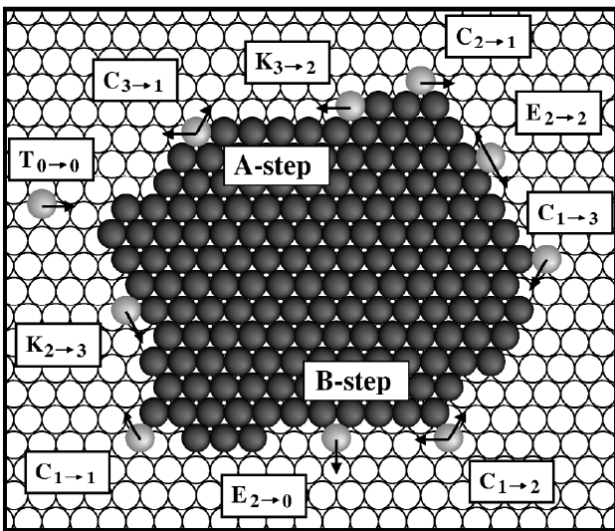
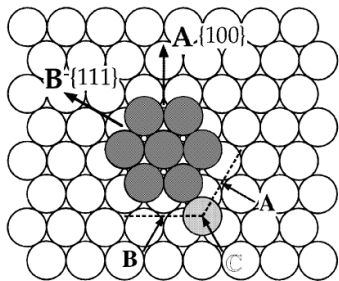
$$i = 1 \rightarrow E_i^c = 0 \rightarrow n_x = \eta(\theta, 1) \left(\frac{D}{F}\right)^{-1/3} = \eta(\theta, 1) \left(\frac{D_0}{F}\right)^{-1/3} \exp\left(\frac{E_1}{3k_B T}\right)$$

The slope gives E_1
(energy barrier for adatom (monomer) diffusion)

Arrhenius plot of saturation island densities (cov. = 0.2 ML) for the regime where dimers are stable nuclei.

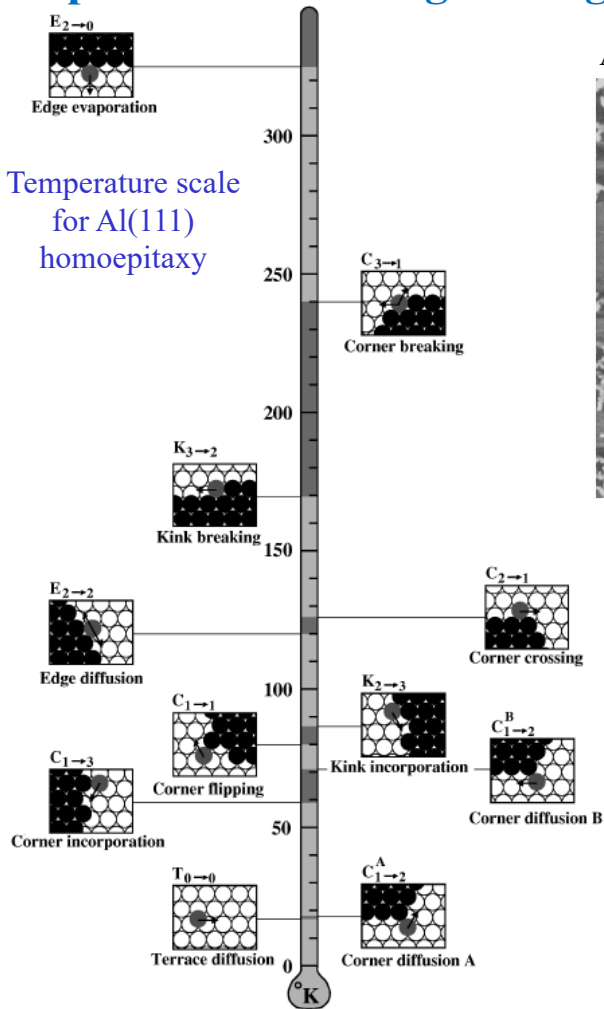


Island shape: diffusion along the edges

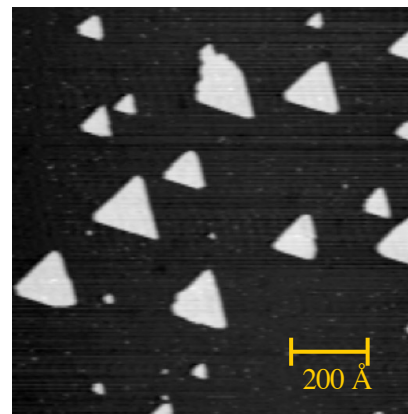
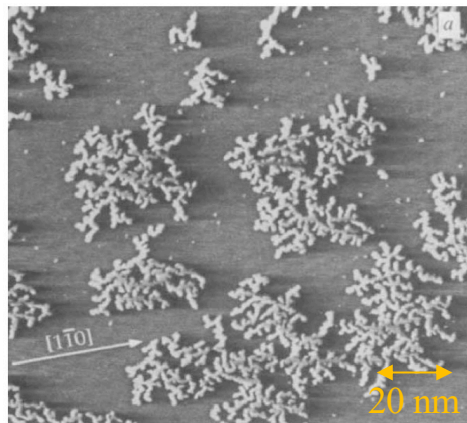


H. Brune *et al.* Nature **369**, 469 (1994);
 S. Ovesson *et al.* Phys. Rev. Lett. **83**, 2608 (1999);
 A. Bogicevic *et al.* **81**, 637 (1998)

Temperature scale
 for Al(111)
 homoepitaxy



Ag/Pt(111) T=110K:
 Adatom stick at the island edge and stop



Co/Pt(111) T=270K:
 Activated adatom edge diffusion

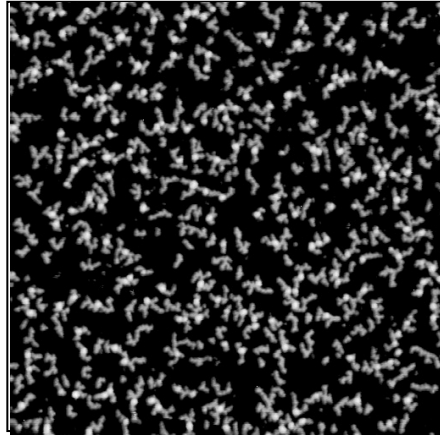
Diffusion rate

Diffusion rate depends on the supporting substrate and on the deposited species

Fe



$$v = v_0 \exp(-E_{\text{Fe}}/k_B T)$$



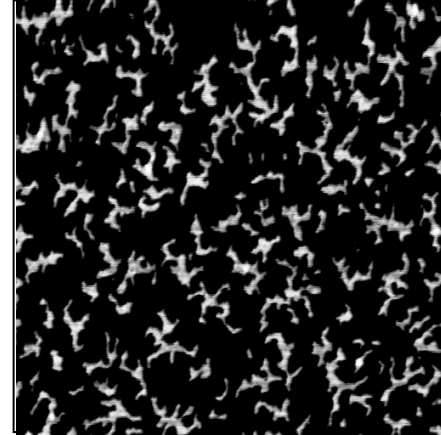
27 nm

Island size = 90 atoms/isl

Co



$$v = v_0 \exp(-E_{\text{Co}}/k_B T)$$



30 nm

Island size = 390 atoms/isl

$T_{\text{dep}} = 140 \text{ K}$
 $\Theta = 0.25 \text{ ML}$
Substrate: Pt(111)

$$E_{\text{Fe}} > E_{\text{Co}}$$

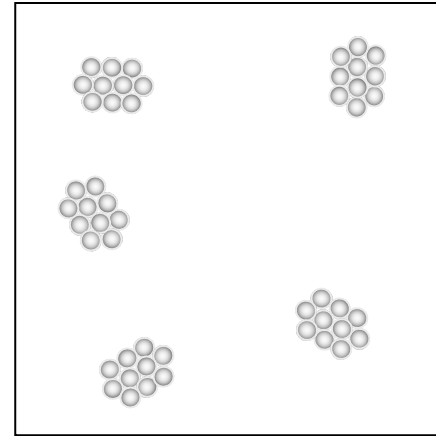
How to form alloy clusters?
How to form lattices?



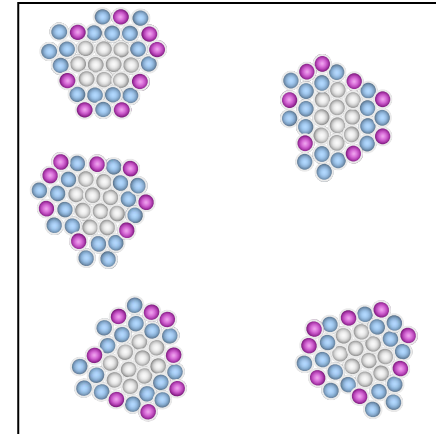
Patterned substrate

Epitaxial growth of two-dimensional alloys

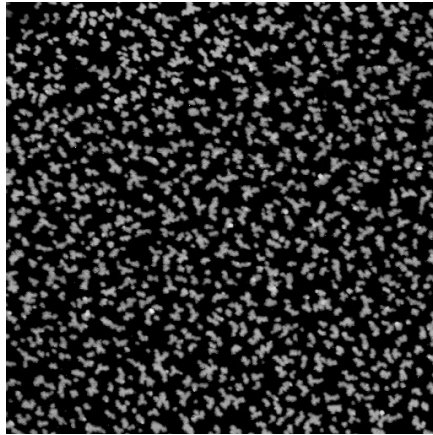
Pre-defined nucleation sites
(seeds) to define the island
density: template



Growth of the alloyed nanostructures
on the template substrate



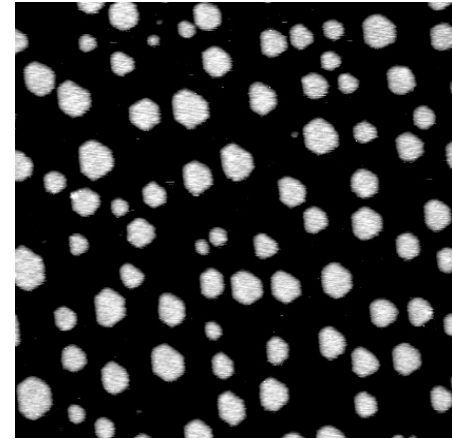
Epitaxial growth of two-dimensional alloys



Pt
 $T_{\text{dep}} = 200\text{K}$
 $\Theta = 0.2 \text{ ML}$

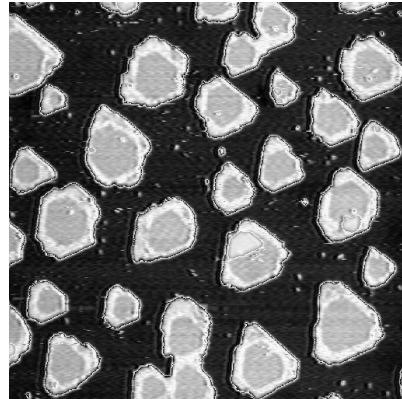


Annealing
to 800 K



10 nm

10 nm



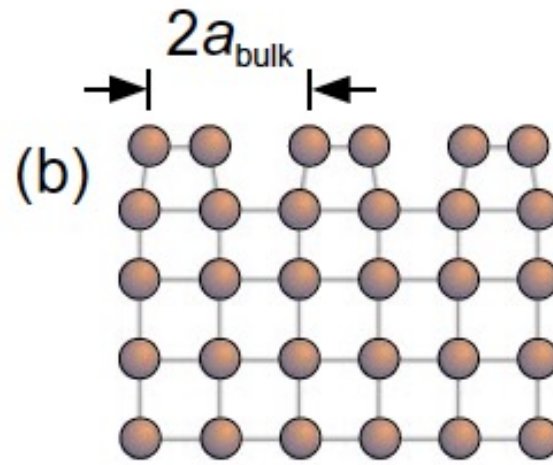
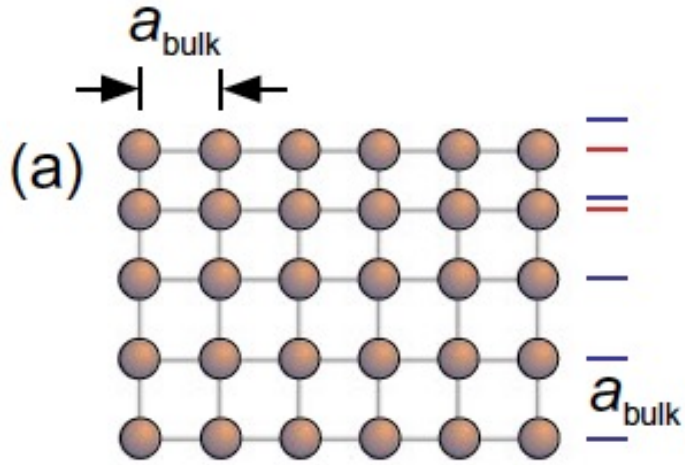
30 nm

$\text{Co}_x\text{Fe}_{1-x}$ decoration

$T_{\text{dep}} = 250\text{K}$

$\Theta = 0.2 \text{ ML}$

Surface relaxation and surface reconstruction



Surface reconstructions

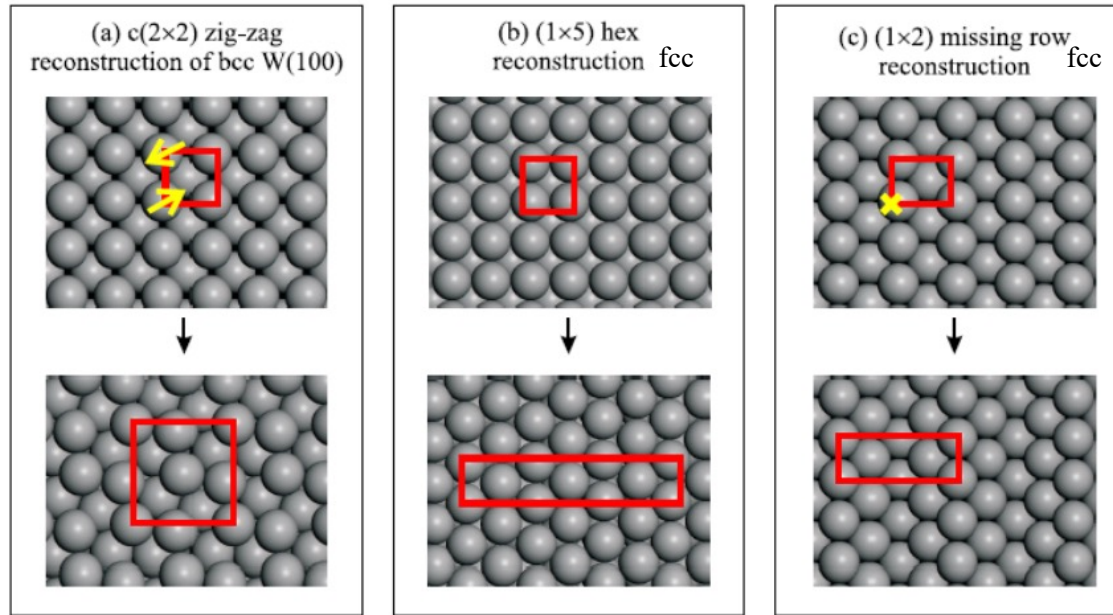
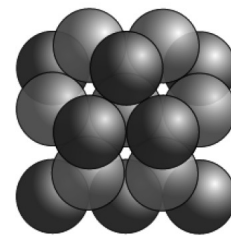
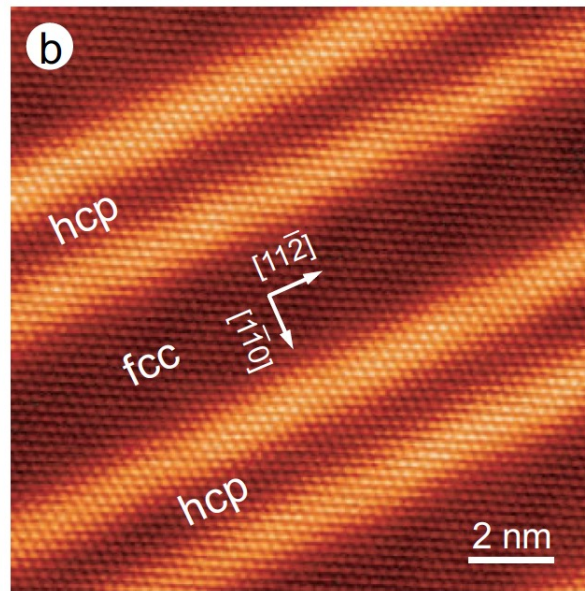
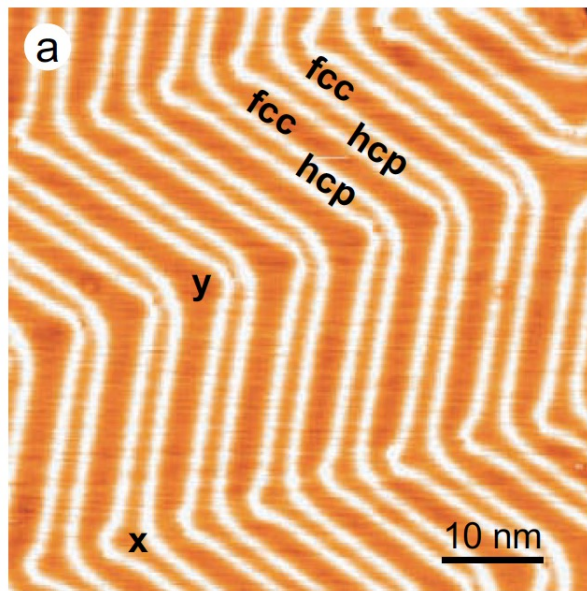


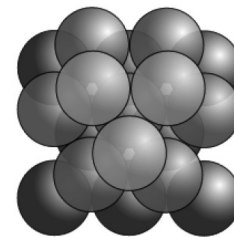
Figure 5.5. - Illustration of three bulk truncated surfaces and typical types of reconstruction that they undergo. (a) depicts the (1×1) to $c(2 \times 2)$ reconstruction of bcc W(100). The arrows indicate the direction in which the top layer W atoms move upon reconstruction. (b) displays an example of the “hex” reconstruction that the late 5d (fcc) transition metals undergo. The specific example is the (1×1) to (1×5) reconstruction of fcc Ir(100). (c) displays the (1×1) to (1×2) “missing row” reconstruction that occurs on the (110) surfaces of the late 5d (fcc) transition metals. The rows of atoms removed by the reconstruction are indicated by the \times at the edge of the unit cell.

Michele Romeo,
PhD Thesis 2015,
Università di Trieste

Au(111): herringbone reconstruction



hcp: ABA



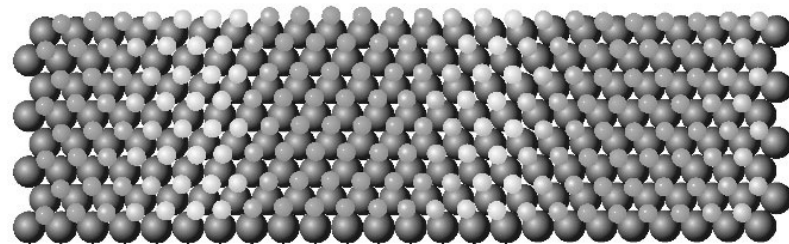
fcc: ABC

Figure 3.1: STM image showing the herringbone reconstructed Au(111) surface. a) Alternating fcc and hcp stacking domains, as well as x- and y-type elbows are visible. b) Atomically resolved STM image, revealing the slightly distorted hexagonal arrangement of the surface atoms together with the domain walls separating fcc and hcp stacking. The interatomic distances along $[11\bar{2}]$ and $[\bar{1}10]$ are 2.88 Å and ≈ 2.75 Å, respectively. (Tunneling parameters: a) $V = -0.7$ V, $I = 0.2$ nA; b) $V = -0.02$ V, $I = 1.3$ nA)

fcc-sites

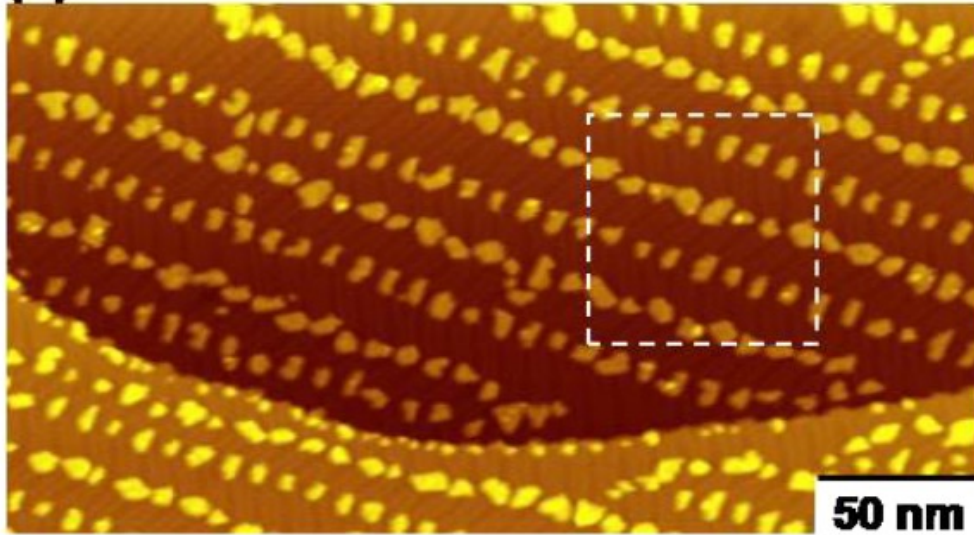
hcp-sites

fcc-sites



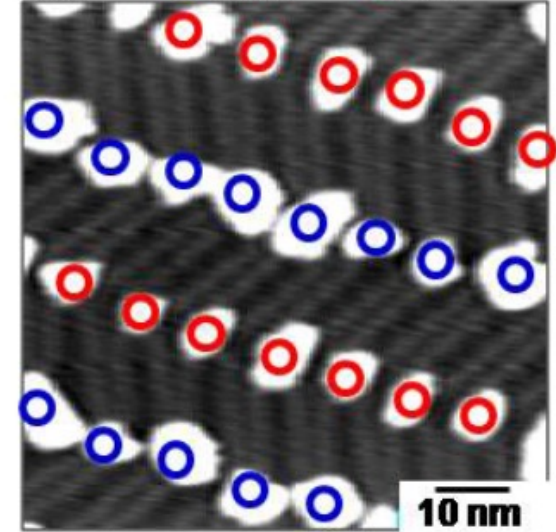
Au(111) herringbone reconstruction - Nucleation

(a) 250 K - 0.18 ML

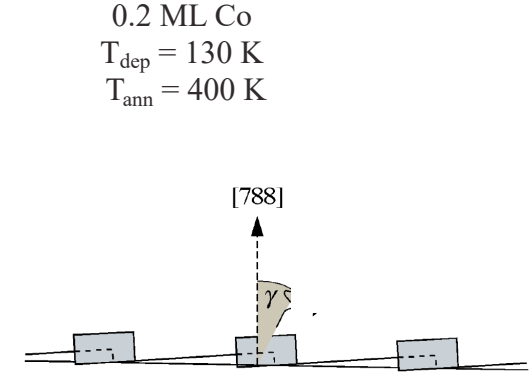
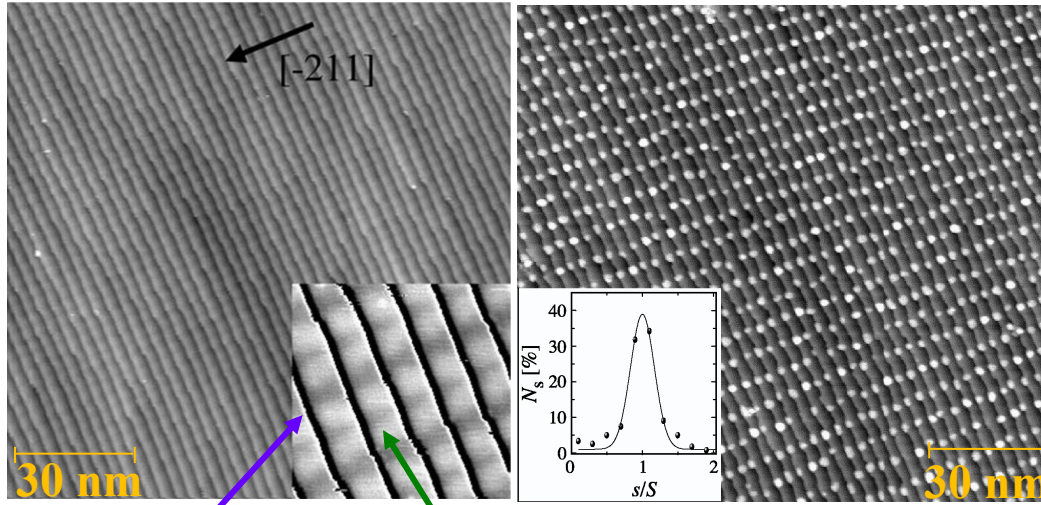


0.18 ML Fe grown at 250 K
islands nucleate at elbows

(b) ○ hcp ○ fcc



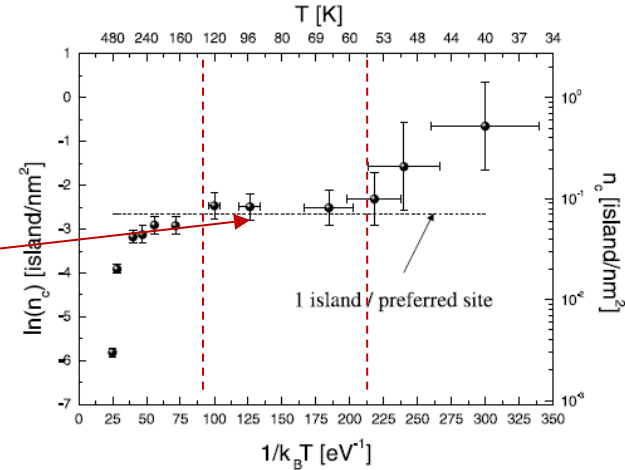
Vicinal Au surfaces: Au(7,8,8)



0.2 ML Co
 $T_{\text{dep}} = 130 \text{ K}$
 $T_{\text{ann}} = 400 \text{ K}$

the **step edges** and the **terrace reconstruction lines**
 confine the **Co adatoms**

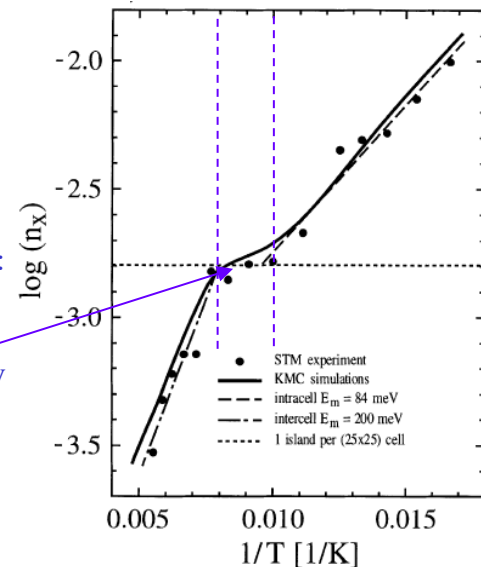
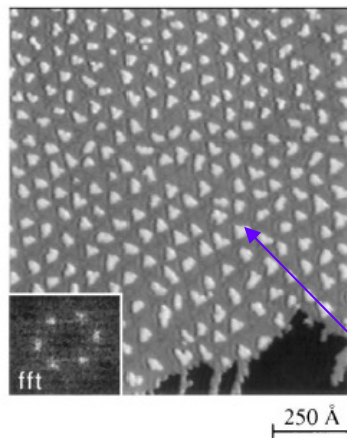
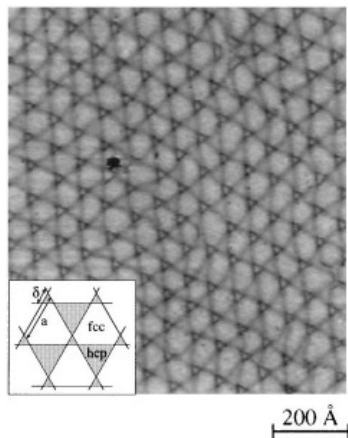
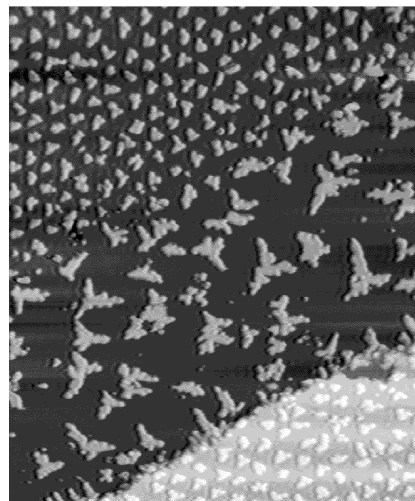
range of T where the island density (n_x) does not change



S. Rohart *et al.* Surf. Sci. **559**, 47 (2004);
 N. Weiss *et al.* Phys. Rev. Lett. **95**, 157204 (2005)

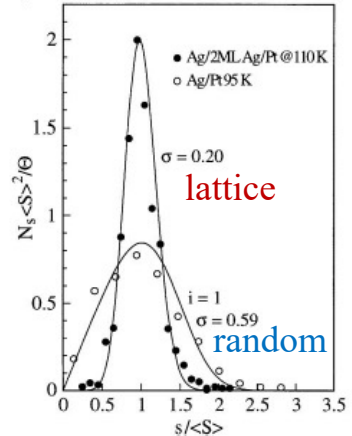
Self assembled nanostructure arrays on patterned substrate

Nucleation of an Ag island superlattice ($T_{dep} = 110$ K) on the dislocation network formed by 2 ML of Ag on Pt(111)

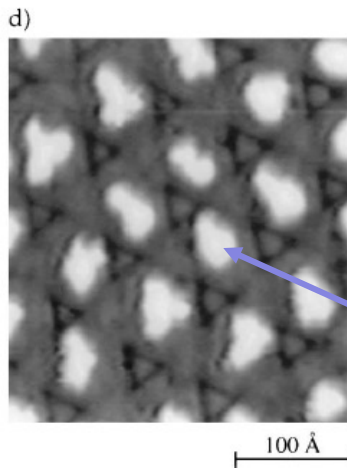


Confinement: range of T where the island density (n_x) does not change

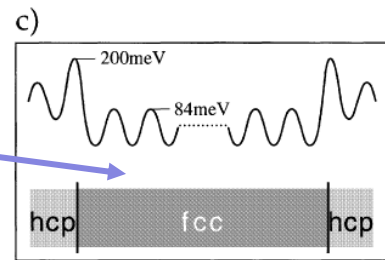
c) Size distribution



Almost monodispersed size distribution thanks to the template effect of the dislocation network



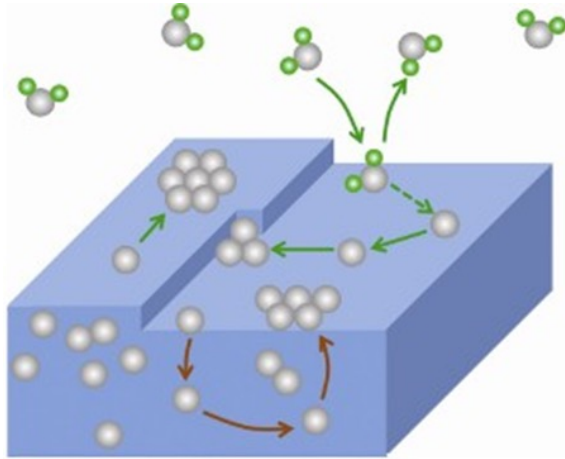
Atoms are confined in the fcc stacking areas



Self assembled nanostructures on graphene

Graphene growth by CVD (chemical vapor deposition)

hydrocarbon flux



- Hydrogen
- Carbon

Hydrocarbon molecules dissociate on the hot surface: H atoms leave the surface while C atoms organize in the honeycomb network of graphene

Ex of hydrocarbons:

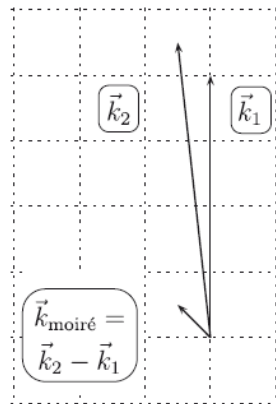
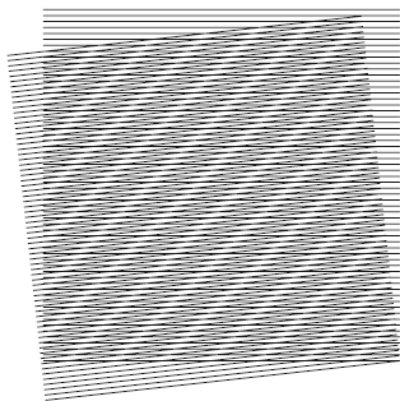
CH_2 → Methylene

C_2H_4 → Ethylene

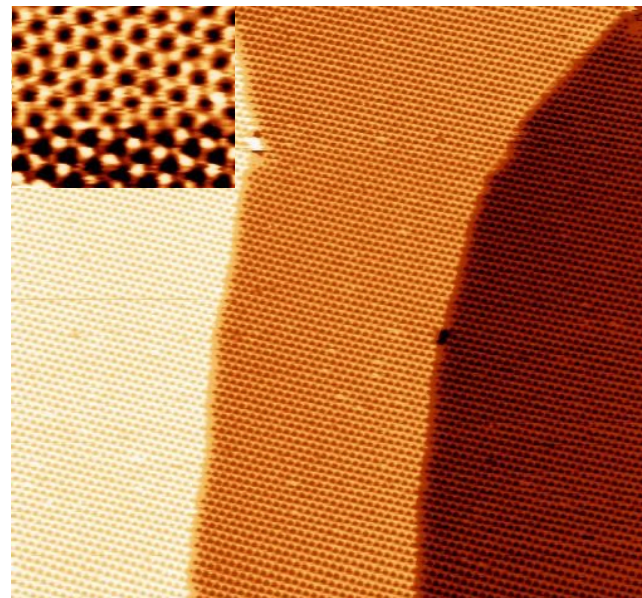
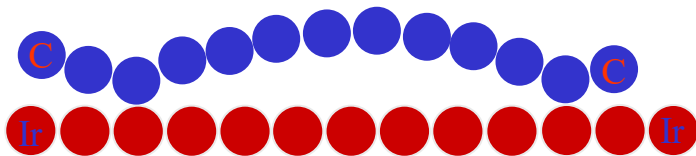
Note: C atoms dissolved in the bulk segregate to the sample surface and also contribute to form graphene

Moiré pattern due to graphene-Ir(111) lattice mismatch

A moiré is a superposition of two lattices generating a third one.



$$a_{\text{Ir}} = 0.27 \text{ nm}$$
$$a_{\text{c}} = 0.245 \text{ nm}$$

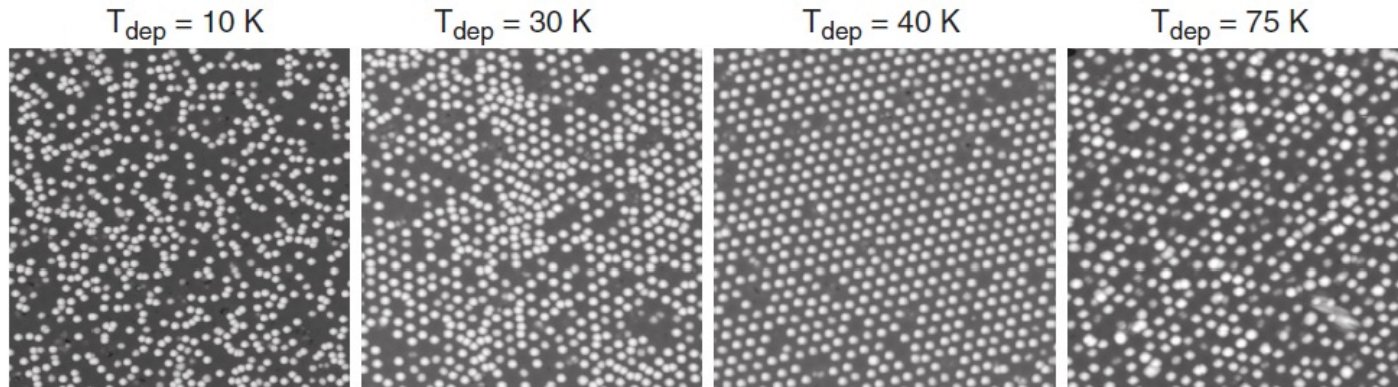
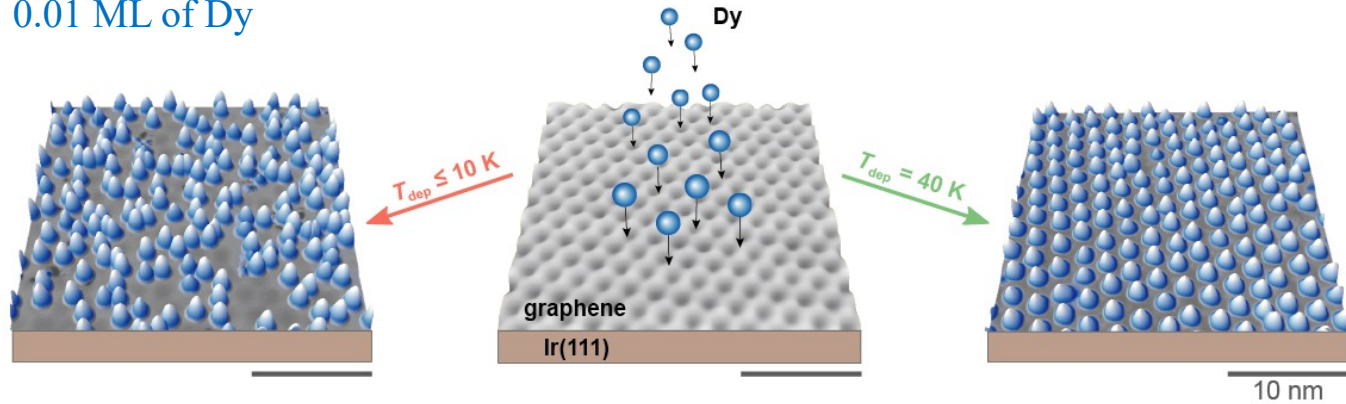


180 x 200 nm²

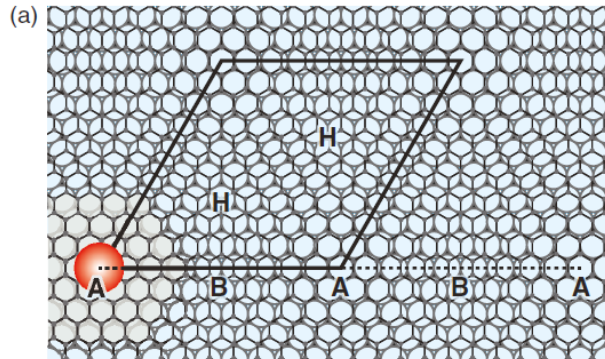
Supercell with (10x10) C atoms
on (9x9) Ir substrate atoms

Superlattice of single atom magnets on graphene

Dy atoms on graphene/Ir(111)
0.01 ML of Dy



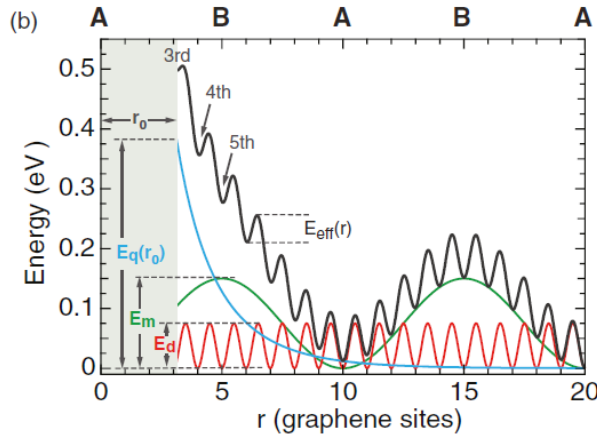
Diffusion energy landscape



Moiré with (10×10) graphene unit cells on (9×9) Ir(111) atoms.

Stacking areas: (A) atop, (B) bridge, and (H) hollow.

Rare-earth atom (red) together with its direct impingement area (gray).



1D diffusion energy profile for a second rare-earth atom resulting from the superposition of:

- 1) atomic corrugation E_d
- 2) moiré corrugation E_m of graphene
- 3) Coulomb repulsion E_q

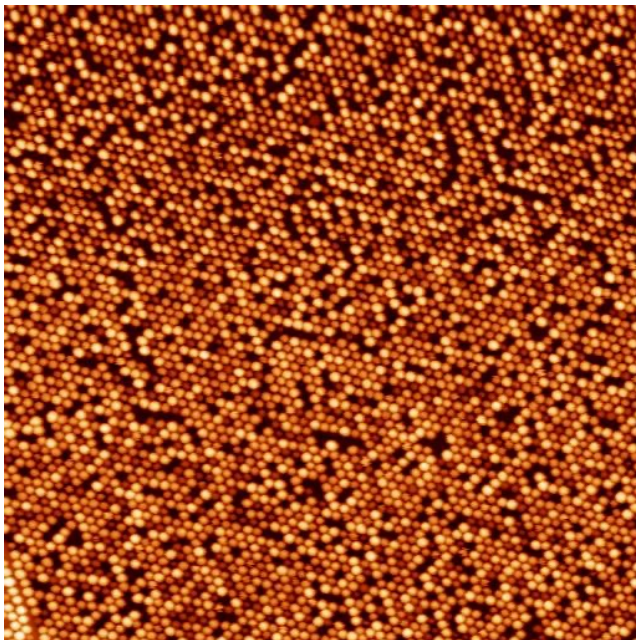
$$E_q(r) = \frac{1}{4\pi\epsilon_0} \frac{q^2}{r} \exp\left(-\frac{r}{r_0}\right)$$

q is the charge transferred from the rare-earth to graphene

Self assembled core-shell nanostructure arrays on graphene/Ir(111)

Ir island

Ir deposition: T=375 K



150 x 150 nm²

graphene

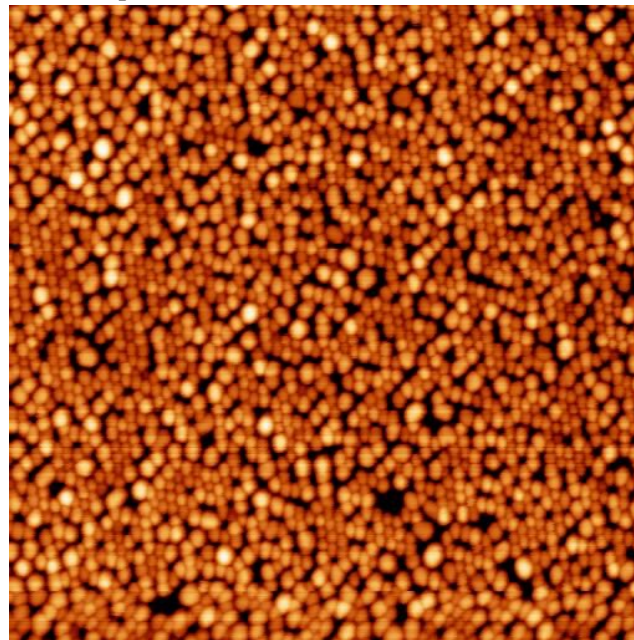


Ir(111)

Ir-core Co-shell islands

Ir deposition: T=375 K

Co deposition: 1 ML, T=300 K



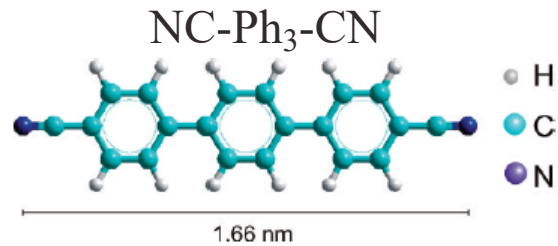
150 x 150 nm²

Ir-core
Co-shell

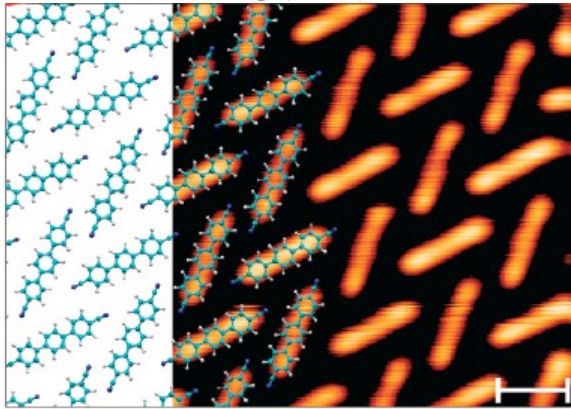


Ir(111)

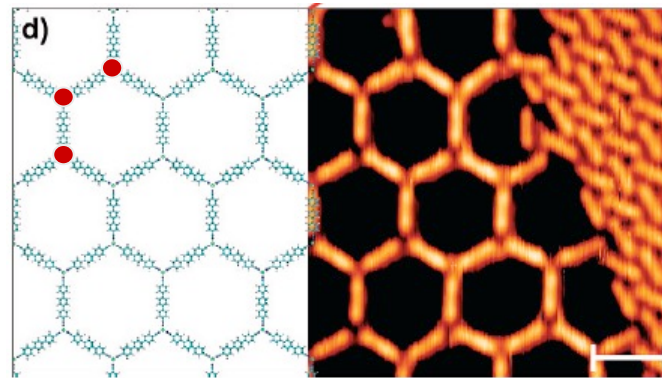
Molecular and metal-organic networks



On Ag(111)



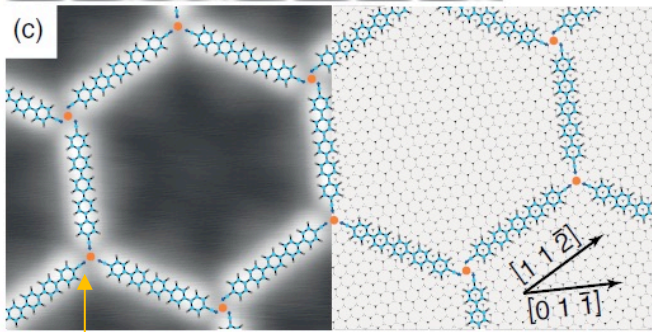
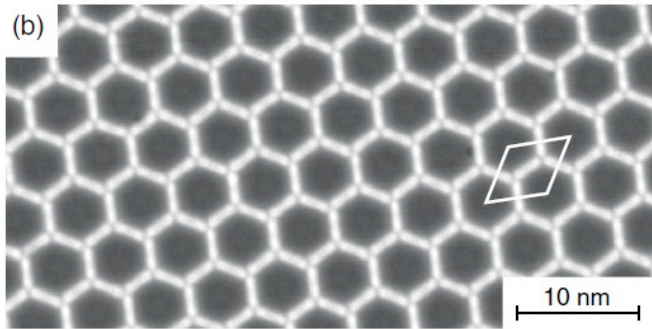
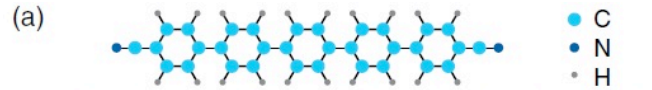
● Cobalt



Co atoms added at room temperature coordinate the molecules in a 3-fold coordinated motif

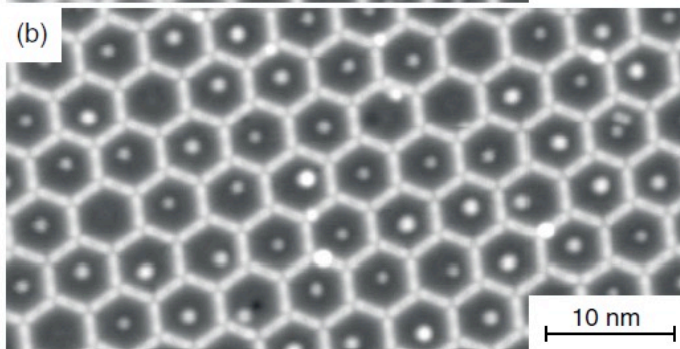
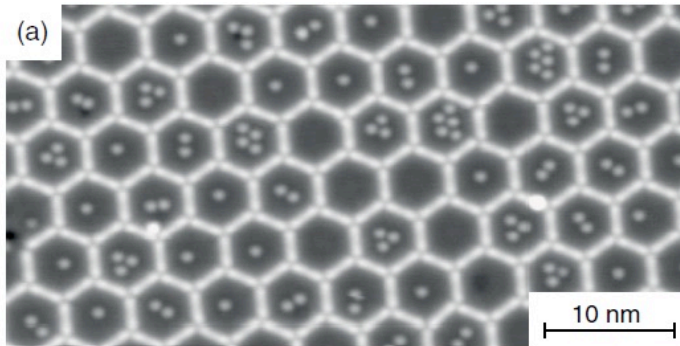
Cluster superlattice in a metal-organic quantum box network

Metal organic quantum box network on Cu(111)

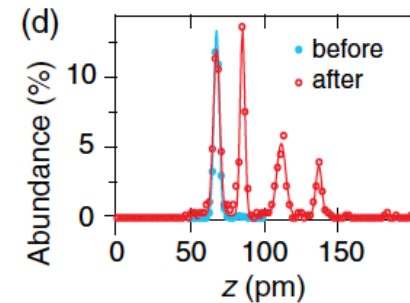
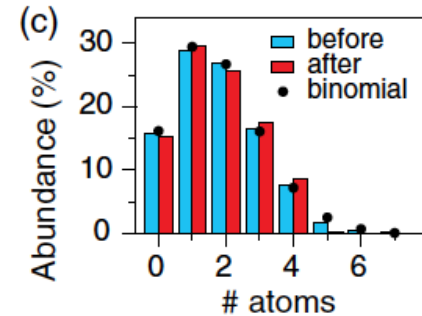


Cu atoms

a) Fe deposition at $T = 10\text{K}$



b) cluster formation after annealing to $T_{\text{ann}} = 18\text{K}$



Superlattices: density vs blocking T

System	density	T _b
Co/Au(11,12,12)	15 T _{dot} /in ²	75 K
Fe/Co/Au(11,12,12)	15 T _{dot} /in ²	105 K
Co/Au(788)	26 T _{dot} /in ²	50 K
Co/GdAu ₂ /Au(111)	52 T _{dot} /in ²	< 90 K
Fe/NC-Ph ₃ -CN/Cu(111)	90 T _{dot} /in ²	?
Fe/Al ₂ O ₃ /Ni ₃ Al(111)	92 T _{dot} /in ²	?
Co/Ir/graphene/Ir(111)	116 T _{dot} /in ²	< 50 K