

## Intelligent Agents

### Paper Exercise: Uncertainty and Negotiation Ungraded

**Question 1:** Consider the game in Figure 1. Let  $\alpha$  and  $\beta$  be the uncertain types of agents 1 and 2; they characterize the payoff for playing action A to that agent.

		Agent 2	
		A	B
Agent 1	A	$\alpha, \beta$	$\alpha, 1$
	B	$1, \beta$	$1, 1$

Figure 1. An uncertain game. Each of two players chooses either action A or B. Payoffs  $\alpha$  and  $\beta$  are uncertain.

Consider first that for both agents, the type is distributed among the 2 values [0.5, 2.0] with equal probability, and that this distribution is common knowledge.

Derive the ex-ante Bayes-Nash equilibria of the game. Does the game have an ex-post Bayes-Nash equilibrium?

Next, consider that agent 1 knows its own type  $\alpha=0.5$ . What are the ex-interim Bayes-Nash equilibria?

Consider another variant where the type is distributed among [2,3] with equal probability. Now does the game have an ex-post Bayes-Nash equilibrium?

**Question 2:** Consider the game in Figure 2. What are the equilibria of this game? What is the Nash Bargaining solution for the case of non-transferable utility?

		Player B	
		0	1
Player A	0	7,8	3,15
	1	10,3	5,5

Figure 2. A game that can use cooperation.

**Question 3:** For the game in Figure 2, consider a version where utility can be transferred from one agent to another. How does this change the space of possible bargaining solutions? What is the new Nash Bargaining solution?

**Question 4:** For the game in Figure 2, what is space of utilities achieved by co-related strategies? Suppose, the set of feasible utilities in the bargaining game is the space of utilities obtained by co-related strategies, what is Nash Bargaining solution? What co-related strategy can implement this? Is this co-related equilibrium?

**Question 5:** How would you modify the Nash bargaining scheme to so that each agent has a different importance? Hint: consider that agents act for a group of agents and that importance is proportional to the size of the group.