

**Computational geomechanics  
applications etc.**

**EPFL**



GeoEnergyLab

# What we did not cover

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- Other multi-physics coupling, notably:
  - Thermo-poro-elasticity (THM)
    - Thermal pressurization (heat induced pp increase), heat conduction / convection (hydro-thermal problems) ...
    - Note that mechanics do not influence thermal effects (TH->M, but no M->T)
  - Chemo-poro...
    - Most of the time chemical reactions → change in mechanical respons: C-> M (not M-> C)
    - Notable exception: pressure solution
- Dynamics
  - Dynamic liquefaction, waves and poroelasticity (squirt flow) etc.
- Material rate dependent effects
  - Viscoplasticity etc.
- Fracture growth

# Natural hazards

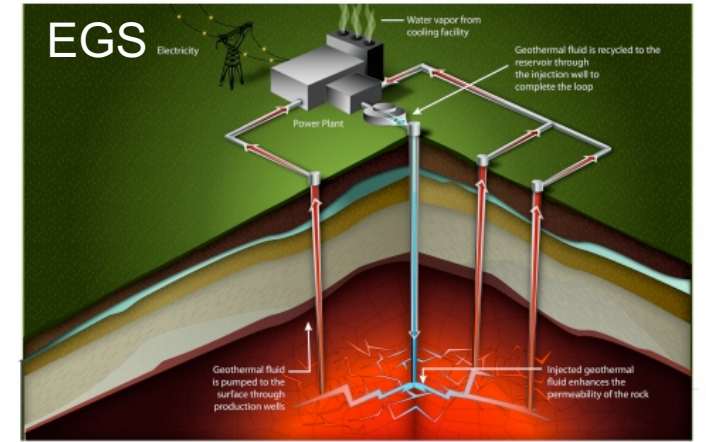


[blogs.agu.org/landslideblog/]

# Oil & Gas

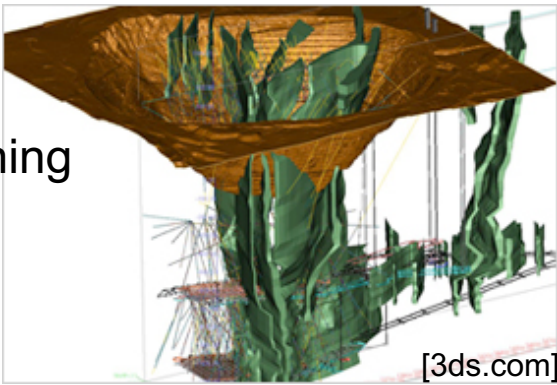


[pubs.spe.org/en/jpt]

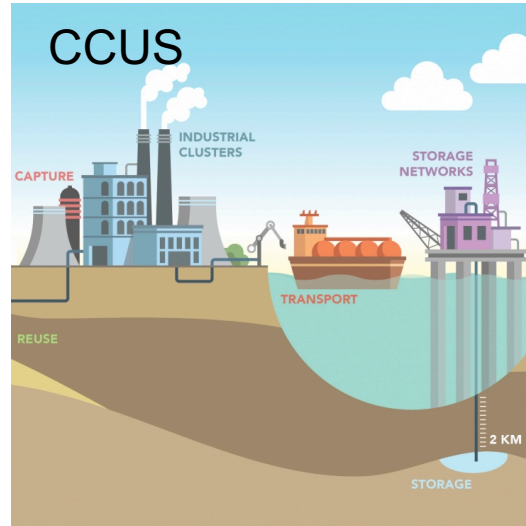


[DOE, Geothermal Technologies Program]

# Mining



[3ds.com]

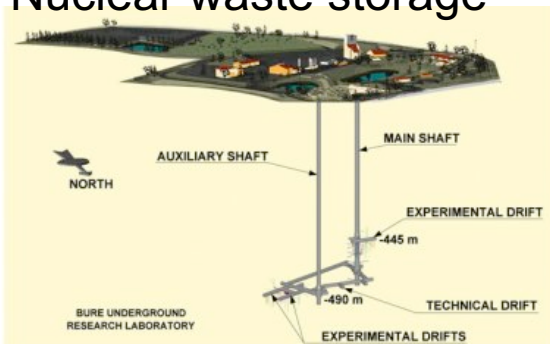


[alignccus.eu]

# Groundwater

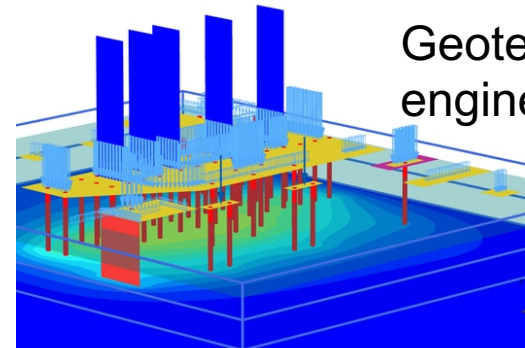


# Nuclear waste storage

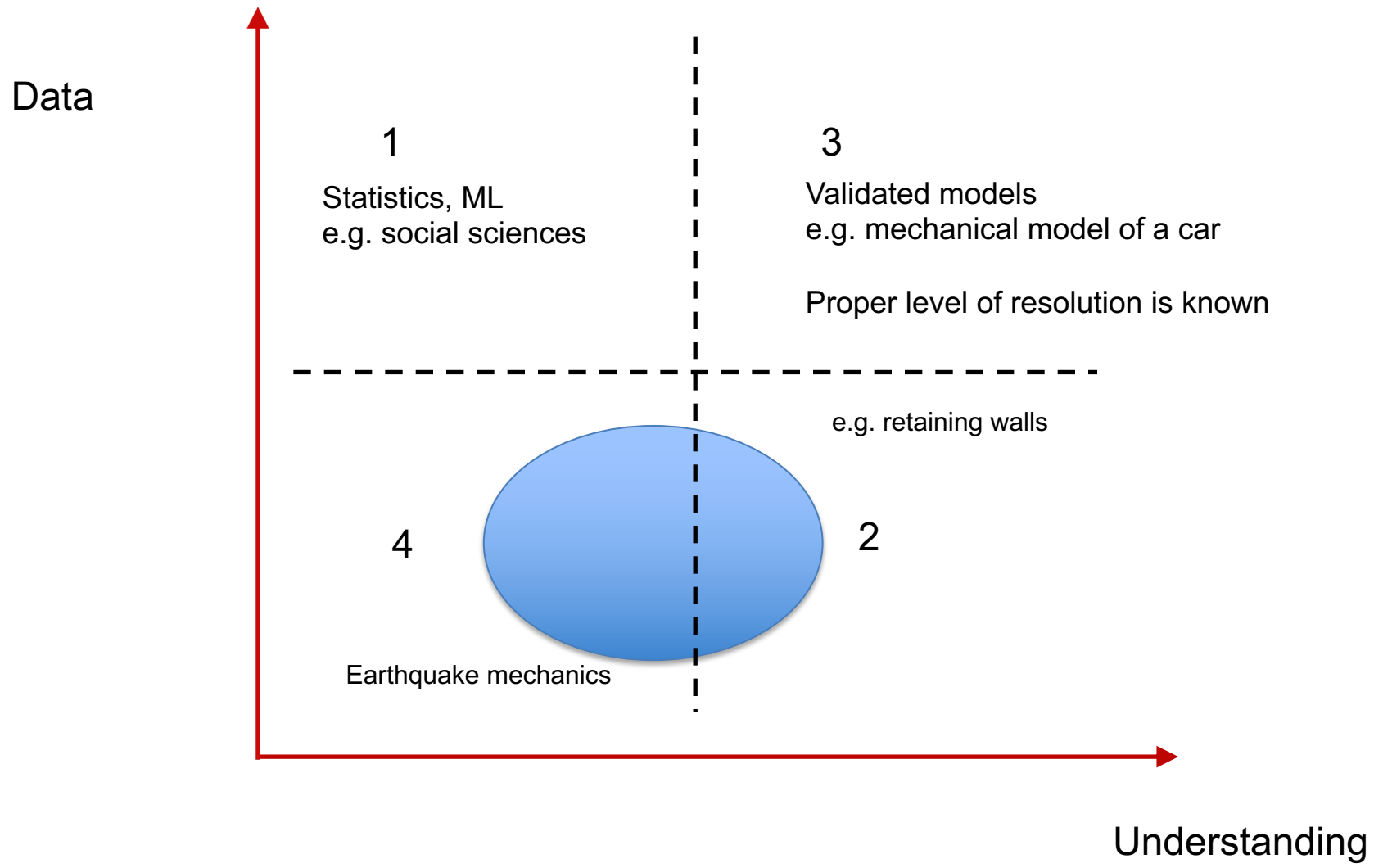


[ANDRA]

# Geotechnical engineering



[cmwgeosciences.com]



# Model verification vs validation

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- Verification

- Ensure that the numerical tool **correctly/accurately** solve the equations it is supposed to solve
  - E.g. check a FEM elastic model against Boussinesq analytical solution for a circularly loaded area
  - Same for more complex equations: -> benchmarking between different numerical codes.

- Validation

- Ensure that the numerical model **correctly/accurately** reproduce the physical phenomena observed
  - E.g. comparison between the prediction of a model and a lab experiment WITHOUT FITTING the model parameters
  - E.g. comparison between the prediction of a model and a field experiment, allowing a reasonable adjustment of the model parameters

- Validation without verification is the road to disaster

# Modeling in geomechanics

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- “ A model is a simplification of reality rather than an imitation of reality. It is an intellectual tool that has to be designed or chosen for a specific task.”
- “The design of a model should be driven by the questions that the model is supposed to answer rather than the details of the system that is being modelled”
  - Over-complexification of models do not lead to better predictability
- “... appropriate to build a few very simple models rather than one complex model; the simple models would either relate to different aspects of the problem, or else address the same questions from different perspectives”
- “Instead of trying to validate a model, one should aim at gaining confidence in it and modify it as data arrives. “
- “Purpose of modeling data limited problems is to gain confidence and explore potential trade-offs and alternative, rather than to make absolute predictions”

[Starfield & Cundall, 1998 – towards a methodology for rock mechanics modeling]

# In practice

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- Why modeling ? What is/are the question/s ?
- Use a model early – do not delay until receiving field data
- Look at the mechanics of the problem – perform dimensional analysis and scaling
- Think of an experiment to decipher between possible mechanisms – this can be numerical experiments
- Start simple, and complexify only when required (when the simple model is invalidated)
- If the model has weaknesses that can not be remedy, make a series of simulations to bracket the true case
- Once simple models have been mastered, complexify slowly to investigate the effects previously neglected

“There is a dialectic between geological detail and engineering understanding”

# Commercial Tools

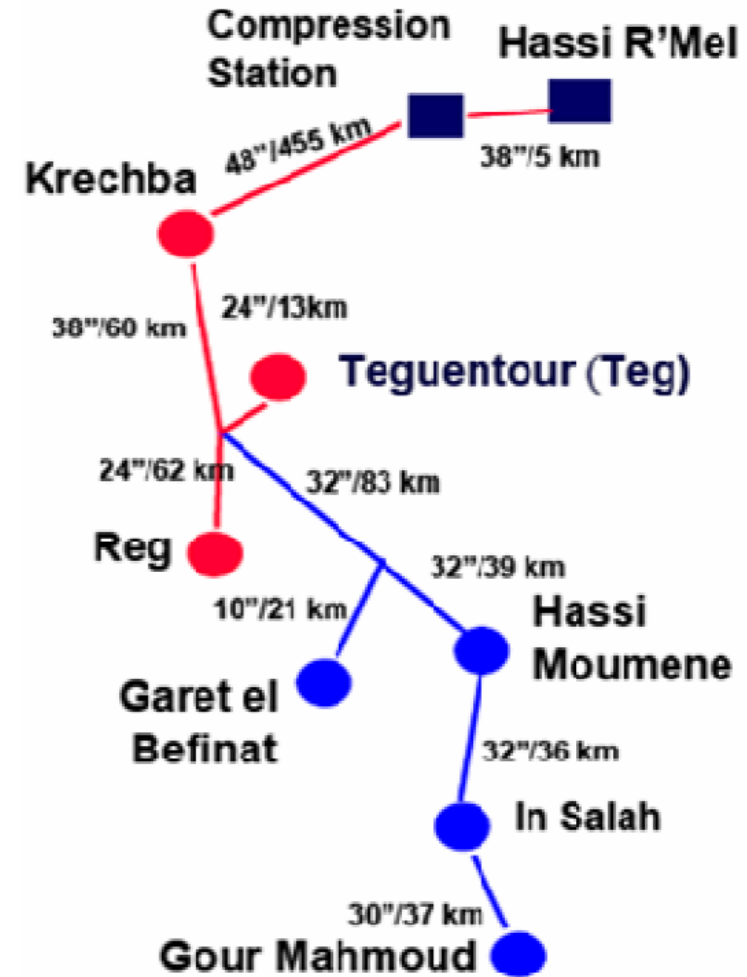
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- Itasca C.G.
  - FLAC 2D / 3D (THM) – explicit FV code – shine for very non-linear problems (elastoplastic)
  - DEM codes: Udec, PFC ...
  - Mining, nuclear waste, O&G
- Plaxis
  - 2D/3D – (T)(H)M – elasto-plastic
  - Geotech.
- RS2/RS3 (RocScience)
  - FE (H)M - elasto plastic
- Optum
  - G2/G3 – (H)M – elasto-plastic, limit analysis
- ELFEN (RockField)
- Abaqus (DS), ANSYS



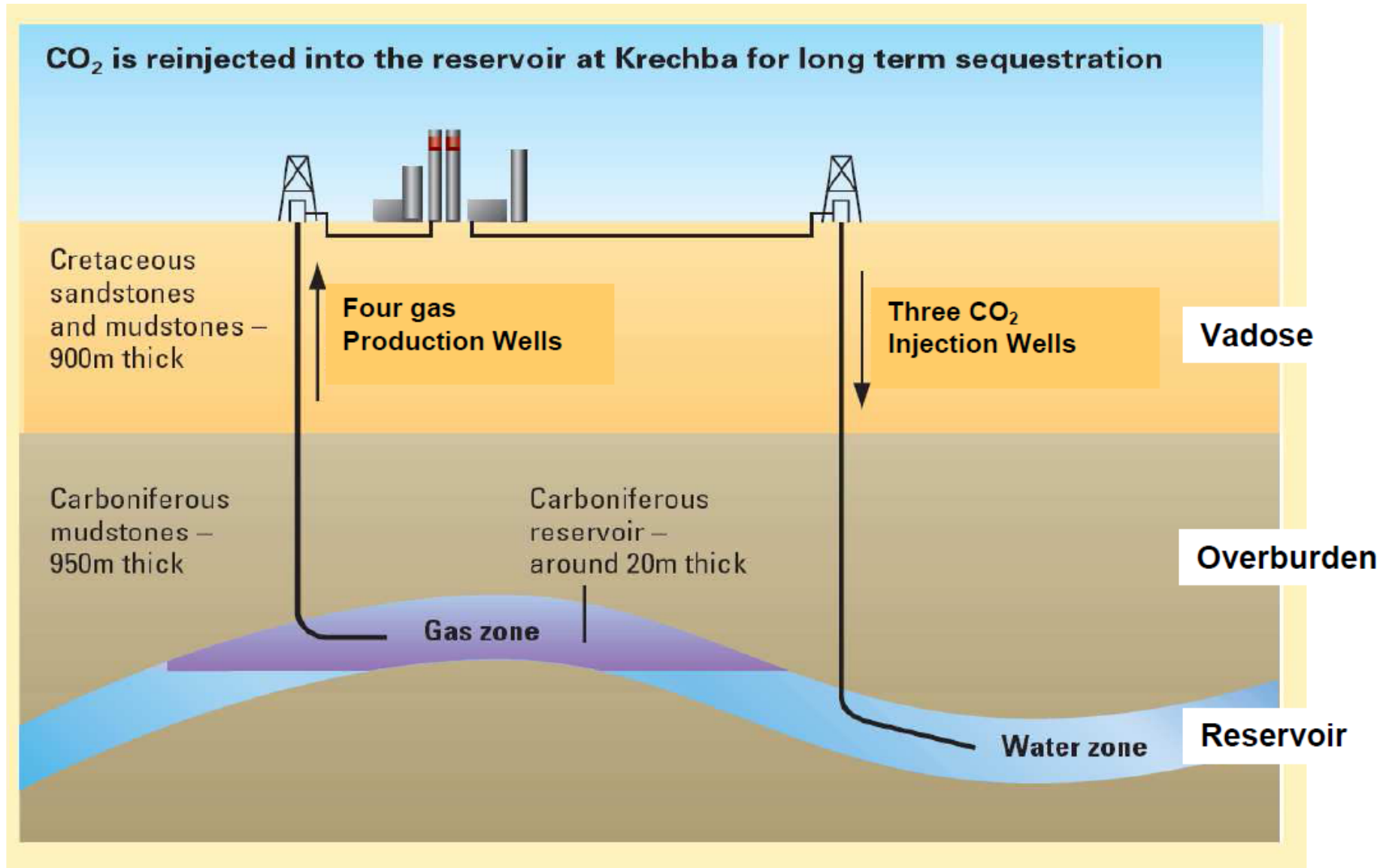
**AN EXAMPLE**

# In Salah Gas (ISG) Project

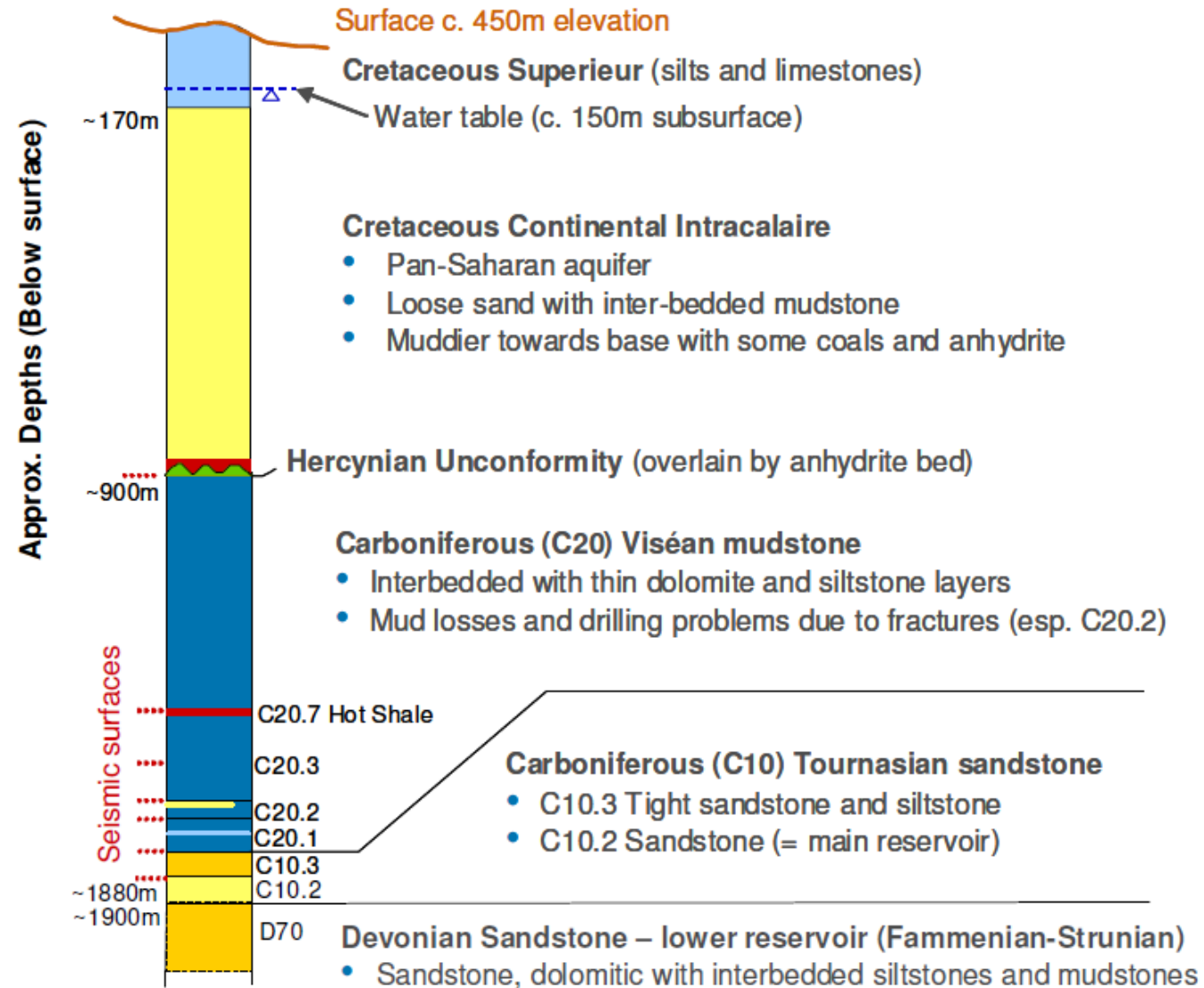


Schematic of ISG  
(Phase 1 is shown in red; phase 2 in blue)

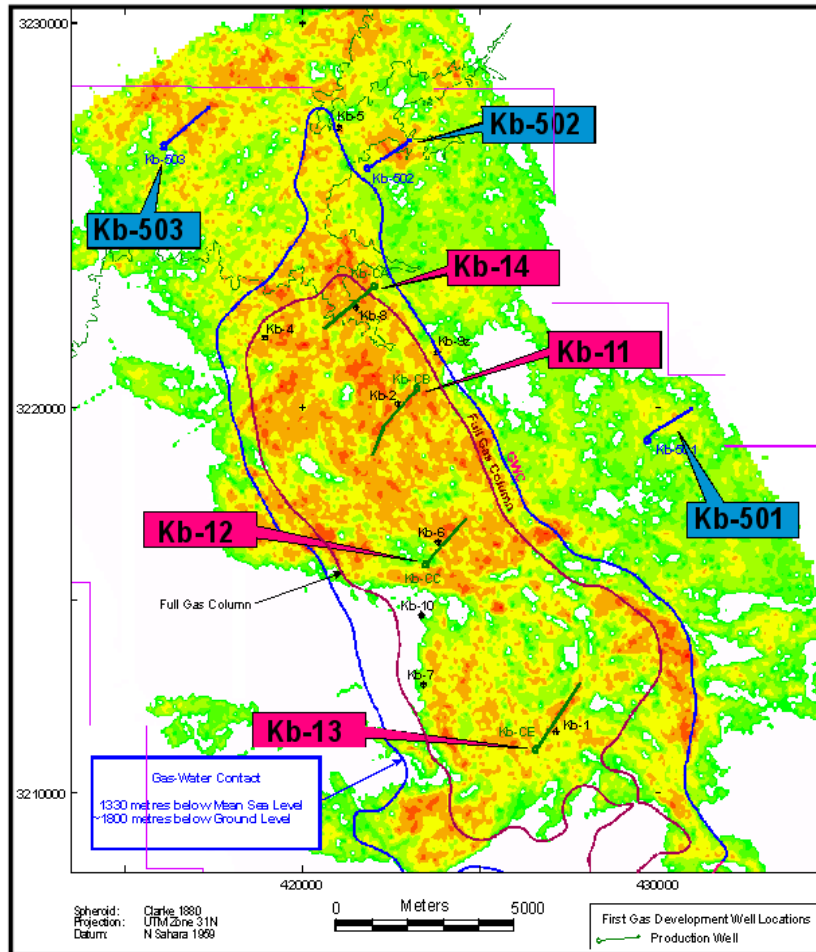
# ISG Schematics



# Krechba Stratigraphic Structure

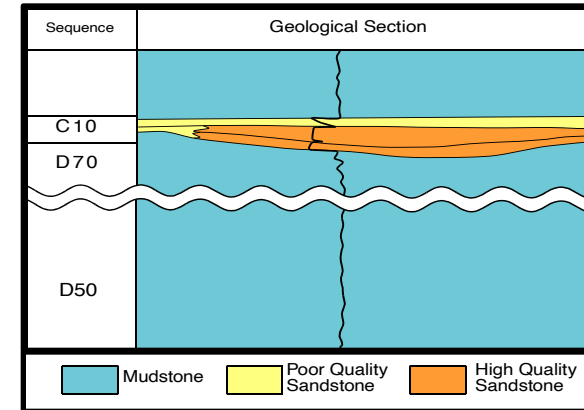


# The In Salah Field Layout



Gas Injectors

Gas Producers



## C10.2 Reservoir Quality

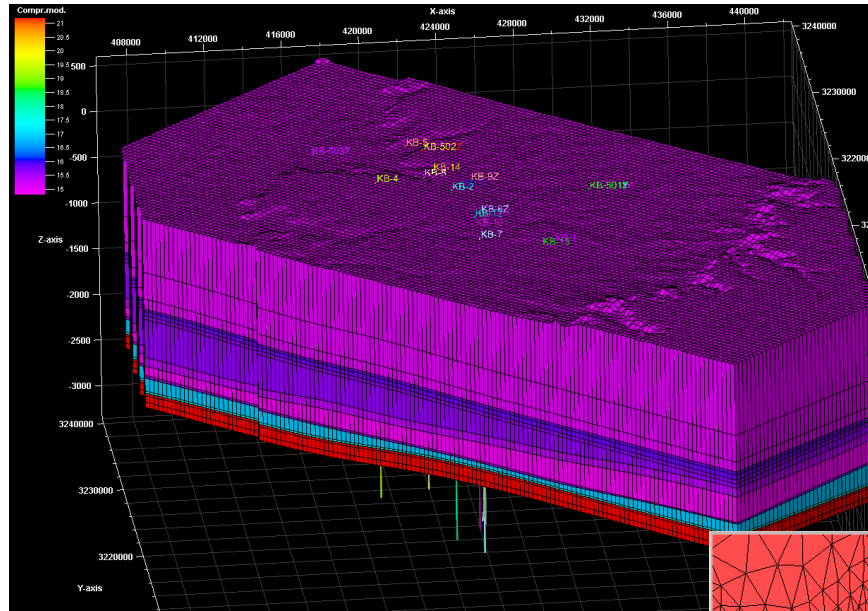
- Avg. porosities range 13 – 20%
- Permeability highly variable - average around 10 mD

# Background

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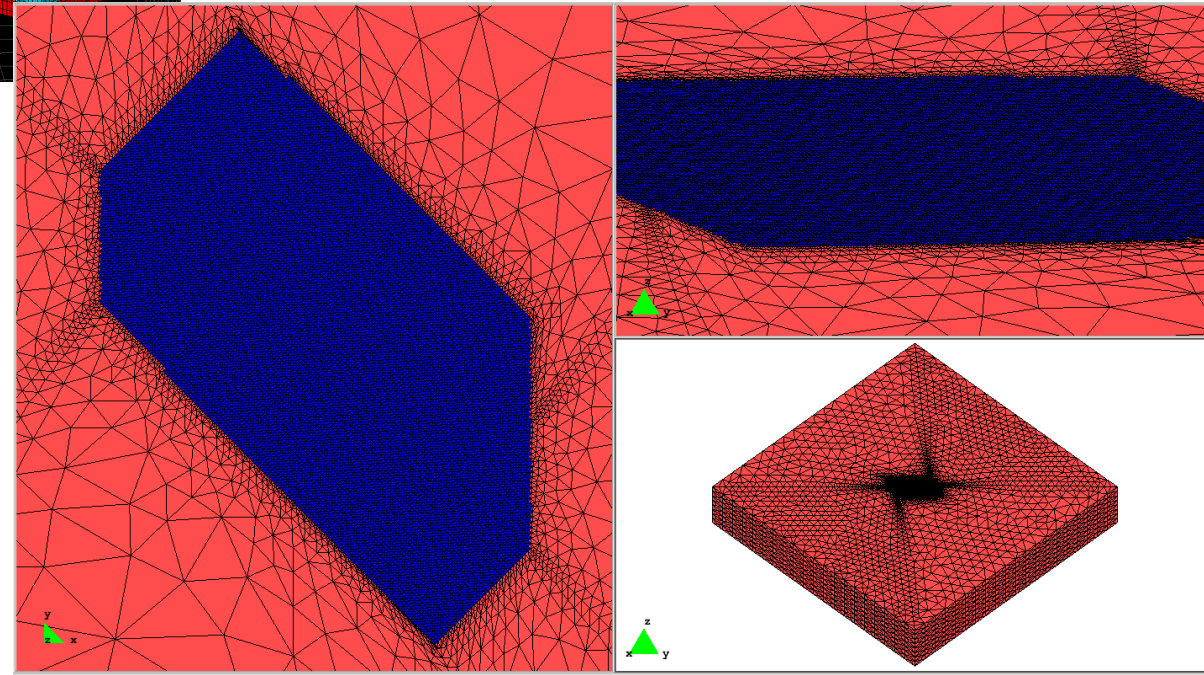
- Krechba is currently described as a fractured and faulted field.
- Fracture:  
Open fracture network along NW-SE.  
Extended to ~1000m TVDSS (lack of data elsewhere).
- Fault: Reverse type  
1 km long to 9 km long. Throw ranging from 10 m to 40 m.
- Only the fracture network is taken into account: fault is not yet taken into account in the geological model.
- The whole field is assumed to be fractured the same (density) as around the well (FMI study, see next).
- BorStress results:  
Stress ratio  $Q = 1.1$ ,  $S_v$  is the intermediate principal stress. Strike-Slip regime  
 $AZ(SH_{max}) = 135$  degree from North (NW-SE).

# 3D Geomechanical Model

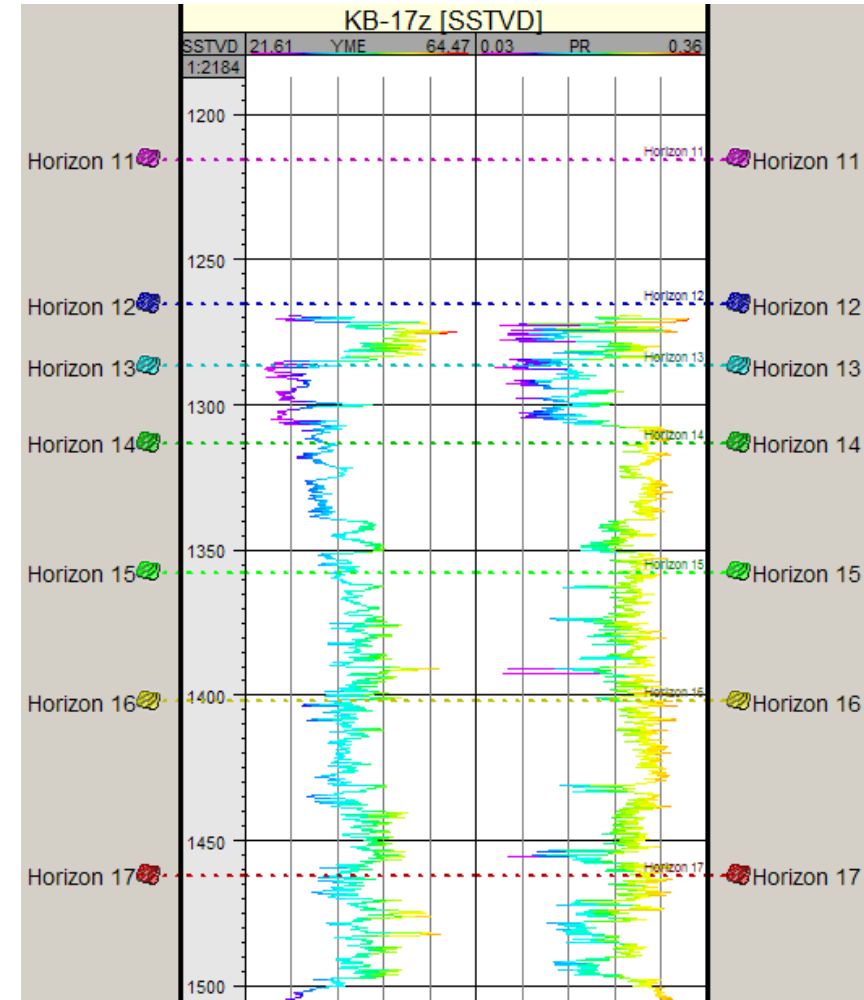
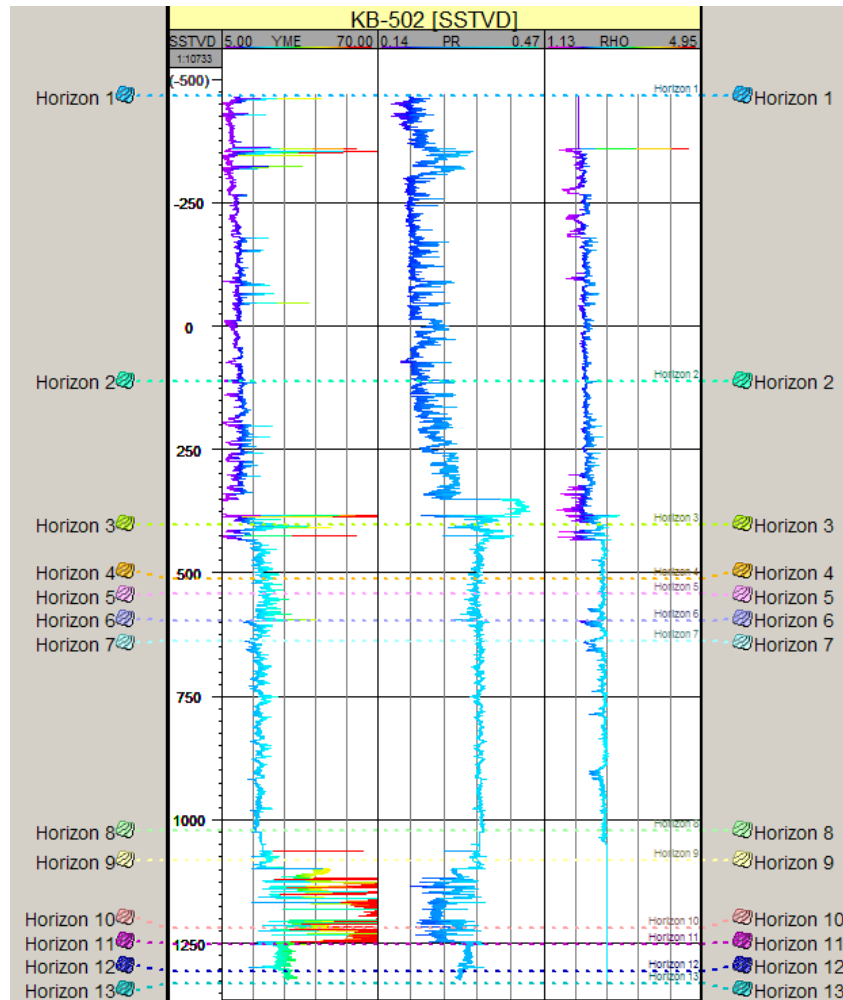


- Petrel model covers 36km by 50km
- Grid size in reservoir: 327m\*289m\*25m
- Embedded model used in Visage covers 285km by 285km  
1,128,191 elements and 195,757 nodes

- Central part corresponds to the Petrel model
- Properties are constant per layer
- Embedding with unstructured tetrahedral mesh

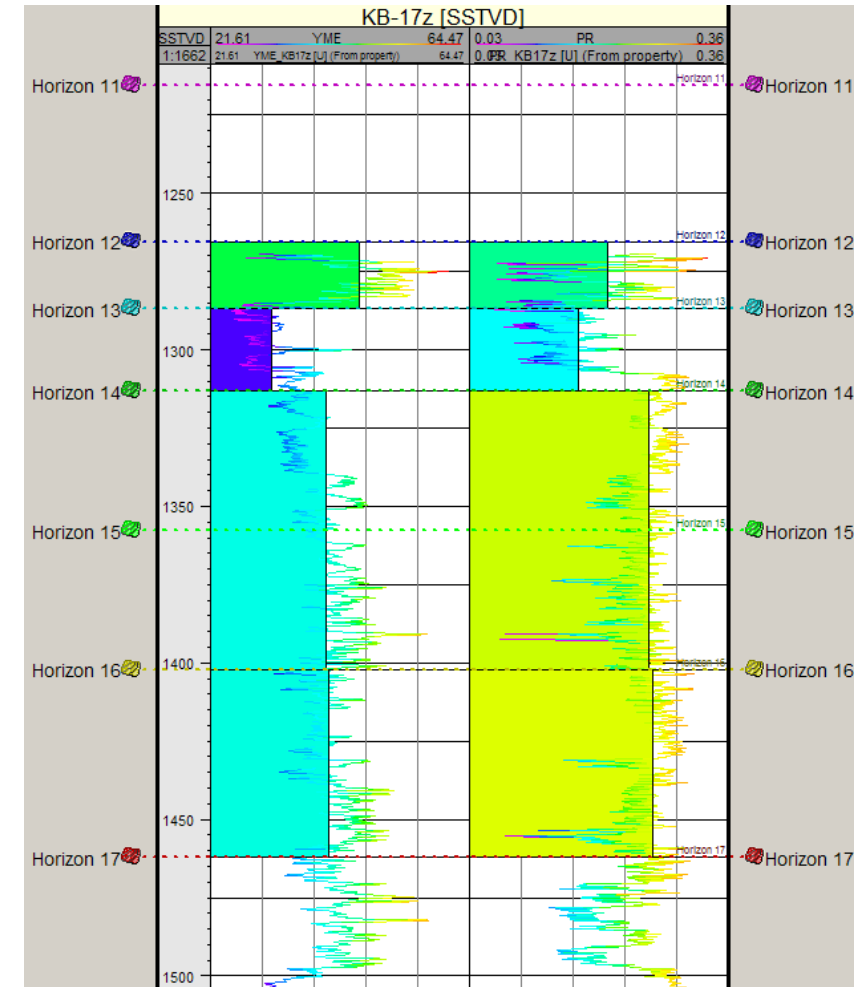
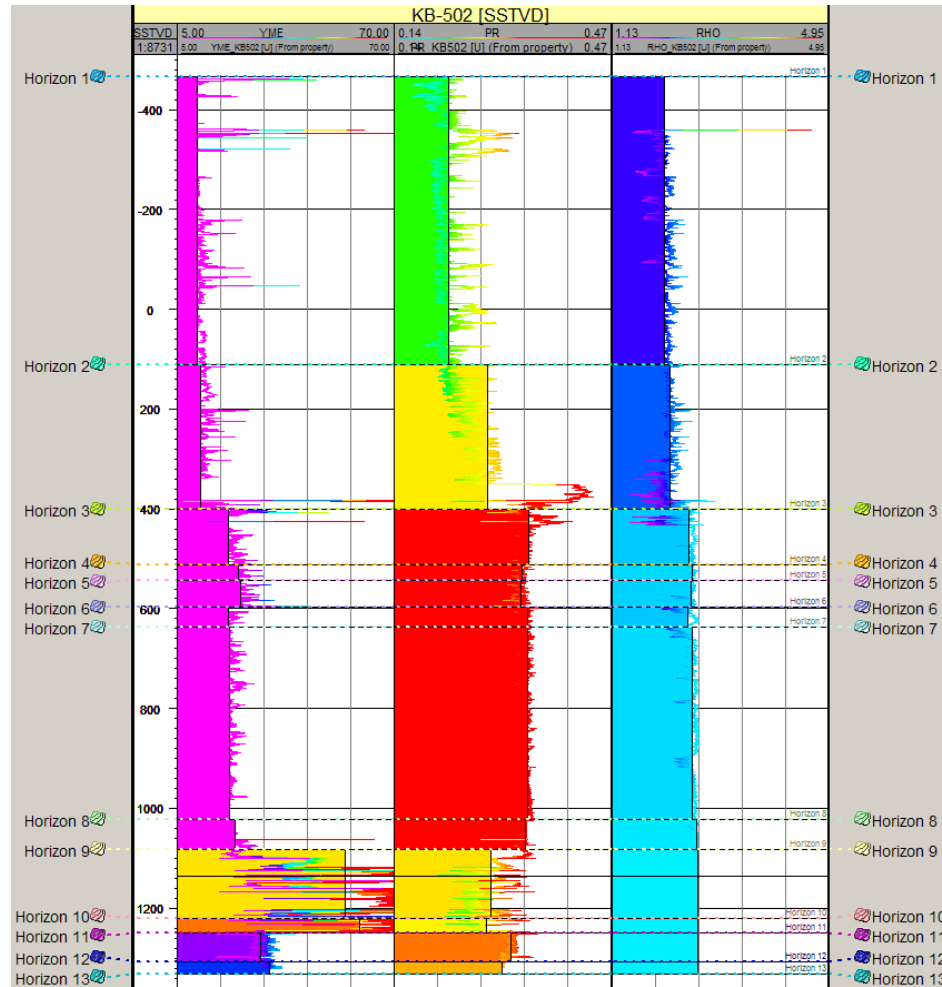


# Rock Properties Upscaled from Sonic Logs





# Rock Properties layer average from Sonic Logs

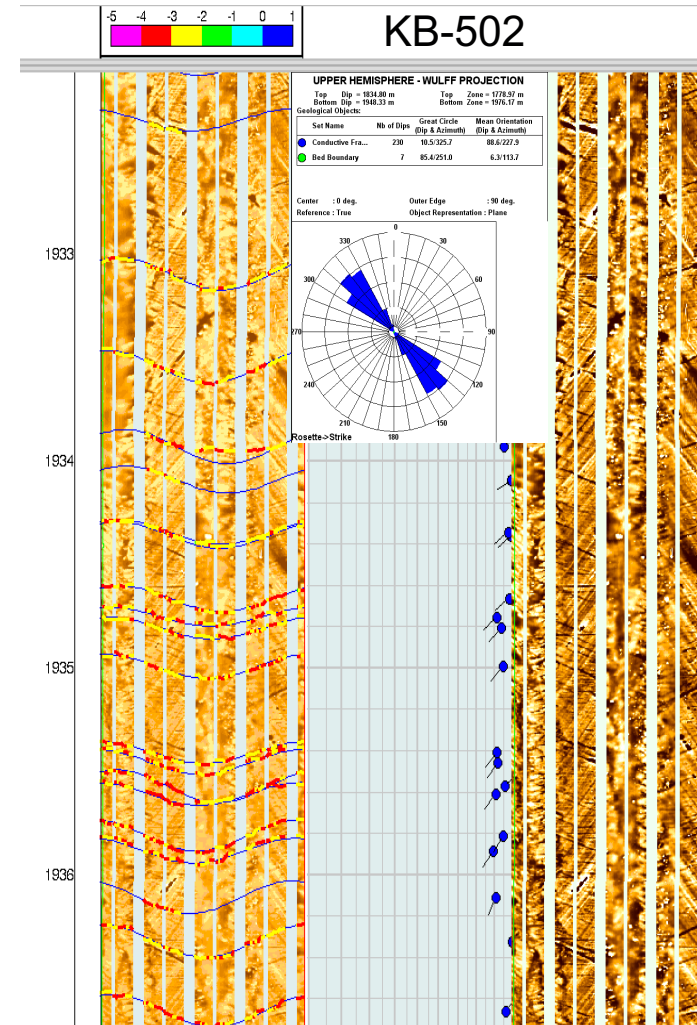
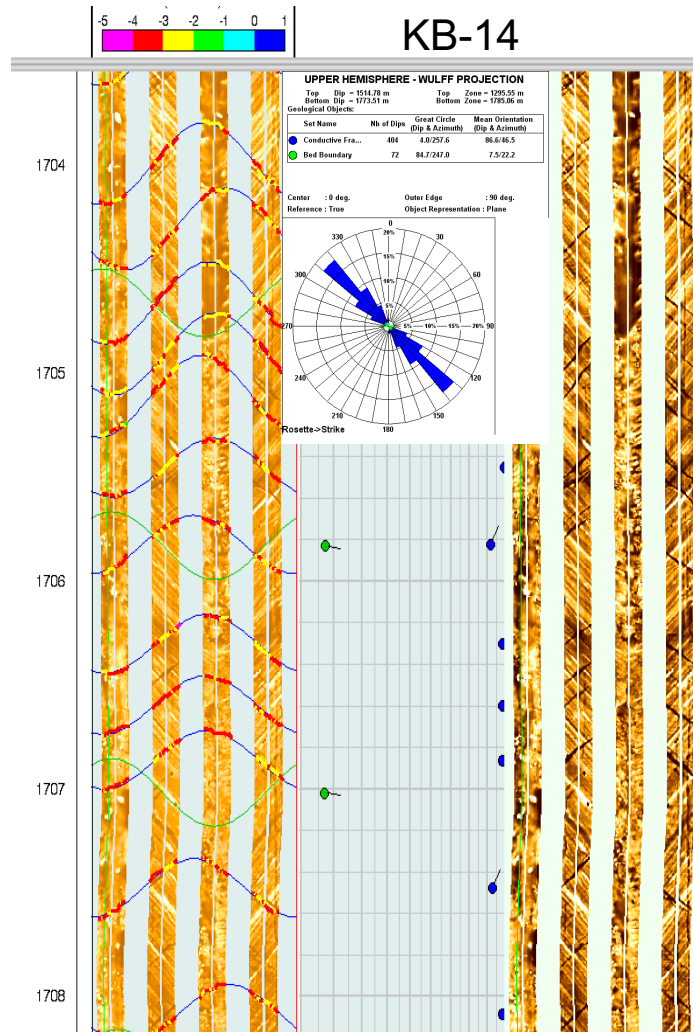


# Layering and Intact Properties

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Description	Zone ID	Thickness (m)	YME (GPa)	PR	RHO (g/cc)	BIOT
Top (ground surface)	1	658	11.1	0.223	2.06	1
New Intermediate zone	2	290	11.9	0.283	2.16	1
New Intermediate zone	3	110	20.3	0.345	2.48	1
Hercynian Unconformity +40	4	27	23.5	0.336	2.55	1
Hercynian Unconformity	5	41	24.0	0.334	2.52	1
Hercynian Unconformity -40	6	40	20.2	0.344	2.48	1
New Intermediate zone	7	306	20.6	0.345	2.56	1
End of Fracture	8	75	22.5	0.340	2.62	1
Hot Shale	9	161	30.0	0.290	2.65	1
New Intermediate zone	10	24	30.0	0.280	2.65	1
C20-2 (Cap Rock)	11	106	30.0	0.320	2.65	1
C10-3 (Tight Reservoir)	12	23	32.6	0.300	2.47	1
C10-2 (Injection zone)	13	27	32.0	0.300	2.51	1
Underburden (new)	14	45	40.0	0.257	2.51	1
Underburden (new)	15	45	40.0	0.257	2.51	1
Underburden (new)	16	60	40.0	0.257	2.51	1

# Fracture Study

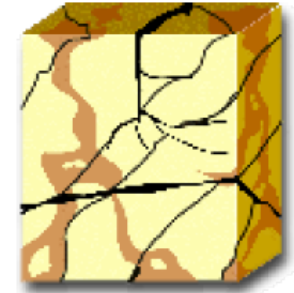


# Effect of Fractures at grid scale

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Estimate the Grid-scale (dual porosity medium) properties from:

- Matrix poroelastic properties (from sonic)
- Fractures properties (P32, compliances, orientation)



- Defect compliance tensor [Kachanov 1980, Sayers & Kachanov 1992 ...]

$$\mathcal{H}_{ijkl} = P_{32} \left( (B_N - B_T) n_i n_j n_k n_l + \frac{B_T}{4} (n_i n_l \delta_{jk} + n_i n_k \delta_{jl} + n_j n_l \delta_{ik} + n_j n_k \delta_{il}) \right)$$

- Grid-scale Properties

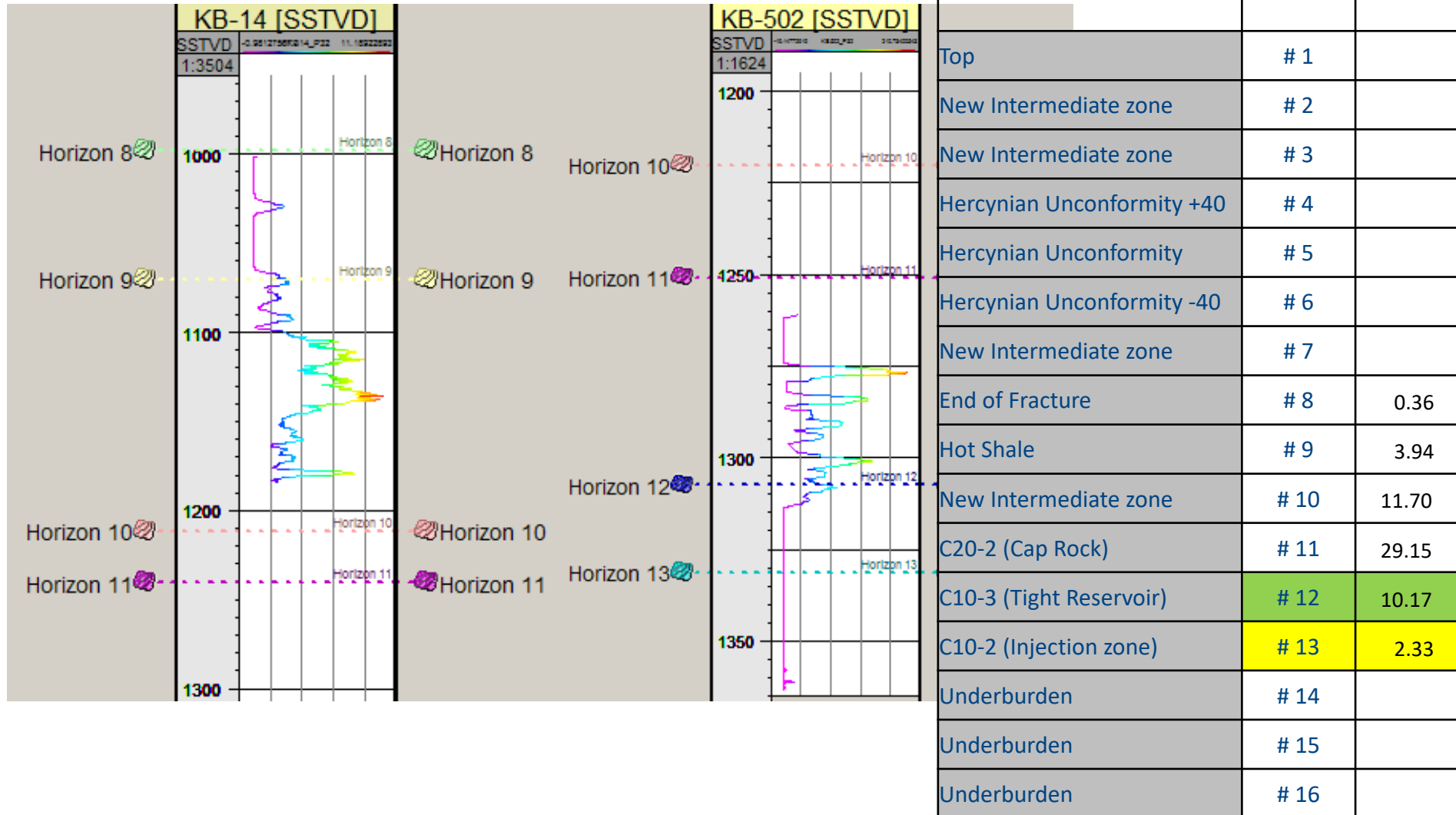
Elastic Compliance

$$\mathbf{M} = \mathbf{M}_m + \mathcal{H}$$
$$\mathbf{L} = \mathbf{M}^{-1}$$

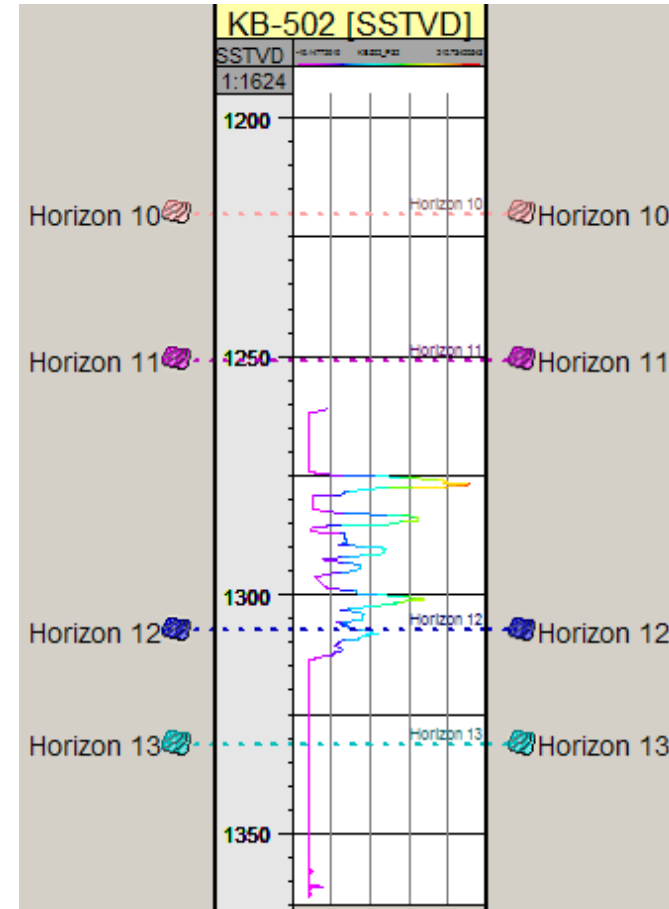
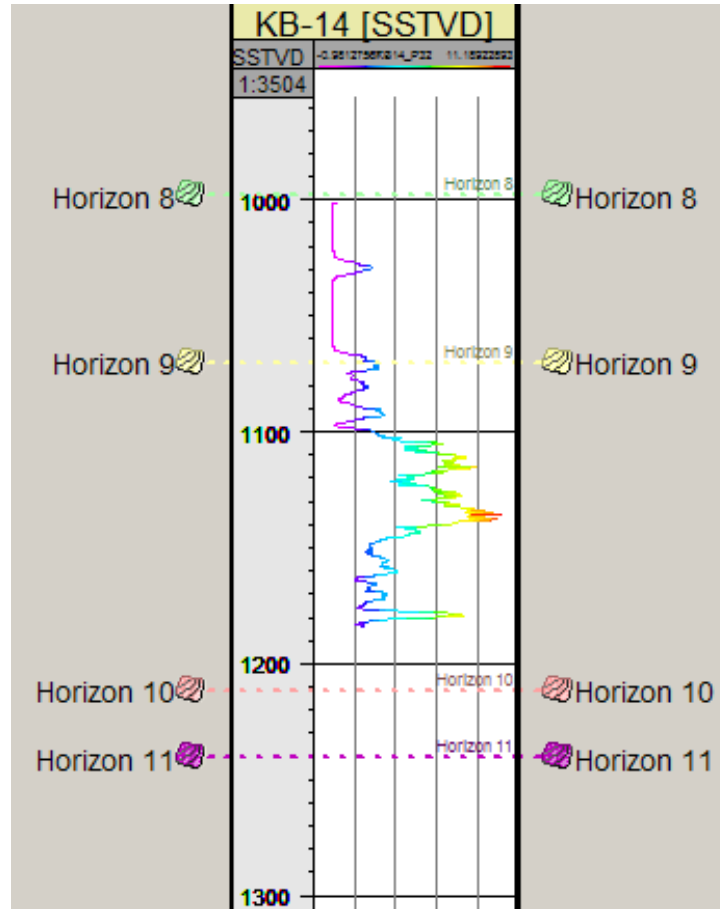
Biot's coefficients

$$\mathbf{b}_M = \mathbf{L} \mathbf{M}_m \mathbf{I} \mathbf{b}_m$$
$$\mathbf{b}_F = \mathbf{L} \mathcal{H} \mathbf{I}$$

# Fracture Intensity P32: Derived from FMI



# Fracture Intensity P32: Derived from FMI



	End of Fracture	Hot Shale	New Intermediate zone	C20-2 (Cap Rock)	C10-3 (Tight Reservoir)	C10-2 (Injection zone)
<b>Zone ID</b>	# 8	# 9	# 10	# 11	# 12	# 13
<b>P32</b>	0.36	3.94	11.7	29.15	10.17	2.33

# Fracture Compliance

Layer ID	P32	A = 0.1m		A = 0.25m		A = 0.5m		A = 1.0m	
		Bn m/GPa	Bs m/GPa	Bn m/GPa	Bs m/GPa	Bn m/GPa	Bs m/GPa	Bn m/GPa	Bs m/GPa
# 8	0.36	0.0209	0.0252	0.0523	0.0631	0.1047	0.1261	0.2094	0.2522
# 9	3.94	0.0163	0.0190	0.0407	0.0476	0.0813	0.0951	0.1627	0.1903
# 10	11.70	0.0164	0.0190	0.0409	0.0476	0.0818	0.0952	0.1637	0.1903
# 11	29.15	0.0159	0.0190	0.0399	0.0474	0.0797	0.0949	0.1594	0.1898
# 12	10.17	0.0149	0.0175	0.0373	0.0439	0.0746	0.0877	0.1491	0.1754
# 13	2.33	0.0152	0.0178	0.0379	0.0446	0.0758	0.0892	0.1516	0.1783

Fracture compliance is modeled by assuming open penny-shaped fractures in the “intact” layer with different crack radius  $a = 0.1, 0.25, 0.5$  and  $1.0$  meters respectively. The crack radius is a proxy for the “open” length of the fracture at grid scale (fracture surface is rough and the opening length is a proxy for its compliance).

# Grid-scale Properties (Including Fractures)

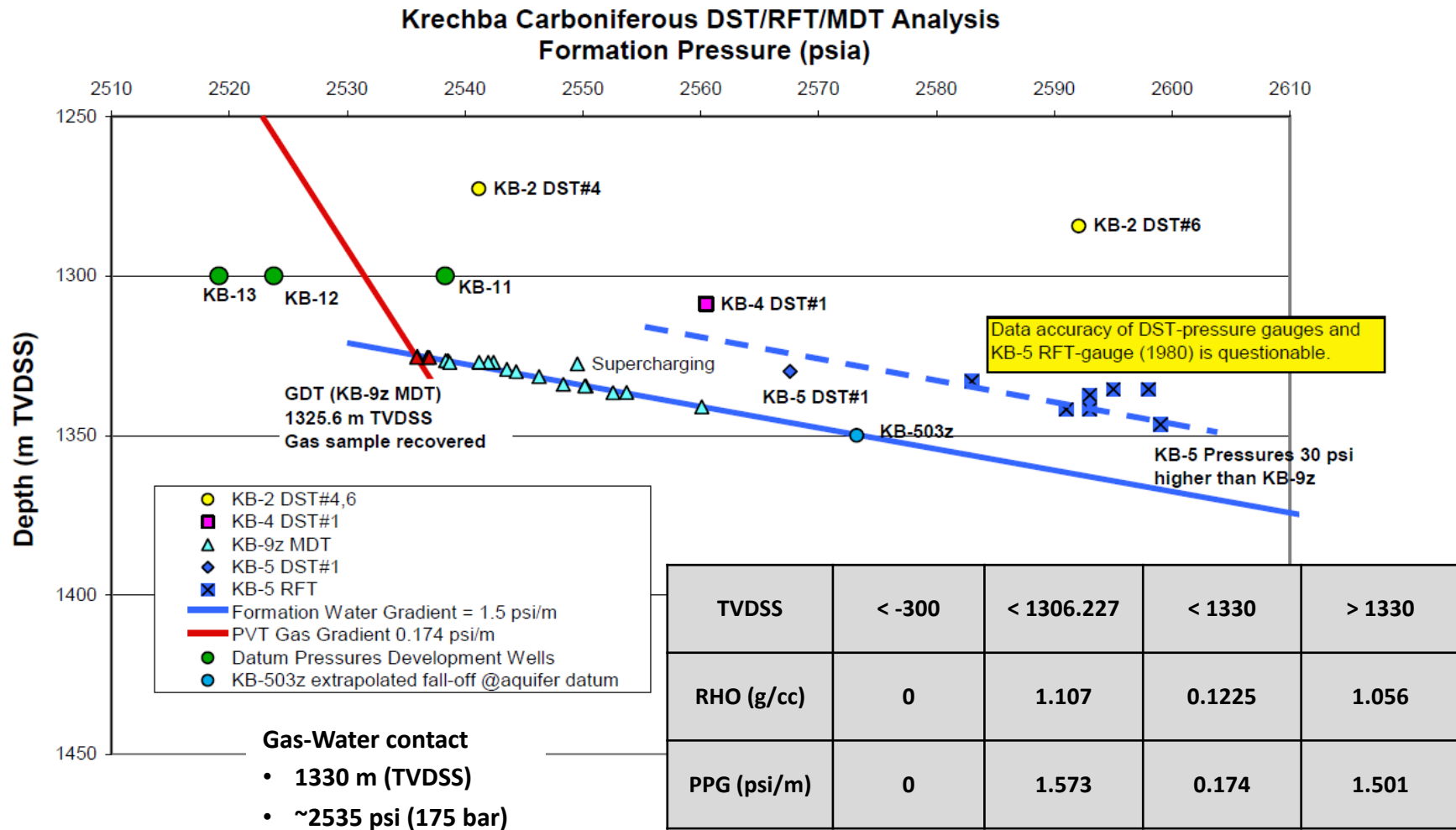
Layer ID	P32	A = 0 (Intact)		A = 0.1m		A = 0.25m		A = 0.5m		A = 1.0m	
		YME	PR	YME	PR	YME	PR	YME	PR	YME	PR
# 1		11.1	0.223	11.1	0.223	11.1	0.223	11.1	0.223	11.1	0.223
# 2		11.9	0.283	11.9	0.283	11.9	0.283	11.9	0.283	11.9	0.283
# 3		20.3	0.345	20.3	0.345	20.3	0.345	20.3	0.345	20.3	0.345
# 4		23.5	0.336	23.5	0.336	23.5	0.336	23.5	0.336	23.5	0.336
# 5		24.0	0.334	24.0	0.334	24.0	0.334	24.0	0.334	24.0	0.334
# 6		20.2	0.344	20.2	0.344	20.2	0.344	20.2	0.344	20.2	0.344
# 7		20.6	0.345	20.6	0.345	20.6	0.345	20.6	0.345	20.6	0.345
# 8	0.36	22.5	0.340	21.3	0.323	19.8	0.303	17.9	0.279	15.3	0.250
# 9	3.94	30.0	0.290	19.8	0.212	15.0	0.194	12.1	0.195	10.1	0.205
# 10	11.70	30.0	0.280	14.2	0.188	10.8	0.196	9.3	0.208	8.4	0.217
# 11	29.15	30.0	0.320	10.9	0.213	9.0	0.227	8.3	0.235	7.9	0.240
# 12	10.17	32.6	0.300	16.1	0.199	12.2	0.203	10.4	0.213	9.3	0.223
# 13	2.33	32.0	0.300	24.0	0.237	18.9	0.208	15.2	0.198	12.3	0.202
# 14		40.0	0.257	40.0	0.257	40.0	0.257	40.0	0.257	40.0	0.257
# 15		40.0	0.257	40.0	0.257	40.0	0.257	40.0	0.257	40.0	0.257
# 16		40.0	0.257	40.0	0.257	40.0	0.257	40.0	0.257	40.0	0.257

A is crack radius (in meter)

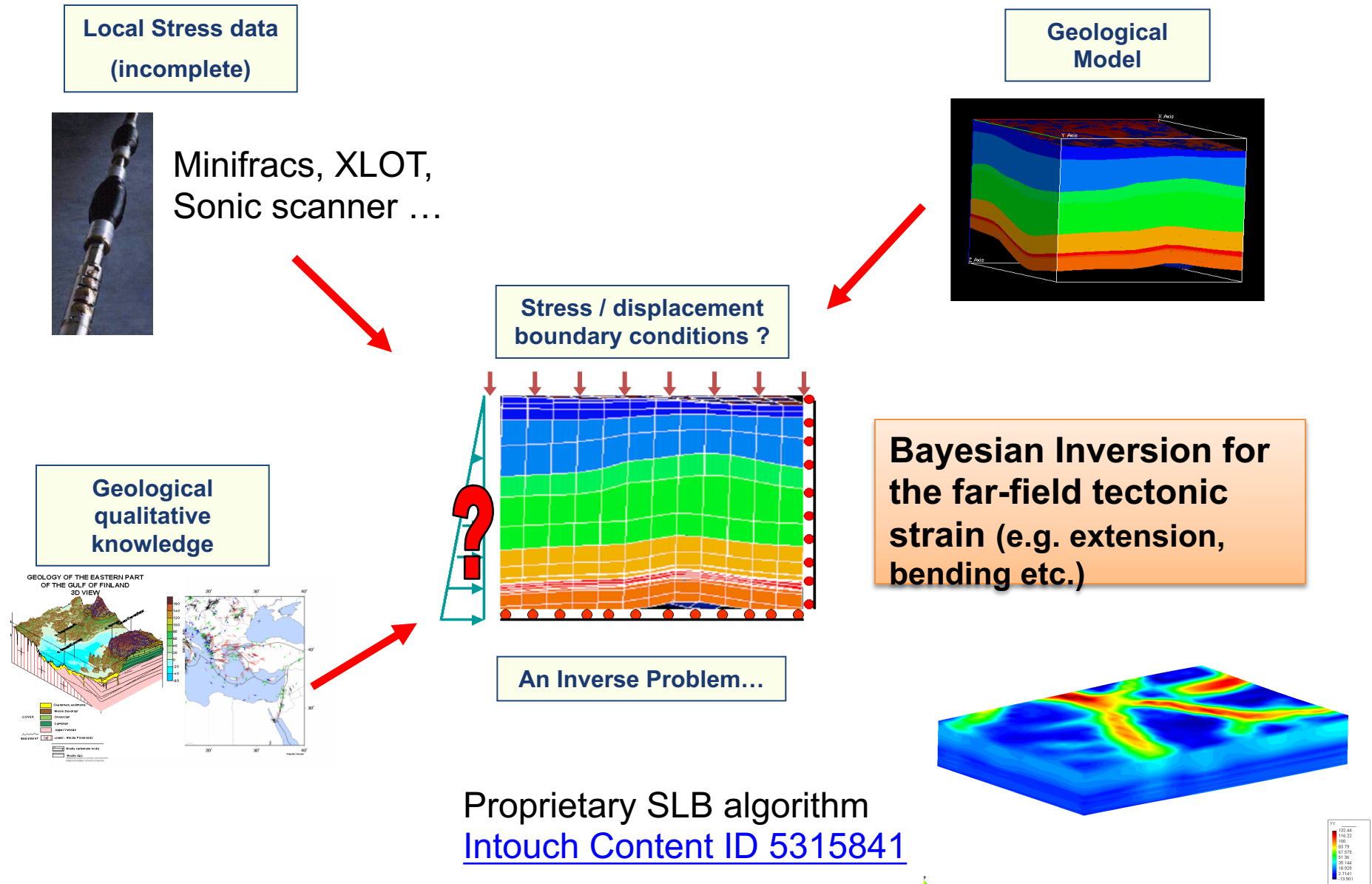


# Initialized Pore Pressure Distribution

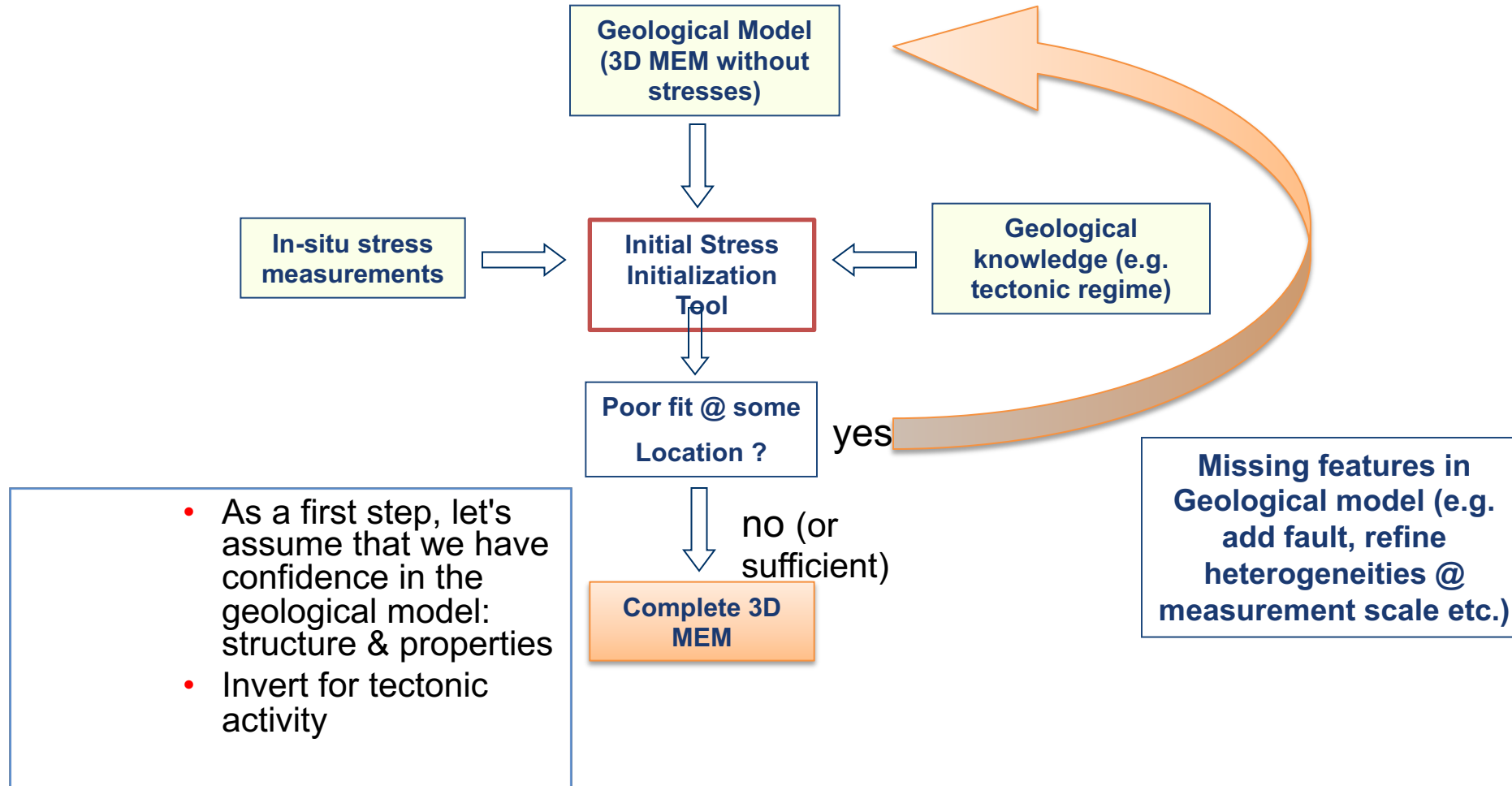
– PPG from BP's Review



# Initial Stress Reconstruction: Integrate all information



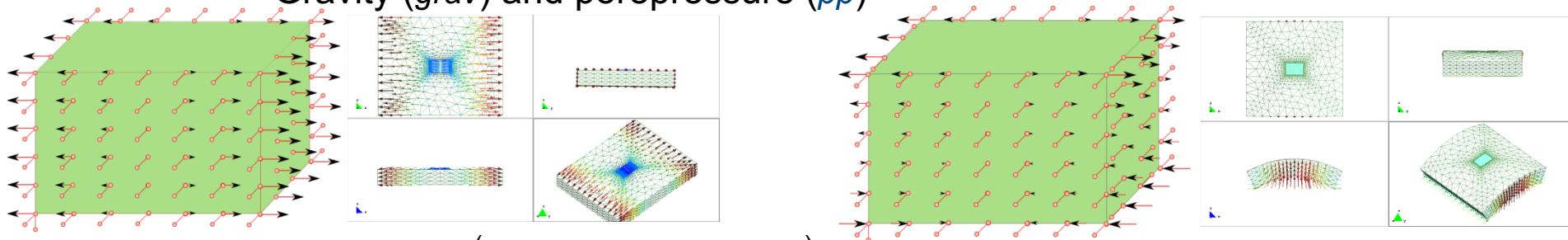
# Position in the Geomechanics simulation workflow



# Boundary conditions as unknowns

– Keep it simple !

- Horizontal constant strain BC: Shortening / extension modes via a 2D uniform strain tensor:  $e_x, e_y, e_{xy}$
- Linear gradient with depth for each of these variables (bending modes):  $f_x, f_y, f_{xy}$
- Gravity (*grav*) and porepressure (*pp*)

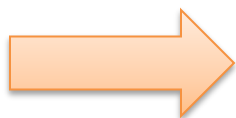


$$\mathbf{m} = (e_x, e_y, e_{xy}, f_x, f_y, f_{xy}) \quad 6 \text{ unknowns}$$

– Superposition of 8 Fundamental elastic problems:

- 1 gravity loading + 1 pore pressure loading + 6 tectonic loadings (unit intensity)
- Theorem of superposition in elasticity gives stress at any point  $x_j$ :

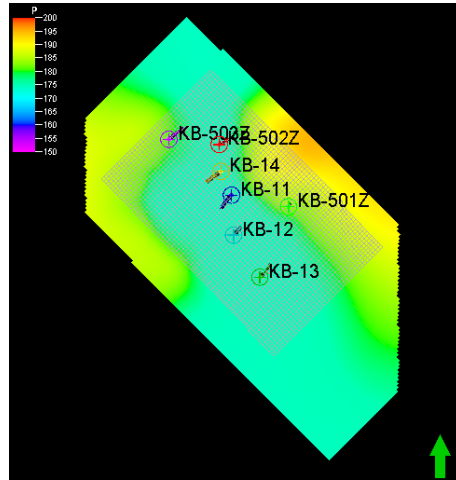
$$\boldsymbol{\sigma}(x_j, \mathbf{m}) = \boldsymbol{\sigma}^{grav}(x_j) + \sum_{q=1,6} m_q \times \boldsymbol{\sigma}^{tect.q}(x_j) + \boldsymbol{\sigma}^{pp}(x_j) - \alpha(x_j) Pp(x_j) \mathbf{I}$$



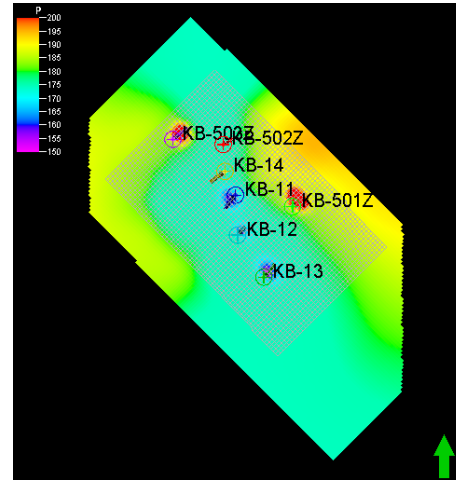
**Needs to solve *only* 8 elastic problems ! Computationally efficient**

# Evolution of Reservoir Pore Pressure: ECLIPSE

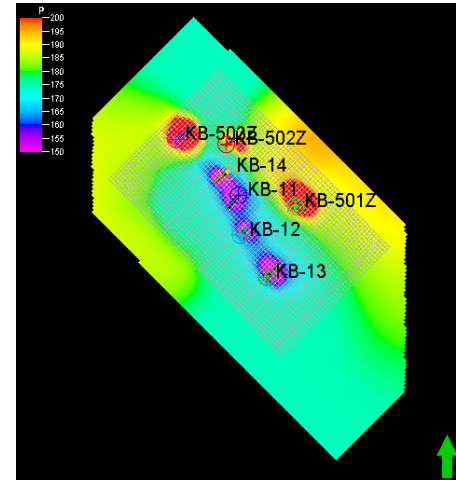
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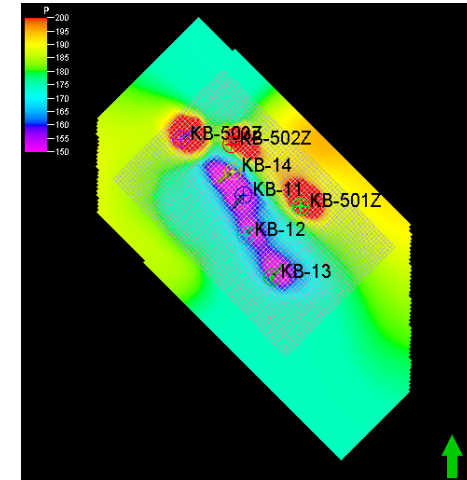
2004-07-31



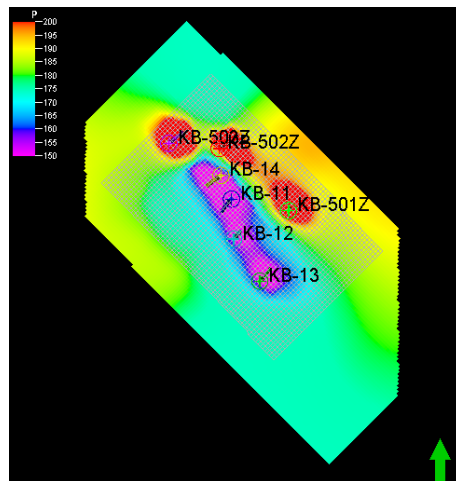
2005-01-22



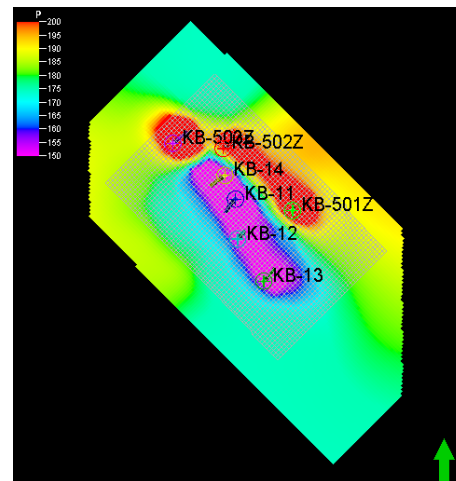
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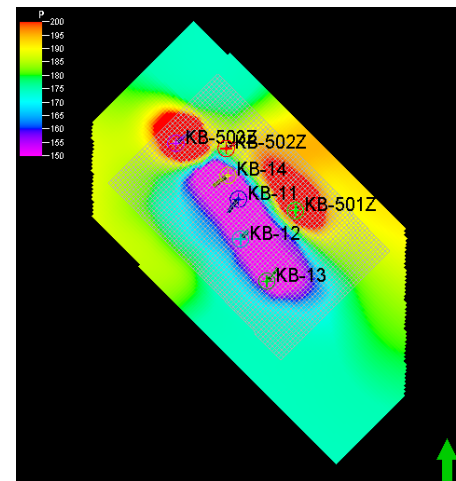
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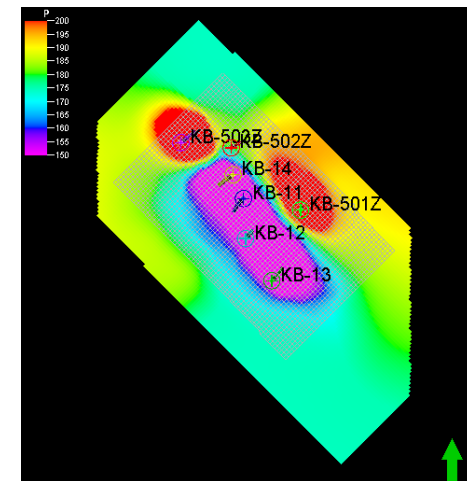
2007-01-27



2008-01-01



2009-01-31

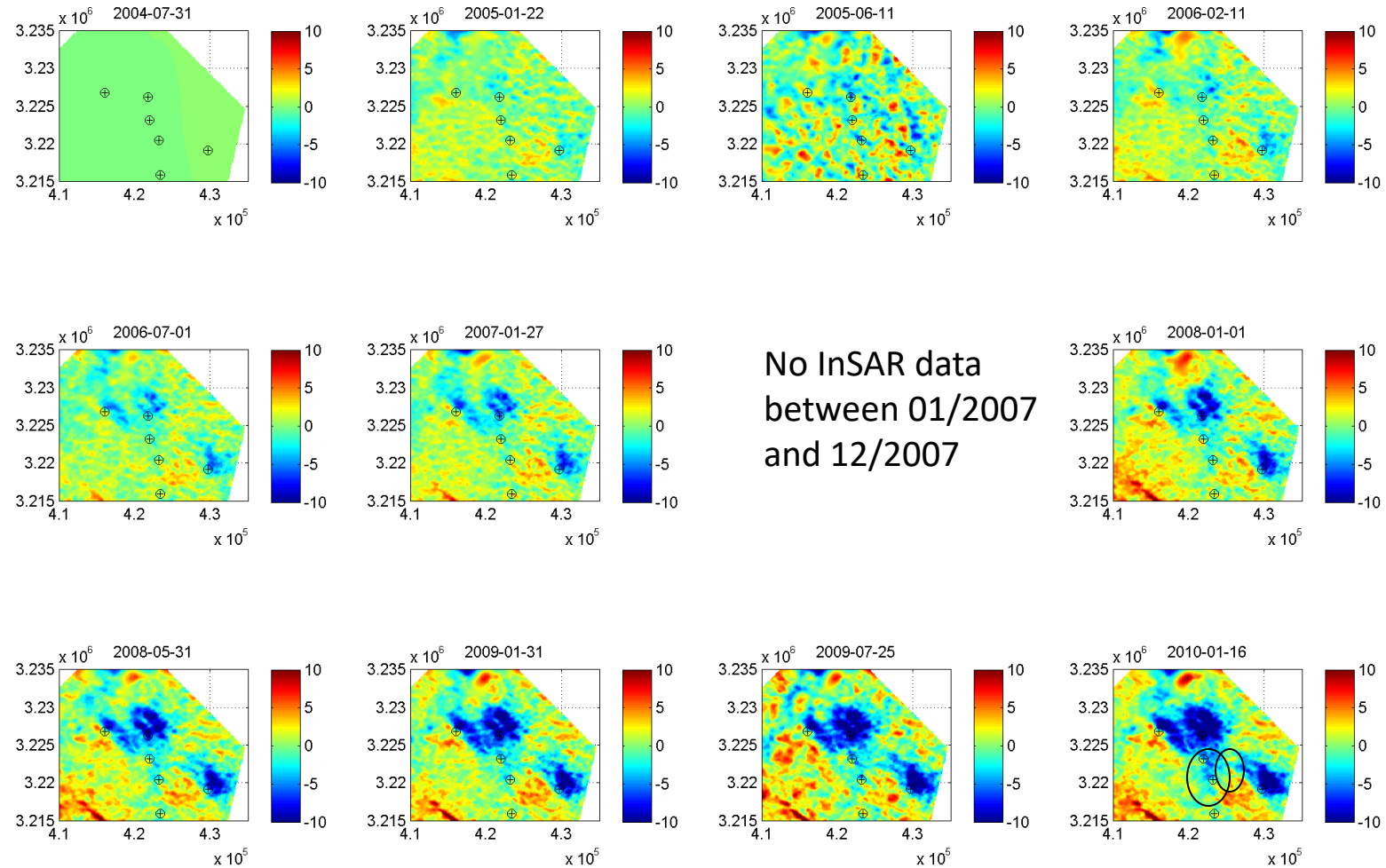


2010-01-16

# Difference measurements - predictions (LOS displacement): Model (a=0) vs InSAR

All scales in mm. Difference of the cumulative displacement from the start of the injection between measurements and predictions.

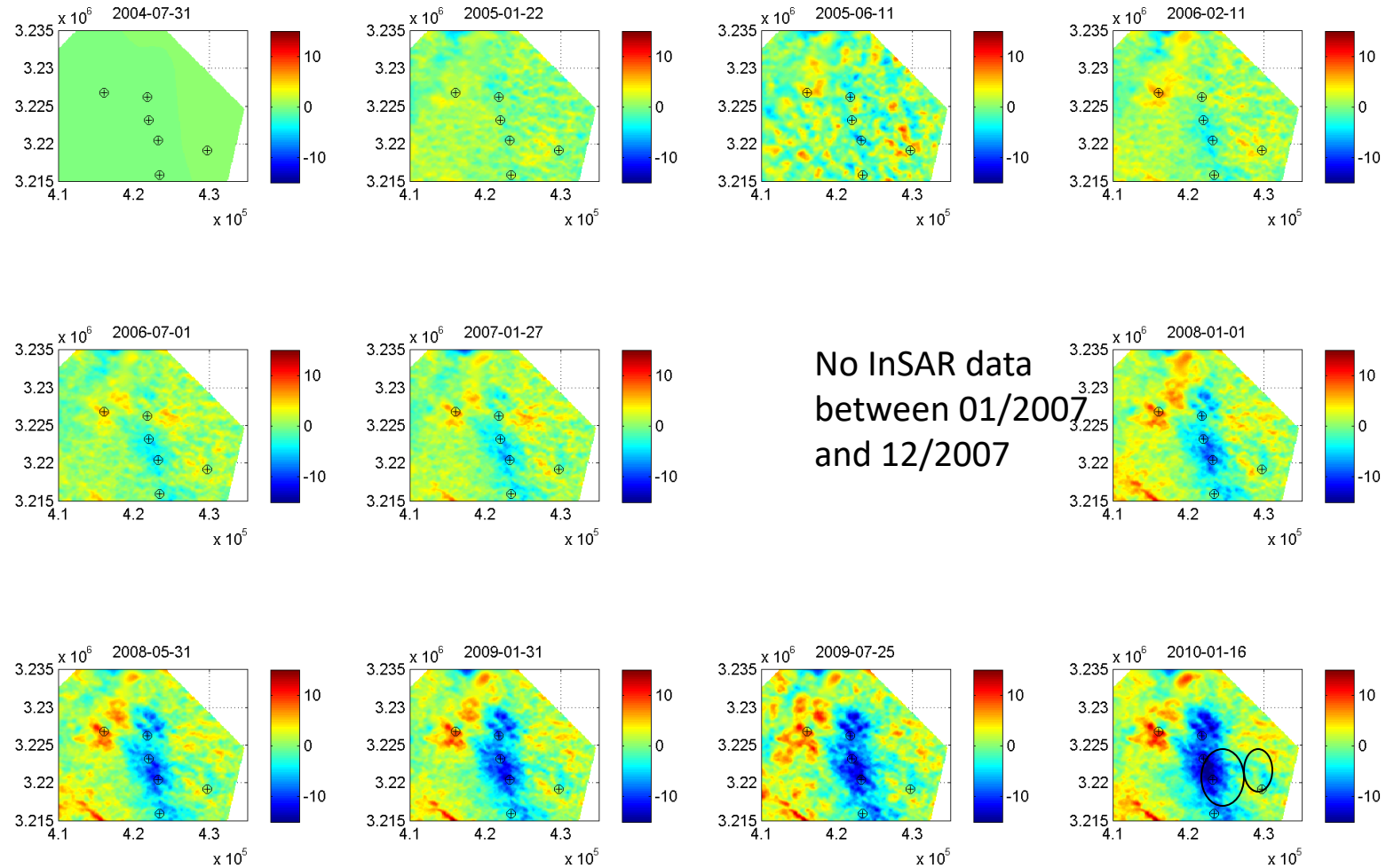
Ground motion  
(no open fractures):  
- *correctly* predicted in  
the production area  
- *underestimated* in the  
injection area



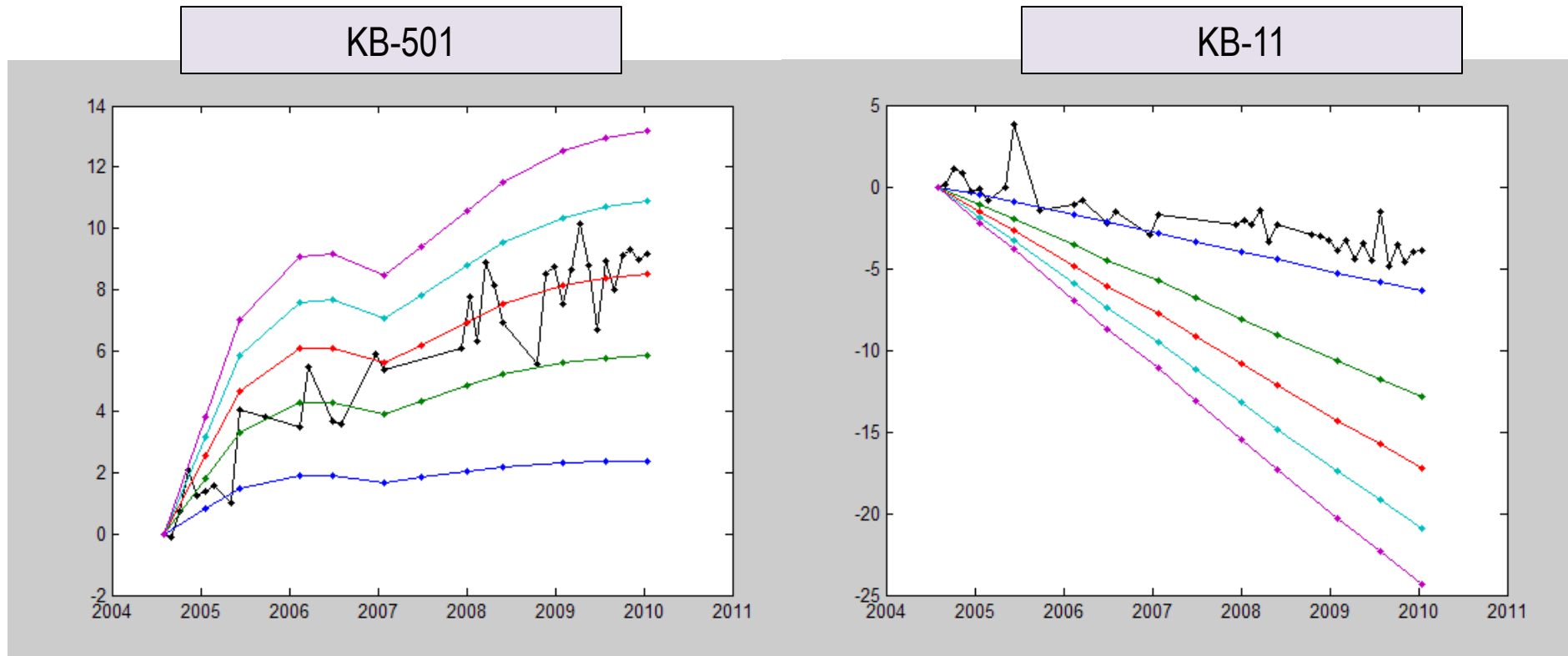
# Difference measurements - predictions (LOS displacement): Model (a=0.25) vs InSAR

All scales in mm. Difference of the cumulative displacement from the start of the injection between measurements and predictions.

Ground motion  
(no open fractures):  
- *correctly* predicted in  
the production area  
- *underestimated* in the  
injection area



# Time evolution of displacement at 2 locations



- The differences between the response of the injection (KB-501) and depletion (KB-11) zones clearly indicates a non-linear dependence of fracture compliance with effective stresses. Fracture compliance remains negligible in the depletion zone (i.e. “closed” fractures) but increase significantly in the injection zone (i.e. “opening” of fractures).